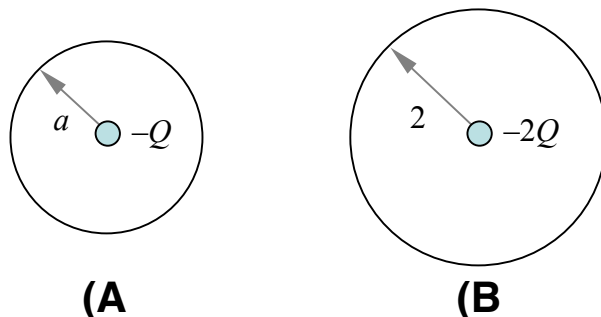


- 1) In figure **A**, a negative charge $-Q$ is located at the center of a sphere of radius a . In figure **B**, a negative charge $-2Q$ is at the center of a sphere of radius $2a$. Compare Φ_A , the flux through the sphere in Figure A, to Φ_B , the flux through the sphere in Figure B. (Remember the sign convention for flux through a closed surface: positive flux points *outwards*.) [4]



- (a) $\Phi_A < \Phi_B$ (b) $\Phi_A = \Phi_B$ (c) $\Phi_A > \Phi_B$

Flux = enclosed charge / ϵ_0

$$\Phi_A = -Q / \epsilon_0$$

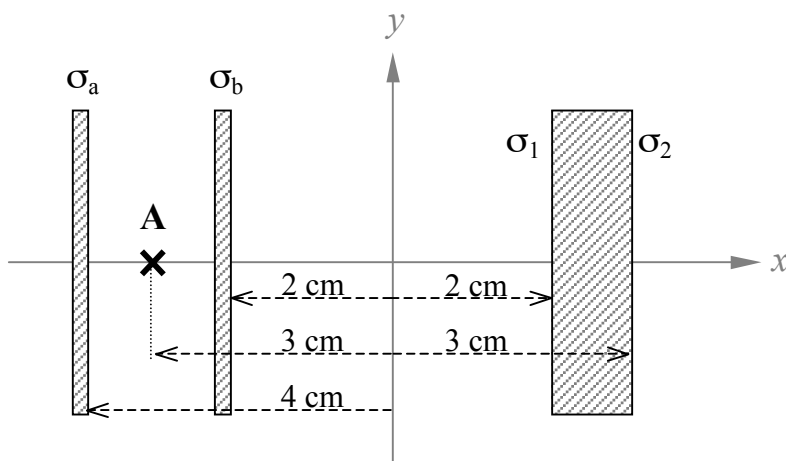
$$\Phi_B = -2Q / \epsilon_0$$

Therefore the correct answer is (c) $\Phi_A > \Phi_B$.

Award 2 points for the correct answer (a).

Award 2 points for correctly setting up Gauss's law, i.e. $\Phi_A = Q_{\text{enclosed}} / \epsilon_0$

Consider the three infinite metal slabs shown below. The left and middle slabs are very thin and carry surface charge densities of -3 C/m^2 and $+5 \text{ C/m}^2$ respectively. The right-hand plate has a thickness of 1 cm and carries no net charge.



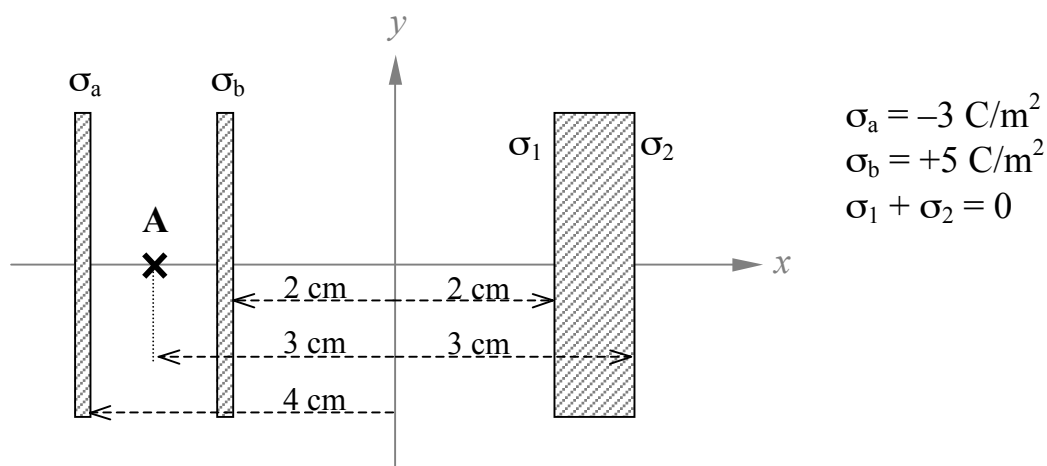
$$\begin{aligned}\sigma_a &= -3 \text{ C/m}^2 \\ \sigma_b &= +5 \text{ C/m}^2 \\ \sigma_1 + \sigma_2 &= 0\end{aligned}$$

- 2) What is the electric field \mathbf{E} at the point A due to the thick slab alone? Be sure to indicate both magnitude and direction. [4]

$\mathbf{E} = 0$ because the total charge on the thick slab is $Q = 0$.

Award 4 points for the correct answer $\mathbf{E}=0$.

- 3) What is the electric field at point A due to all three slabs? Be sure to give both magnitude and direction. [8]



$$\begin{aligned}
 \mathbf{E} &= +(\sigma_a - \sigma_b) / (2\epsilon_0) \\
 &= (-3 - 5) / (2\epsilon_0) \\
 &= -4.5 \times 10^{11} \text{ N/C (in the negative-} x \text{ direction)}
 \end{aligned}$$

4 points for setting up problem

2 points for correct solution

2 points for correct direction

- 4) What is the sign of σ_2 (the surface charge induced on the right-hand face of the thick slab)? You must supply a reason to receive credit. [4]

$\sigma_2 > 0$ because σ_b is positive and σ_a is negative, with $|\sigma_b| > |\sigma_a|$, which means the net E-field on the slab is in the positive x-direction and pushes positive charges to the right

2 points for correct answer and 2 points for correct explanation