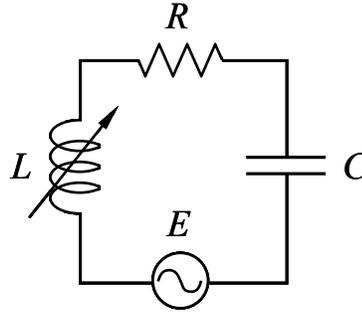


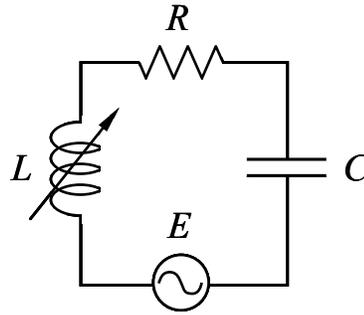
In the RLC circuit shown at right, the resistance  $R$  and capacitive reactance  $X_C$  are set to the given values. The inductor is of variable magnitude (indicated by the diagonal arrow). The AC generator puts out a peak EMF of  $\mathcal{E}_{\max} = 120 \text{ V}$ .



$$\begin{aligned} R &= 200 \, \Omega \\ X_C &= 400 \, \Omega \\ \mathcal{E}_{\max} &= 120 \text{ V} \end{aligned}$$

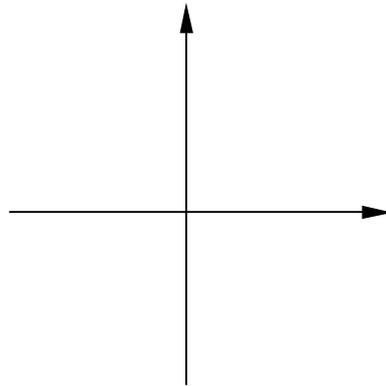
- 1) If the inductance is set to  $L = 300 \, \mu\text{H}$ , the circuit is in resonance. Given this information, calculate the capacitance  $C$  of the circuit and the frequency  $\omega$  of the generator. [5]
- 2) Leaving the frequency  $\omega$  and peak voltage  $\mathcal{E}_{\max}$  of the AC generator unchanged, the variable inductor is now changed to  $L = 200 \, \mu\text{H}$ . This puts the circuit off resonance. What is the phase angle  $\phi$  of the generator EMF with respect to the current? [4]
- 3) Does the generator EMF lead or lag the current when  $L = 200 \, \mu\text{H}$ ? Provide a brief but clear reason for your answer. [3]

- 4) What is the impedance  $Z$  of the final circuit (with  $L = 200 \mu\text{H}$ )? [4]



$$\begin{aligned} R &= 200 \Omega \\ X_C &= 400 \Omega \\ E_{\max} &= 120 \text{ V} \end{aligned}$$

- 5) Draw the voltage phasor diagram ( $E$ ,  $V_C$ ,  $V_L$ ,  $V_R$ ) for this final circuit, with the angles and lengths of the phasors indicated numerically. [4]



Q8A

$X_C = 1/\omega C$ . At Resonance,  $X_L = \omega_{res}L = X_C = 400\Omega$ .

1) So,  $\omega_{res} = 400\Omega / 300\mu\text{H} = 1.33 \times 10^6 \text{ rad/sec}$ . (5)

$C = 1/\omega X_C = 1.88 \text{ nF}$

Equation for  $X_C$  (1)

Equation for  $X_L$  (1)

Condition for resonance (1)

Solution for  $\omega_{res}$  (1)

Solution for  $C$  (1)

Numerical errors (-1, but only once per quiz)

2)  $X_L \Rightarrow \frac{200}{300} 400\Omega = 267\Omega \Rightarrow X_L - X_C = -133\Omega$  (4)  
 $\phi = \tan^{-1}\left(\frac{X_L - X_C}{R}\right) = -33.6^\circ = -0.59 \text{ rad}$

Equation for  $\phi$  (2)

New  $X_L$  (1)

Answer (1)

If  $X_C$  changes (-1)

Numerical errors (-1, but only once per quiz)

3)  $V$  lags  $I$ , because  $X_C > X_L$ . Alternatively, because  $\phi < 0$ .

This can be said in words, or graphically.

$V$  lags  $I$  (2)

Explanation (1)

No credit w/o explanation..

4)  $|Z| = \sqrt{R^2 + (X_L - X_C)^2} = 240\Omega$  (4)

Equation for  $|Z|$  (2)

Answer (2)

Numerical errors (-1, but only once per quiz)

Do not take off points for errors propagated from previous parts.

5) Magnitude of each  $V_i$ -phasor is  $I_{max}X_i = (\mathcal{E}/Z)X_i = \frac{1}{2}X_i$ .

$\mathcal{E}$ : 120 V,  $33.6^\circ$  below the  $+x$ -axis (1)

$V_C$ :  $\frac{1}{2}400 = 200$  V, down (along  $-y$ ) (1)

$V_L$ :  $\frac{1}{2}267 = 134$  V, up (along  $+y$ ) (1)

$V_R$ :  $\frac{1}{2}200 = 100$  V, to the right (along  $+x$ ) (1)

Equation for phasor magnitude (2)

Each correct phasor ( $\frac{1}{2}$ )

Numerical errors (-1, but only once per quiz)

Do not take off points for errors propagated from previous parts.