



C.A.R.E. PHYS 213 Quiz 1

Review Session



CARE/CARE PHYS 213 Exam Review Session

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Welcome

Tutors

Tuesday

Workshop

Slides

Solutions

Also, here

install

Jupyter

Good luck



session!

during these times:

in the test. If you do not have a Jupyter Notebook environment, try suggestion for this coding example!

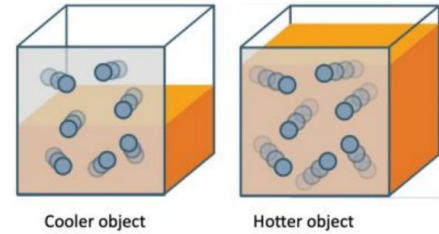
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Units for the Exam

- Internal Energy
- Temperature
- Heat Capacity
- Entropy

Internal Energy

- Total energy is **ALWAYS** conserved



- Positive work on a system increases the system's internal energy
- Higher temperature → More Internal Energy

- First law of thermodynamics:

$$\Delta U = W_{on} + Q$$

Change in
internal
energy

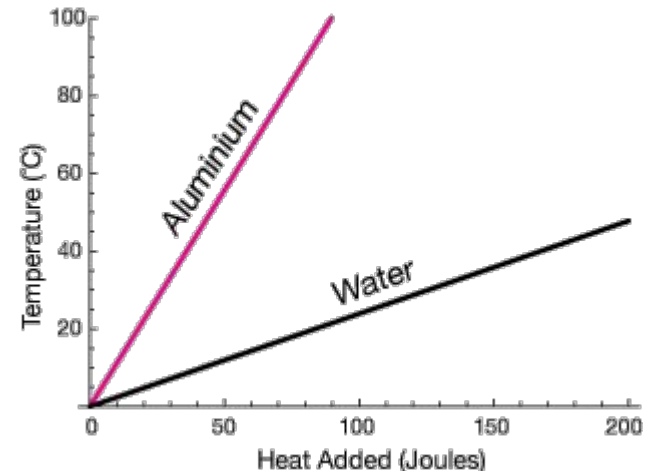
Work done
on the
system

Heat added
to the
system

Temperature & Heat Capacity

- **Heat Capacity (C)** - how much energy it takes to **increase** the temperature of a substance by 1 K/°C
 - Units of J/K
- **Larger C → More energy** is required to **increase the temperature** of the object
- Water has a larger heat capacity than Aluminum

$$C = dQ/dT$$

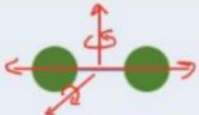
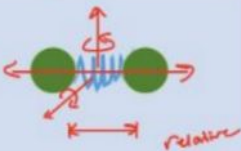
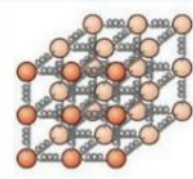


Types of Heat Capacity

- **Molar Heat Capacity [J/mol K]:** The amount of heat required to raise the temperature of **1 mole** of a substance by 1 K/°C
 - $c_{molar} = C/n$, where n is the number of moles
- **Specific Heat Capacity [J/kg K]:** The amount of heat required to raise the temperature of **1 kg** of a substance by 1 K/°C
 - $c = C/m$, where m is the mass [kg]
- **Heat Capacity at a Constant Volume and Constant Pressure:**
 - $C_v = dU/dT$
 - $C_p = dU/dT + p dV/dT$

Equipartition

Monatomic:
DOF = 3

Molecule	Degrees of freedom	U	C_v
	$N_{\text{DOF}} = 3$ x, y, z momentum	$U = \frac{3}{2} NkT$	$C_v = \frac{3}{2} Nk$
	$N_{\text{DOF}} = 5$ x, y, z momentum 2 rotation axes	$U = \frac{(3+2)}{2} NkT$	$C_v = \frac{5}{2} Nk$
	x, y, z momentum 2 rotation axes vibration mode (momentum+potential) $N_{\text{DOF}} = 7$	$U = \frac{(3+2+2)}{2} NkT$	$C_v = \frac{7}{2} Nk$
	x, y, z momentum x, y, z spring modes	$U = \frac{(3+3)}{2} NkT$	$C_v = 3Nk$

Solid:
DOF = 6

Equipartition & Heat Capacity

- Only need to memorize DOFs for monatomic gas, diatomic gas, and solids (3, 5, and 6, respectively)
- For substances under the **equipartition assumption**:

$$U = \frac{N_{\text{DOF}}}{2} NkT \implies C = \frac{dU}{dT} = \frac{N_{\text{DOF}}}{2} Nk$$

$$*Nk = nR$$

$$R = 8.314 \text{ J/(mol K)}$$

$$R = 0.08206 \text{ L atm/(mol K)}$$

Entropy

- Microstate vs Macrostate:
 - Microstate: individual, **specific** arrangement
 - Macrostate: property that arises from the microstates
 - **Many microstates can lead to the same macrostate**
 - Two people have the same weight (macrostate), but the distribution of the weight can be different (microstate)



Entropy (Cont.)

- Entropy (S) is a measure of the degree of 'diversity' associated with a macrostate
 - $S = k \ln(\Omega)$, where Ω is the number of microstates
 - **Second Law of Thermodynamics: $\Delta S \geq 0$**
- Equilibrium
 - Occurs when the macrostate of the system ceases to change
 - The **most probable macrostate** is the one with the **highest entropy (most microstates)**
 - **Equilibrium** is achieved when **S , entropy, is maximized**

Binomial Coefficient

If I have **N coins** and I am looking for the macrostate with **q heads**, the number of microstates:

$$\binom{N}{q} = \frac{N!}{q!(N-q)!}$$

Example: If I have **20 coins**, how many microstates are associated with the macrostate of getting **7 heads**?

Answer:

Binomial Coefficient

If I have **N coins** and I am looking for the macrostate with **q heads**, the number of microstates:

$$\binom{N}{q} = \frac{N!}{q!(N-q)!}$$

Example: If I have **20 coins**, how many microstates are associated with the macrostate of getting **7 heads**?

Answer:

$$\binom{20}{7} = \frac{20!}{7!(20-7)!} = 77520$$

Entropy (Cont.) - Dice Example

- **Microstate:**

- **Macrostate:**

- What is the most likely macrostate?

-

-

- What is the macrostate with the highest entropy?

-

- Entropy of a macrostate is simply a measure of the number of microstates associated with it

- More microstates → Higher Entropy, Higher Probability

						
	2	3	4	5	6	7
	3	4	5	6	7	8
	4	5	6	7	8	9
	5	6	7	8	9	10
	6	7	8	9	10	11
	7	8	9	10	11	12

Entropy (Cont.) - Dice Example

- **Microstate:** set of individual die values
- **Macrostate:**
- What is the most likely macrostate?
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Entropy (Cont.) - Dice Example

- **Microstate**: set of individual die values
- **Macrostate**: sum of die values
- What is the most likely macrostate?

○

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- What is the macrostate with the highest entropy?

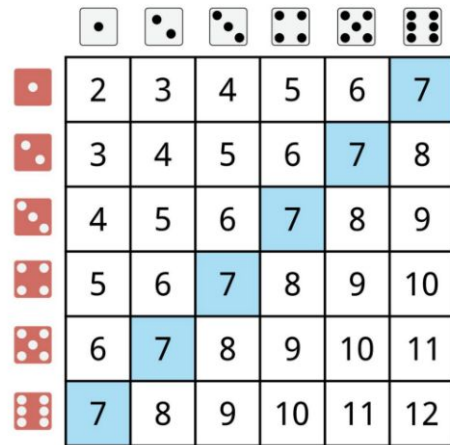
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Entropy (Cont.) - Dice Example

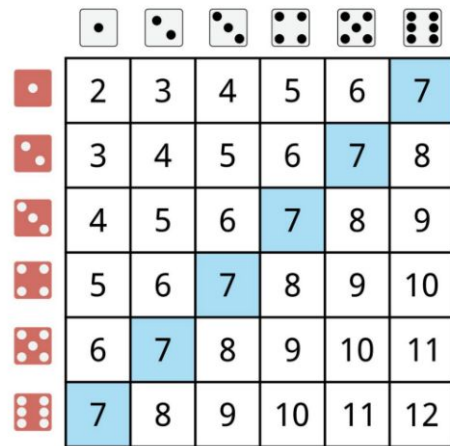
- **Microstate**: set of individual die values
- **Macrostate**: sum of die values
- What is the most likely macrostate?
 - 7: has the largest number of microstates associated with it
 - Probability = $6/36 = 0.167$
- What is the macrostate with the highest entropy?
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Entropy (Cont.) - Dice Example

- **Microstate**: set of individual die values
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- What is the most likely macrostate?
 - 7: has the largest number of microstates associated with it
 - Probability = $6/36 = 0.167$
- What is the macrostate with the highest entropy?
 - Again, 7: has the largest number of microstates associated with it
- Entropy of a macrostate is simply a measure of the number of microstates associated with it
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Important Equations

Start with the definition
of temperature

$$\frac{1}{T} \equiv \left(\frac{\partial S}{\partial U} \right)_{V,N}$$

multiply by dU

$$\frac{1}{T} dU = dS$$

integrate

$$\Delta S = \int_{U_i}^{U_f} \frac{1}{T} dU$$

plug dU into ΔS

$$\Delta S = \int_{T_i}^{T_f} \frac{C_V(T)}{T} dT$$

Or the definition of
heat capacity

$$C_V = \left(\frac{dQ}{dT} \right)_{V,N}$$

at constant volume
 $dQ = dU$

$$C_V = \left(\frac{dU}{dT} \right)_{V,N}$$

multiply by dT

$$C_V dT = dU$$

multiply by dT

$$C_V dT = dQ$$

integrate

$$\Delta U = \int_{T_i}^{T_f} C_V(T) dT$$

Differential Manipulation

- Know these tricks!

$$C = \frac{\partial U}{\partial T} \implies \Delta U = \int_{T_i}^{T_f} C dT$$

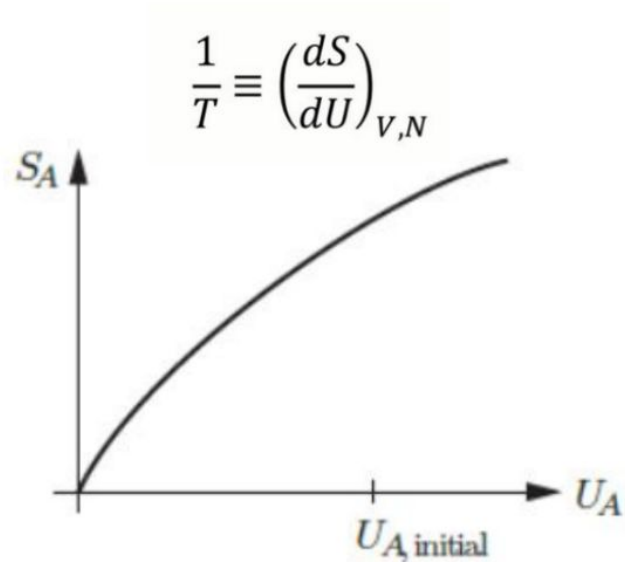
- Heat Capacity is the link between dU and dT

$$\frac{\partial S}{\partial U} = \frac{1}{T} \implies \Delta S = \int \frac{dU}{T} = \int_{T_i}^{T_f} \frac{C dT}{T}$$

- **If you know the heat capacity and the temperature change, you can find the change in internal energy and the change in entropy**

Entropy (S) vs. Internal Energy (U)

- Since slope is always positive, temperature is always positive
- **More energy = greater entropy**
- **Diminishing returns:** it gets harder and harder to increase the entropy as internal energy increases
- **Decreasing slope = increasing temperature**
 - **More energy means greater temperature**



Good luck!

Feel free to ask any
questions you may have.

You got this!

