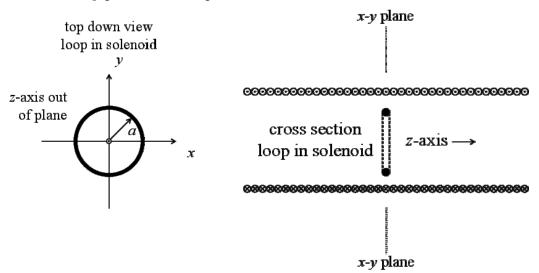
EMA Consider a wire loop of radius a and area $A_{\text{loop}} = \pi a^2$ that lies in the x-y plane. The loop has self inductance L and total resistance R.



- a) If the loop carries a current I(t) write down the expression involving L and perhaps A_{loop} that gives the magnetic flux Φ_{self} that passes through the loop and that is due to the current I(t).
- b) The loop is placed in long solenoid as shown in the figure. The solenoid has cross sectional area A_{solenoid} and N turns per meter. Compute the *mutual inductance* M of the solenoid and the loop.
- c) The solenoid is now driven by an alternating current so that it applies an external magnetic field $B_z = \operatorname{Re}(B_0 e^{i\omega t})$ perpendicular to the plane of the loop. This external field will induce an alternating current in the loop. Consider first the two extreme cases: R very large, and R = 0. How do you expect the *total* flux through the loop to vary with time in the these two cases? (Assume the current has been oscillating for a long time — *i.e.*, ignore any transient effects.)
- d) By considering all sources of flux through the loop, find an expression in terms of L, B_0 , a, ω and I(t) for the total EMF $\mathcal{E}(t)$ driving the current in the loop.
- e) Use your answer to part (d) to solve for current I(t) in the loop, and hence find the total flux $\Phi_{tot}(t)$ passing through the loop. Examine your answer to see if it agrees with your expectation from part (c).