

Suppose that some gas (helium) is present at five parts per million in the atmosphere, at 300K. You want a 99% pure sample of it at 1 atm. About how much work must be done per mole to get that? (Ignore changes of F due to the other constituents.)

a) What's the difference in μ between the inside of the sample tank (containing the pure helium) and the outside? Which has a bigger μ ?

$$\mu(n,T) = kT \ln (n / n_T(T))$$

$$n_{\text{in}}/n_{\text{out}} = 0.99/5 \times 10^{-6} = 2 \times 10^5$$

$$\mu_{\text{in}} - \mu_{\text{out}} = kT \ln(n_{\text{in}} / n_{\text{out}}) = (4 \times 10^{-21} \text{ J}) \ln(2 \times 10^5) = 5 \times 10^{-20} \text{ J}$$

b) How much work is needed per mole of purified helium?

$$(5 \times 10^{-20} \text{ J}) (6 \times 10^{23}) = 3 \times 10^4 \text{ J}$$

c) Suppose we want to take advantage of semipermeable membrane technology. Can we avoid having to do any work to obtain our helium?

Consider this apparatus:

1) What is the equilibrium pressure of the helium in the box?

The helium pressure must be the same inside and outside: $p = 5 \times 10^{-6} \text{ atm}$.

2) How much work is needed to produce 1 mole of He at 1 atm?

You'll need to start with a vacuum box that is 2×10^5 times larger than you want, then compress it to get 1 atm.

$$\text{Using } W = \int P dV = nkT \ln(2 \times 10^5) = 6.02 \times 10^{23} k (300) \ln(2 \times 10^5) = 3 \times 10^4 \text{ J}$$