

An electron is prepared in a superposition of two energy eigenstates,  $\psi \propto (3\psi_1 + 4\psi_2)$ .  $\psi_1$  and  $\psi_2$  are individually normalized wave functions, and have energies of  $E_1 = 2$  eV and  $E_2 = 7$  eV, respectively.

- a) [4 points] Suppose you measure the electron's energy. What result or results might you obtain?

2 eV and 7 eV

- b) [6 points] What are the probabilities of the various possible results?

$$P(E_1) = 9/25 \quad P(E_2) = 16/25$$

- c) [5 points] Suppose you were to measure the energies of a large number of particles that are each described by the wave function  $\psi$ . What will be the average value of your energy measurements?

$$\langle E \rangle = (9/25 * 2 + 16/25 * 7) \text{ eV} = 5.56 \text{ eV}$$

- d) [5 points] Consider the time dependence. At  $t = 0$ , the probability density is  $P(x, 0)$ . When is the next time that the probability density  $P(x, t)$  returns to its  $t = 0$  value (i.e.,  $P(x, t) = P(x, 0)$ )? You should give a numerical answer, in seconds.

The interference term goes like  $e^{i(\omega_1 - \omega_2)t}$  so we get back to the original  $P(x, t)$  when  $t = 2\pi/(\omega_1 - \omega_2) = h/(E_2 - E_1) = 8.27 * 10^{-16}$  sec.