

An electron is prepared in a superposition of two energy eigenstates, $\psi \propto (3\psi_1 + 4\psi_2)$. ψ_1 and ψ_2 are individually normalized wave functions, and have energies of $E_1 = 2$ eV and $E_2 = 7$ eV, respectively.

- a) [4 points] Suppose you measure the electron's energy. What result or results might you obtain?

2 eV and 7 eV

- b) [6 points] What are the probabilities of the various possible results?

$$P(E_1) = 9/25 \quad P(E_2) = 16/25$$

- c) [5 points] Suppose you were to measure the energies of a large number of particles that are each described by the wave function ψ . What will be the average value of your energy measurements?

$$\langle E \rangle = (9/25 * 2 + 16/25 * 7) \text{ eV} = 5.56 \text{ eV}$$

- d) [5 points] Consider the time dependence. At $t = 0$, the probability density is $P(x,0)$. When is the next time that the probability density $P(x,t)$ returns to its $t = 0$ value (i.e., $P(x,t) = P(x,0)$)? You should give a numerical answer, in seconds.

The interference term goes like $e^{i(\omega_1 - \omega_2)t}$ so we get back to the original $P(x,t)$ when $t = 2\pi/(\omega_1 - \omega_2) = h/(E_2 - E_1) = 8.27 * 10^{-16}$ sec.