Your Comments

This stuff is fun and easy. I still think the lecture explained it all too quickly though.

I know all of this stuff from high school, I just need to review it a little because it's been a while.

I didn't understand were s` came from, which made all the questions really hard to answer.

I'm still a tad bit confused with virtual image. Is there no way to see this image then?

I think specific examples about how common geometric optical instruments work would be very helpful. → Lecture 28

Can you talk about how this relates to contact lenses? I can't really seem to grasp the concept and having an example would be very helpful. → Lecture 28

I want to appear in the comments section, I've tried since PHYS 211, come on!

End-of-Term and Exam Stuff

*There will be NO CLASS on Tuesday, Dec. 2.

*Homework Unit 27 ("Mirrors") is now due at 5pm on Wednesday, Dec. 10. Note that there is NO 80% extension on this HW.

* All old HW is now open for 70% credit through Dec. 10

- Make sure your gradebook is up to date! The last day to request an EX is Thursday, Dec. 11.

- **Final Exam dates are scheduled**: 12/19, 1:30-4:30pm (combined) and 12/16, 1:30-4:30pm (conflict). You will be automatically signed up for the combined exam; if you want to instead take the conflict you must sign up in the gradebook. Please email shunk@illinois.edu if you have a double conflict. The last day to register for a conflict exam is Wed., Dec. 10.

Exam 3: Wed. Dec. 3 at 7:00

- Covers material in Lectures 19 – 26
- Sign up in Gradebook for Conflict Exam at 5:15pm
- Link in Gradebook if you have a double-conflict

Exam Preparation:

- Study HW, Discussion, Checkpoints
- Old Exams are a good way to assess what you need to know
- Video Solutions of Spring 2013 Hour Exam 3 (Dec. 3 "optional HW")

Extra Office Hours:

- Mon., Tue., Wed. (see website for schedule and rooms)

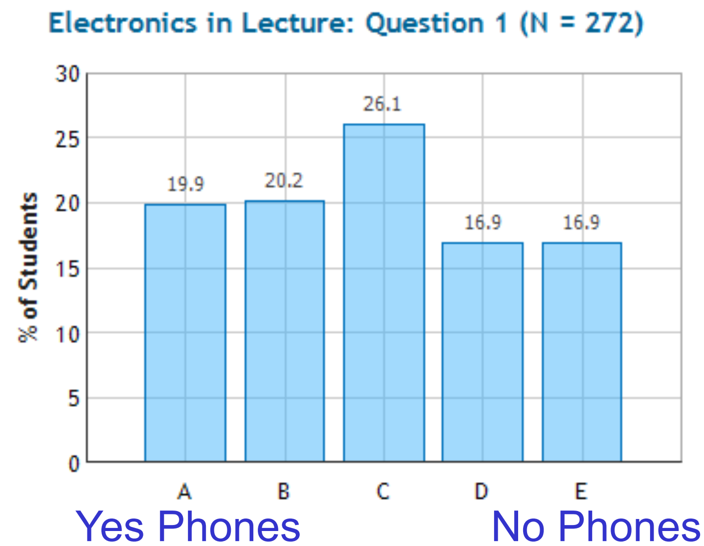
Electronics In Lecture Survey

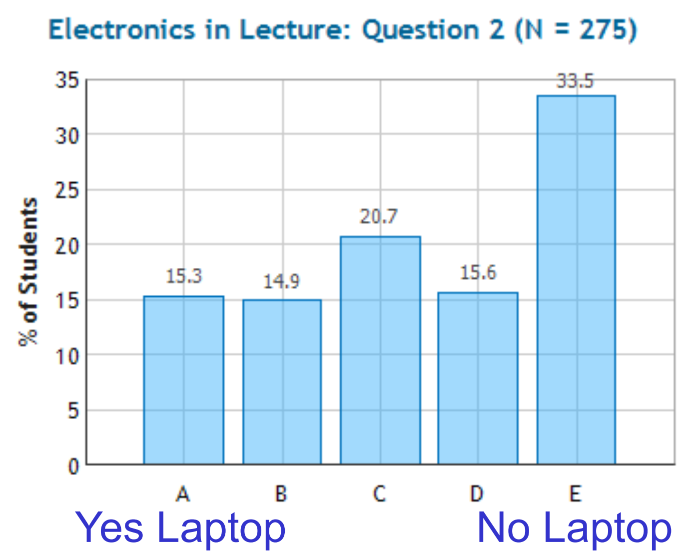
I prefer people not talk on their phones during lecture, but if they want to check texts or something of that manner, it isn't distracting. Laptops are almost always distracting.

I think phones are invaluable. I've left a lecture/ discussion because of family emergency, so I think cell phones should be available for it. Granted, some people use it for facebook and whatnot, but I think the pros outweigh the cons. Plus, a phone screen is less likely to attract attention than a monitor. No excuse to use a laptop. That's a fairly sized monitor asking people to look at whatever you're doing. I've seen people online shop instead of vote on an iClicker before. Call these people out! Come to learn!

laptops can help if we want to look back on the prelecture notes, online notes, etc

Just keep the lectures as quiet as possible. I have noticed that my physics lectures this year have been much more loud that in previous semesters. It's unfortunate people don't respect some lecturers until they kick a student out of class for the day.

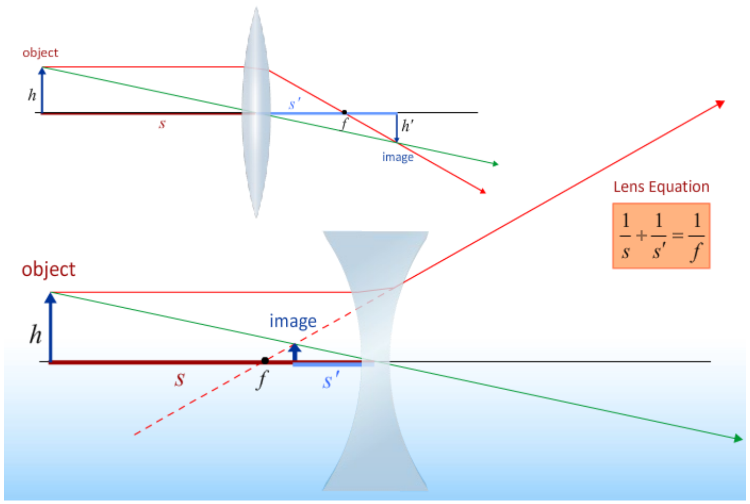




Physics 212
Lecture 26

Today's Concept:

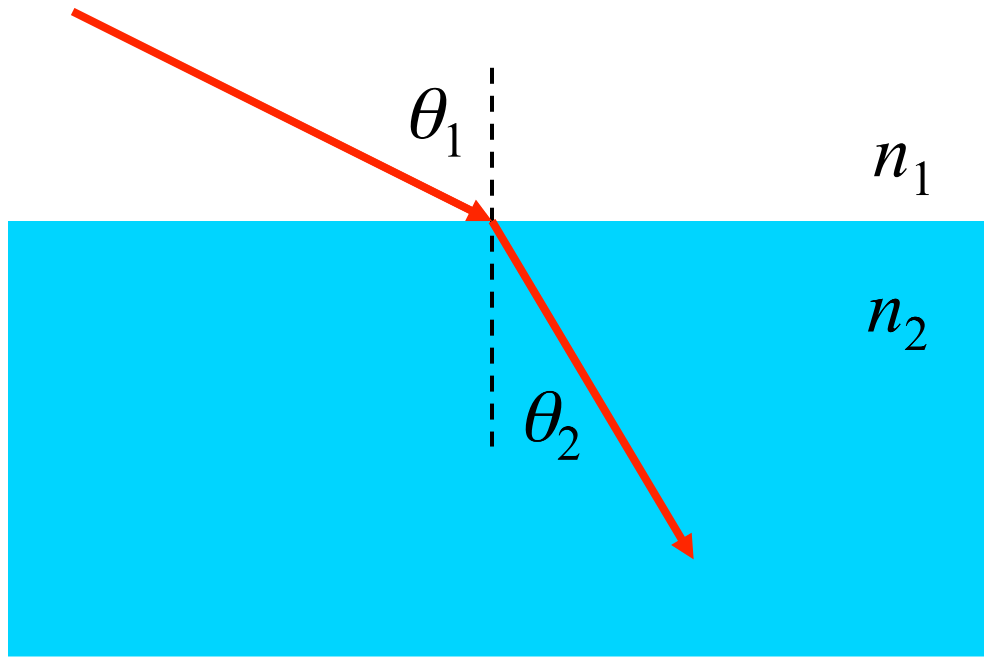
Lenses



Refraction

Snell's Law

$$n_1 \sin(\theta_1) = n_2 \sin(\theta_2)$$

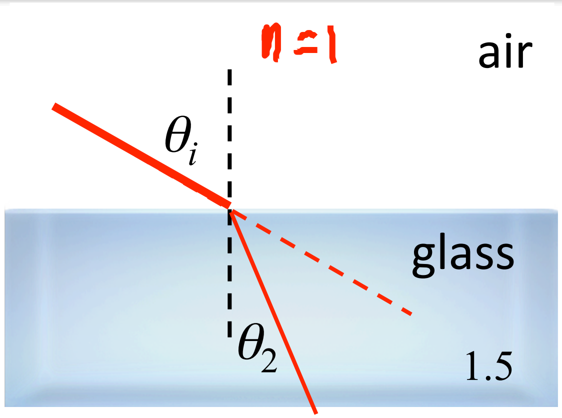


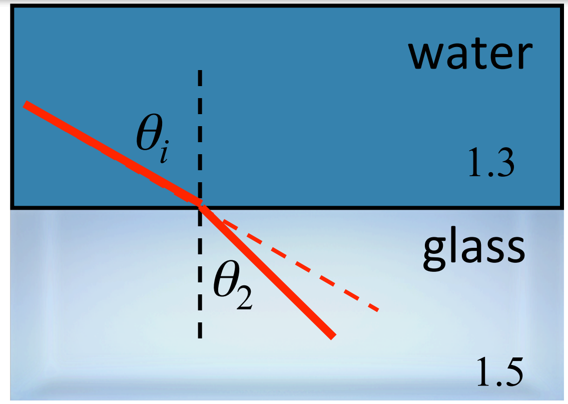
That's all of the physics –

everything else is just geometry!

CheckPoint

Case A





Case B

In Case A light in air heads toward a piece of glass with incident angle θ_i
In Case B, light in water heads toward a piece of glass at the same angle.

In which case is the light bent most as it enters the glass?

A) Case A
B) Case B
C) Same

The angle of refraction in bigger for the water – glass interface:

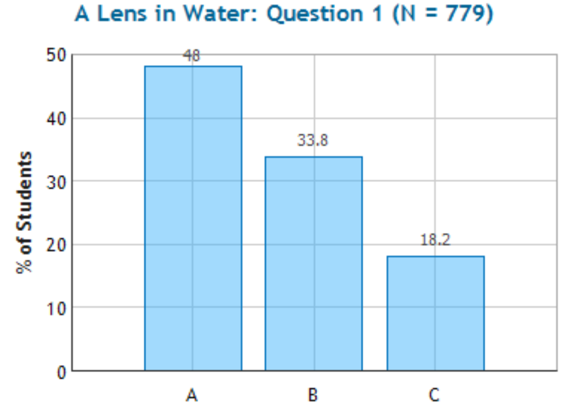
$$n_1 \sin(\theta_1) = n_2 \sin(\theta_2) \quad \longrightarrow \quad \sin(\theta_2)/\sin(\theta_1) = n_1/n_2$$

Therefore the BEND ANGLE $(\theta_1 - \theta_2)$ is BIGGER for air – glass interface

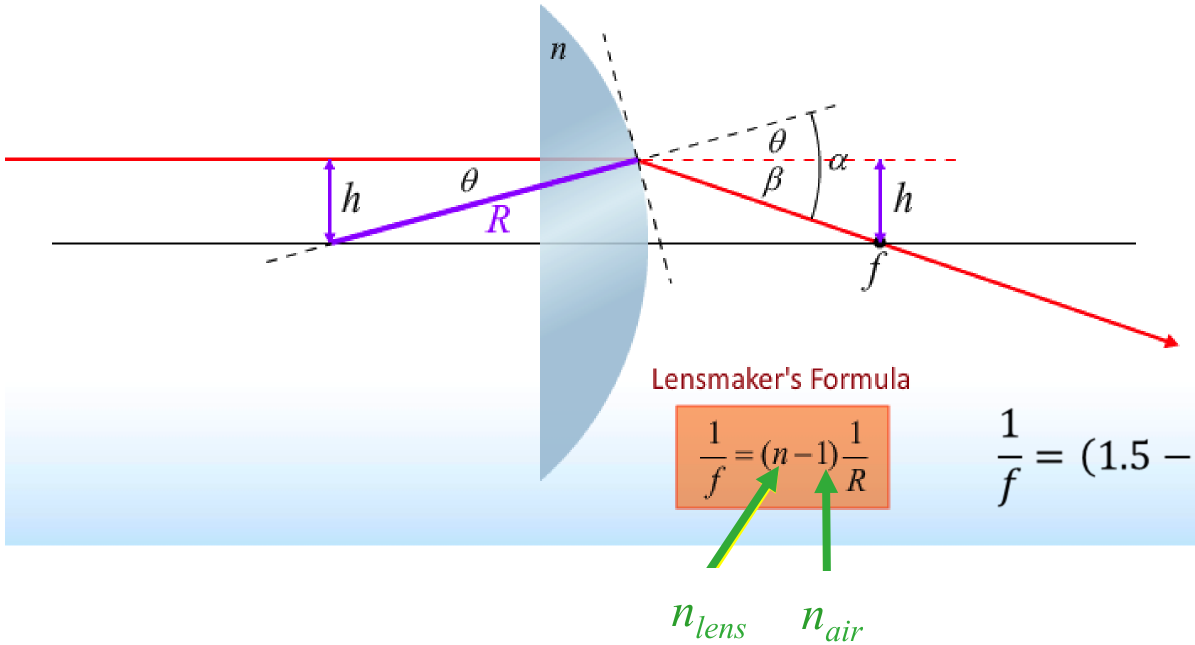
CheckPoint 2

What happens to the focal length of a converging lens when it is placed under water?

A. Increases
B. Decreases
C. Stays the same



We can see this also from Lensmaker's Formula

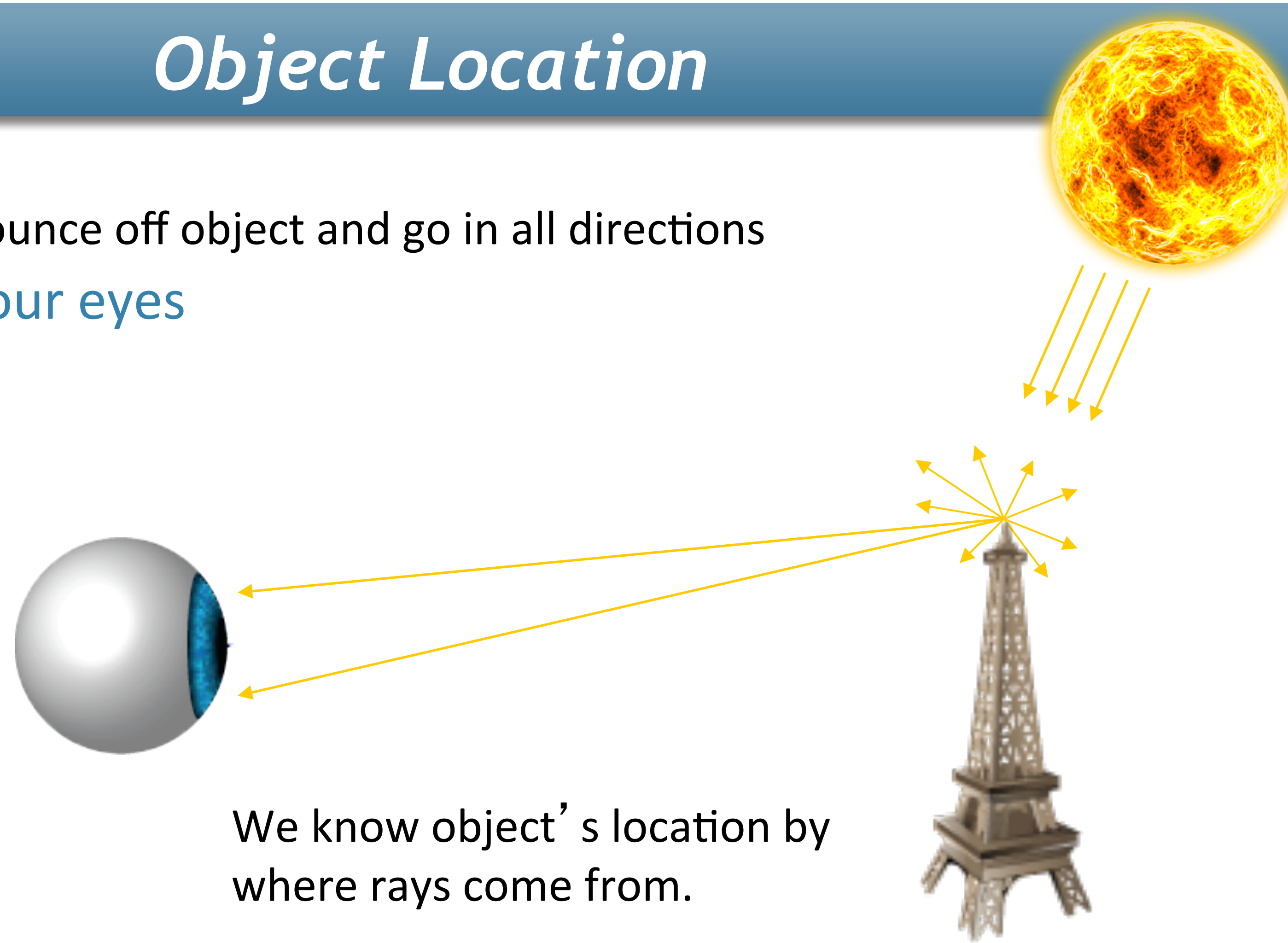


$$\frac{1}{f} = (1.5 - 1.1)\frac{1}{R} \Rightarrow \frac{1}{f} = (1.5 - 1.3)\frac{1}{R}$$

Object Location

Light rays from sun bounce off object and go in all directions

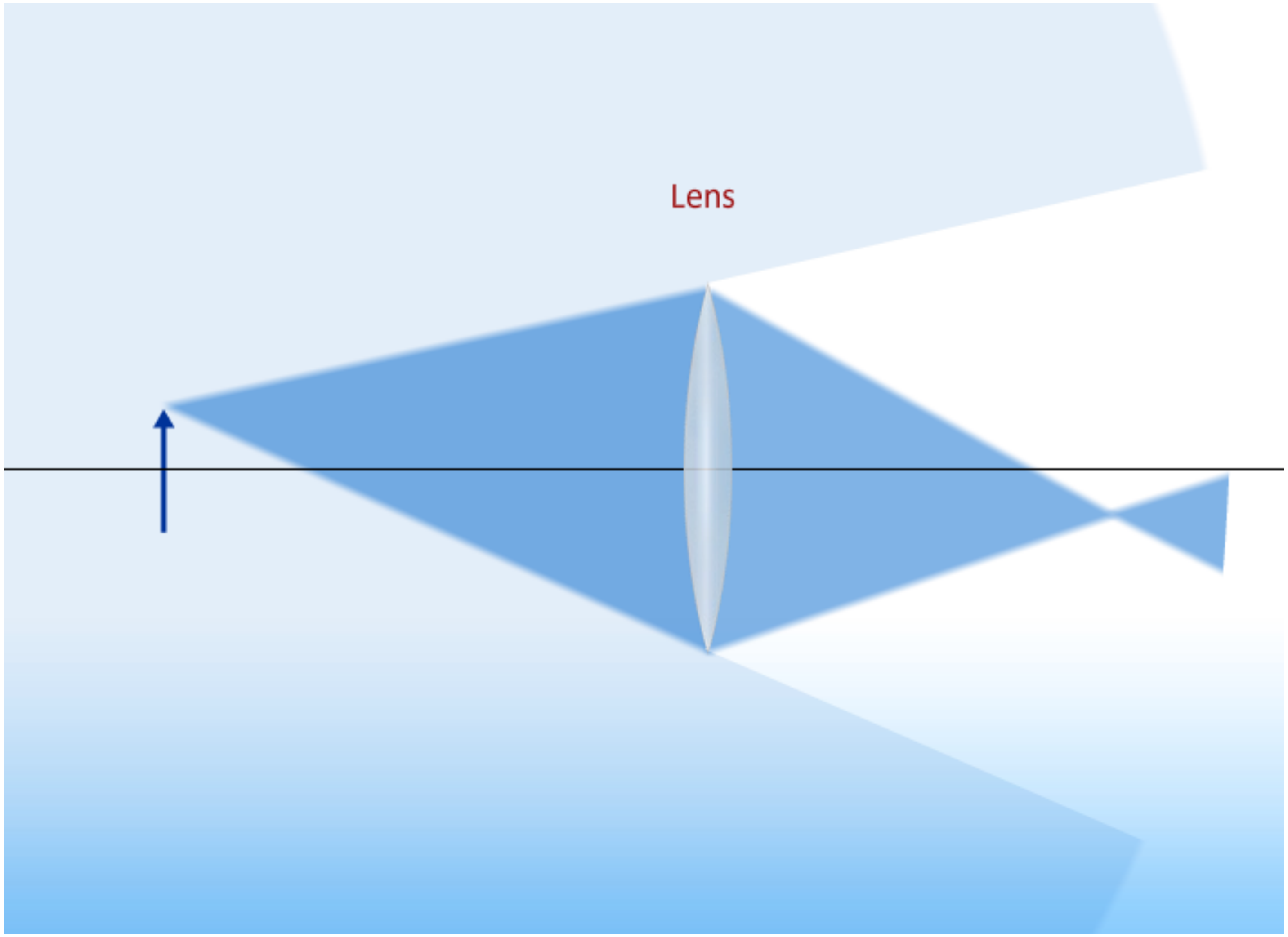
- Some hits your eyes



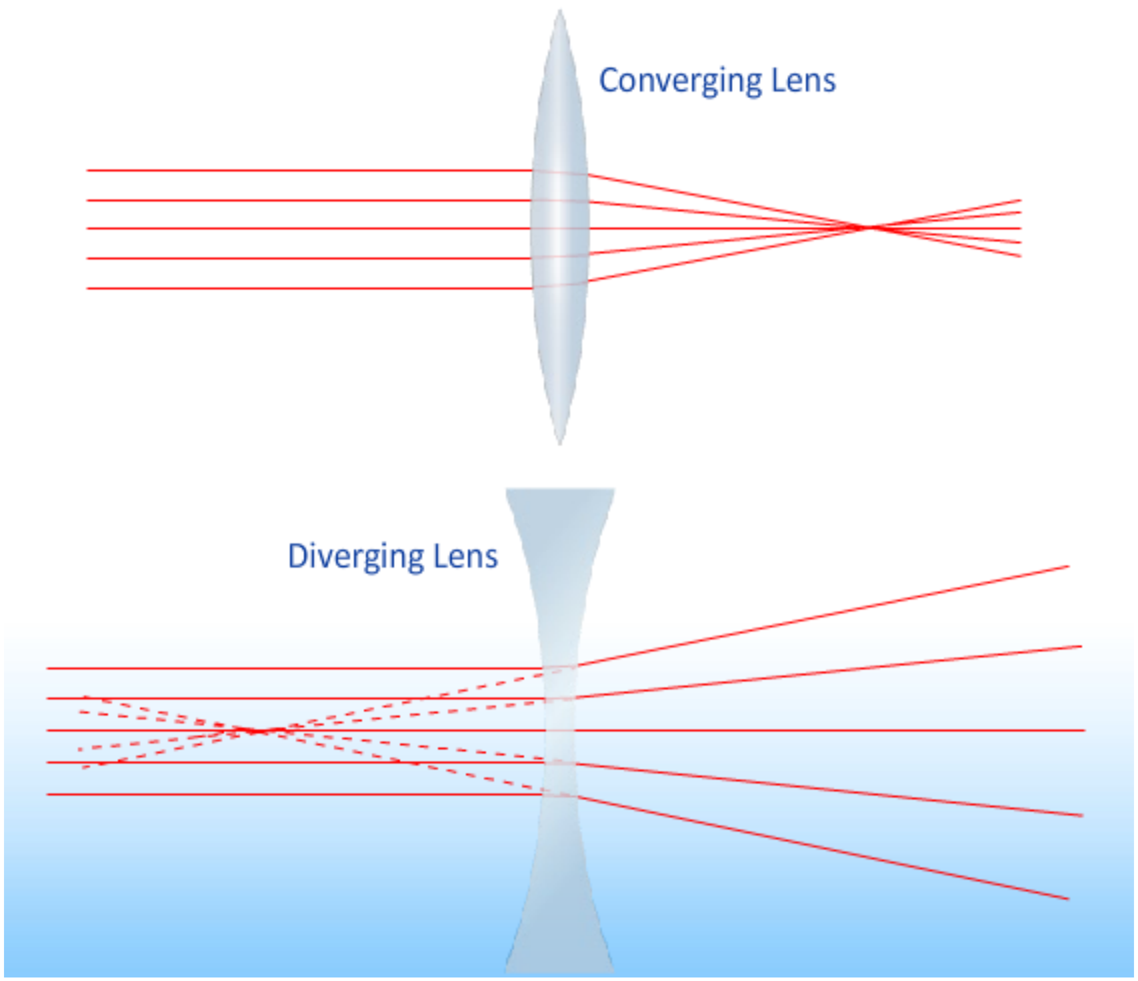
We know object's location by where rays come from.

We will discuss eyes in lecture 28…

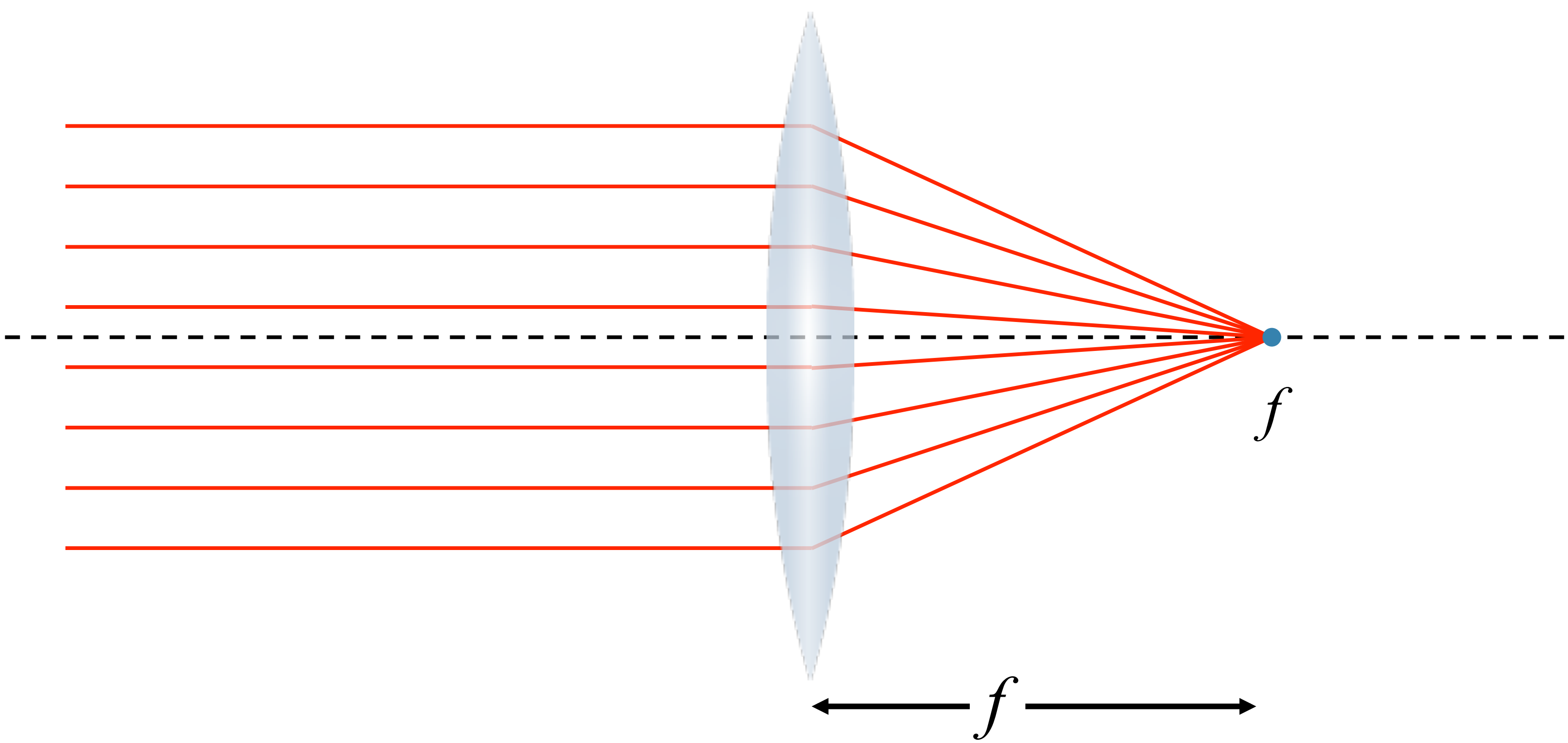
Waves from Objects are Focused by Lens



Two Different Types of Lenses



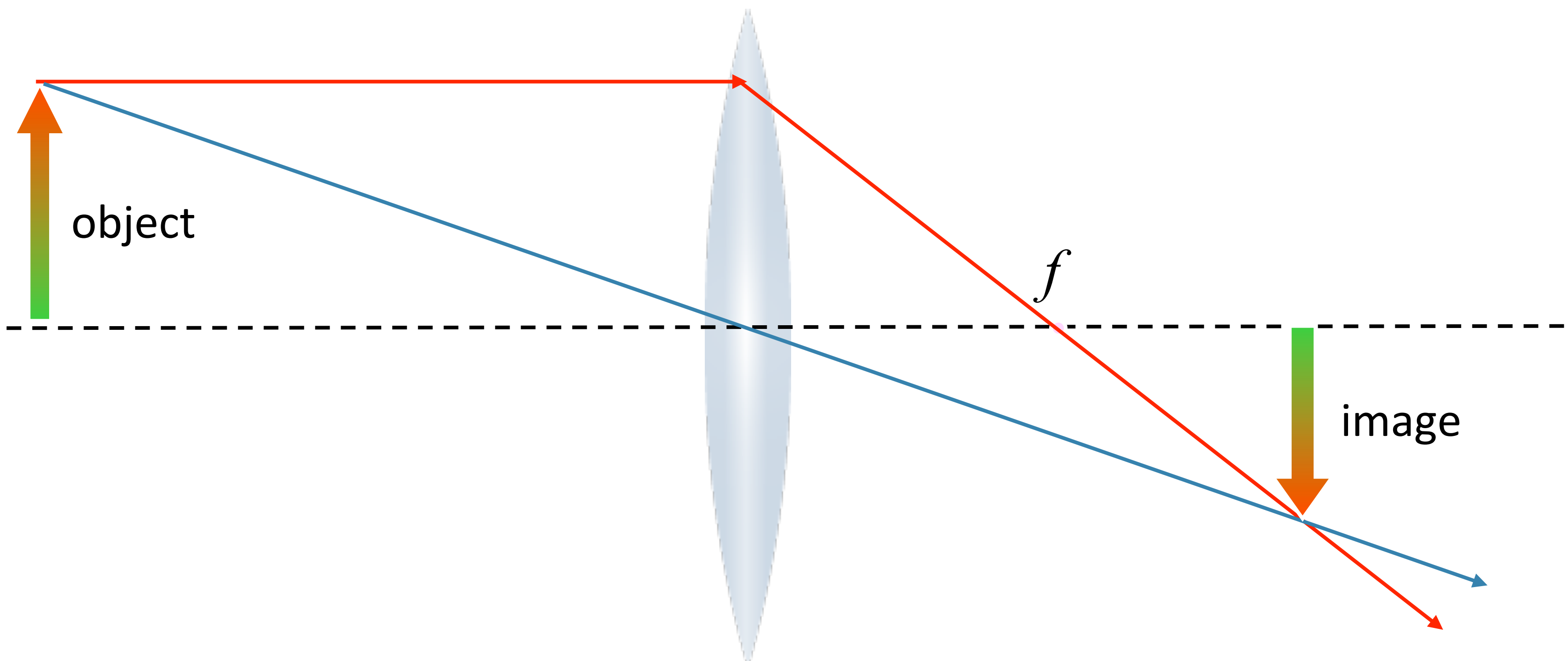
Converging Lens: Consider the case where the shape of the lens is such that light rays parallel to the axis of the mirror are all "focused" to a common spot a distance f behind the lens:



Recipe for Finding Image:

1) Draw ray parallel to axis — refracted ray goes through focus

2) Draw ray through center — refracted ray is symmetric



You now know the position of the same point on the image

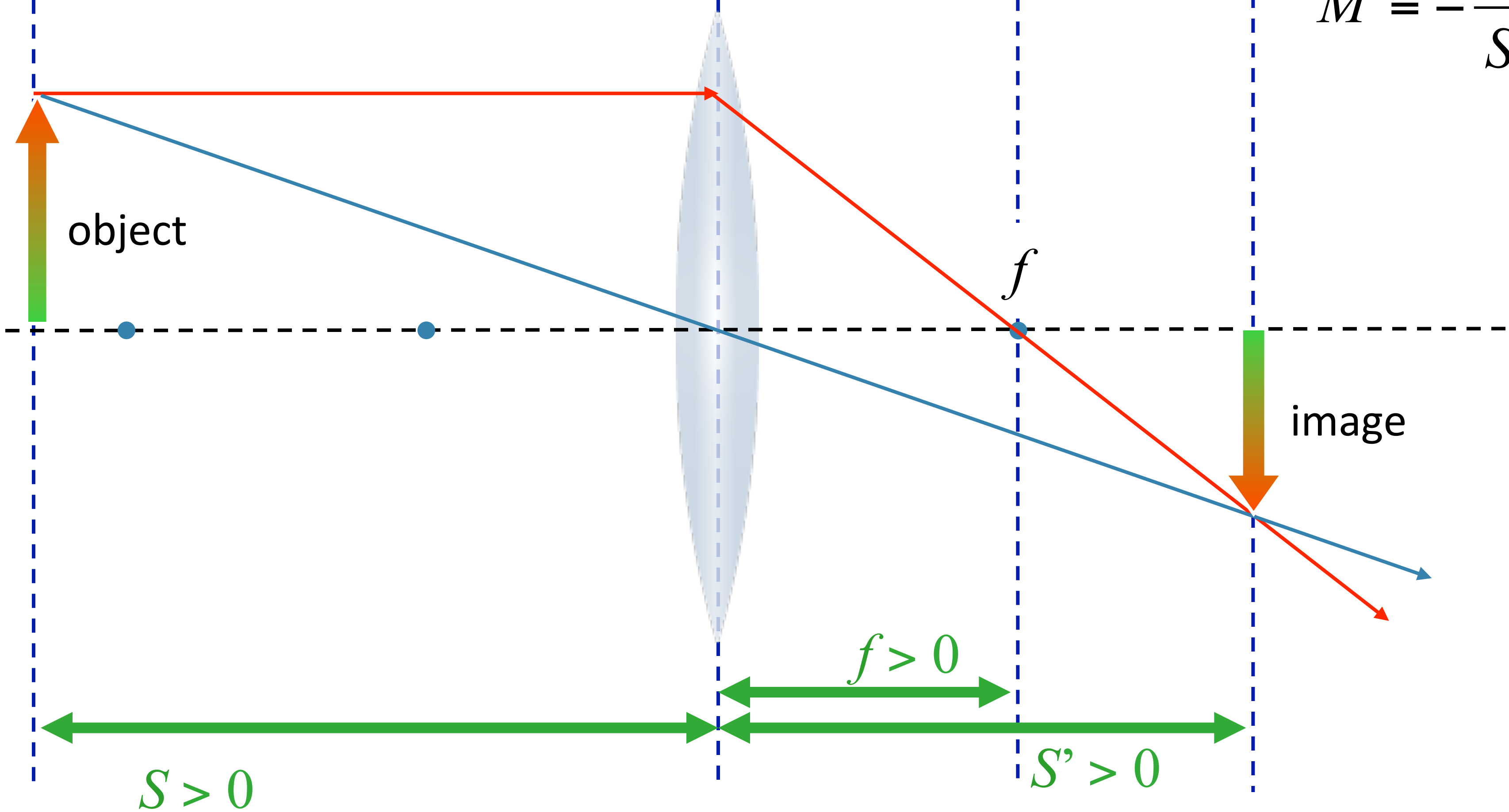
Example

$S > 2f$

image is:
real
inverted
smaller

$$\frac{1}{S} + \frac{1}{S'} = \frac{1}{f}$$

$$M = -\frac{S'}{S}$$



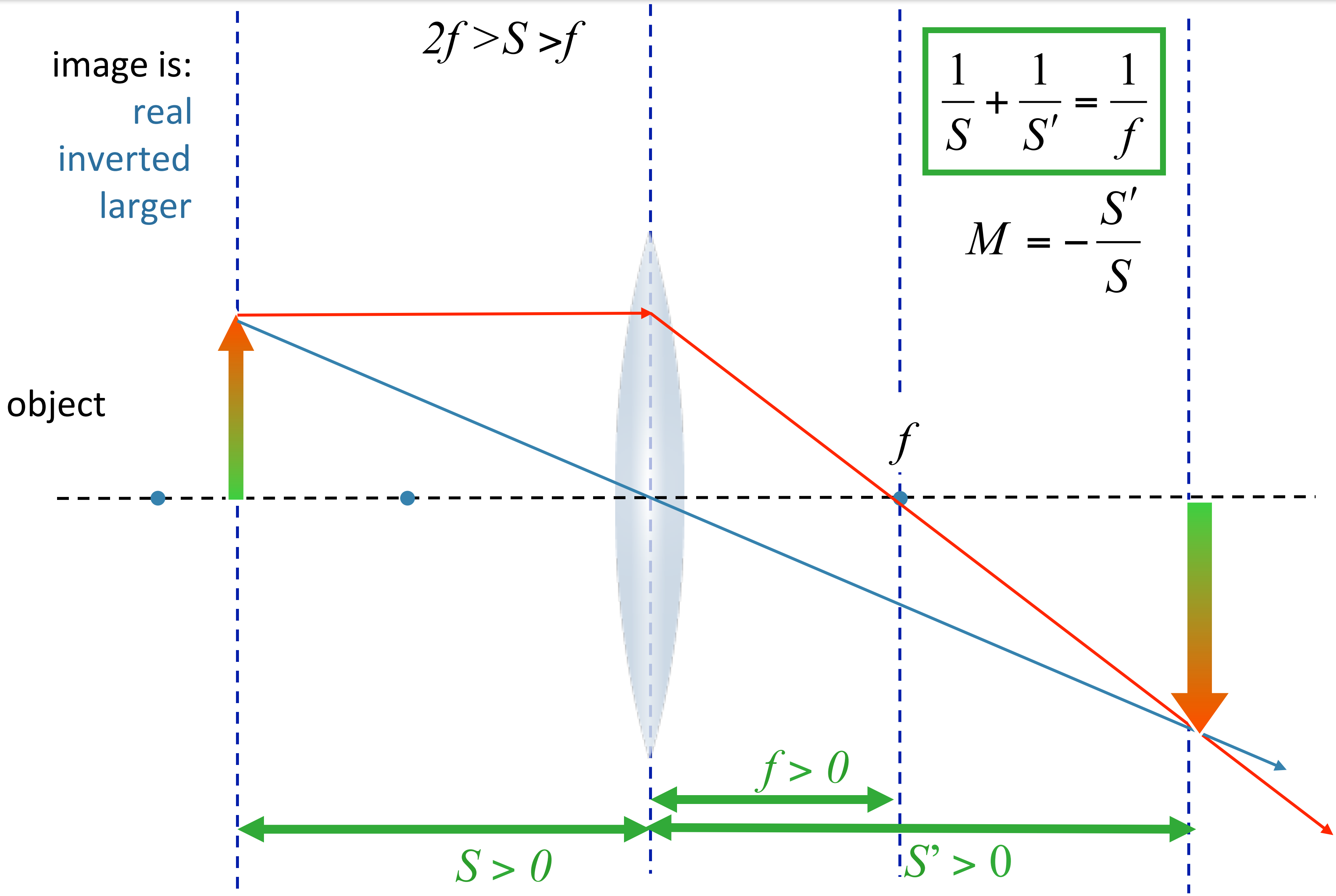
Example

image is:
real
inverted
larger

$2f > S > f$

$$\frac{1}{S} + \frac{1}{S'} = \frac{1}{f}$$

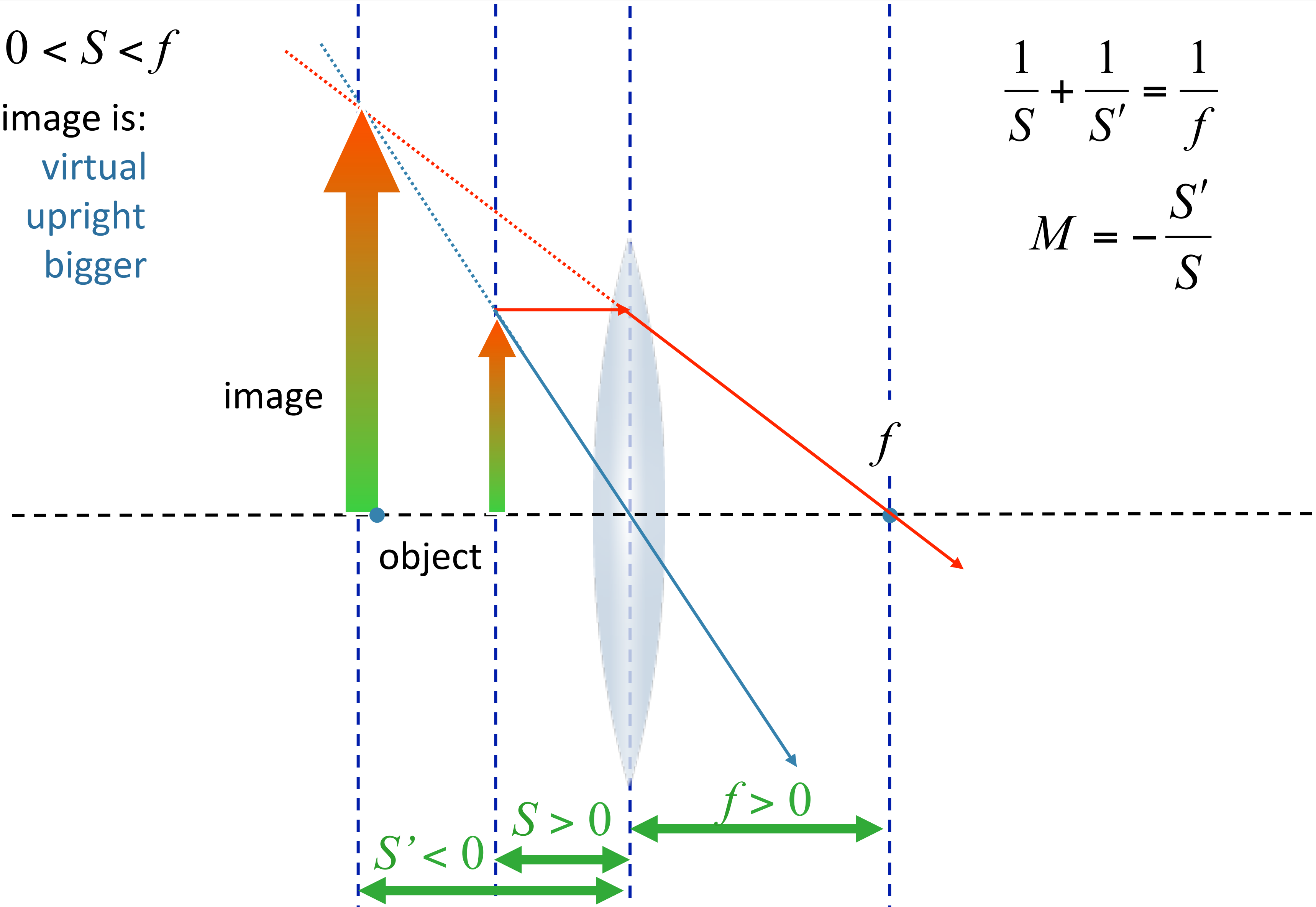
$$M = -\frac{S'}{S}$$



Example

$0 < S < f$

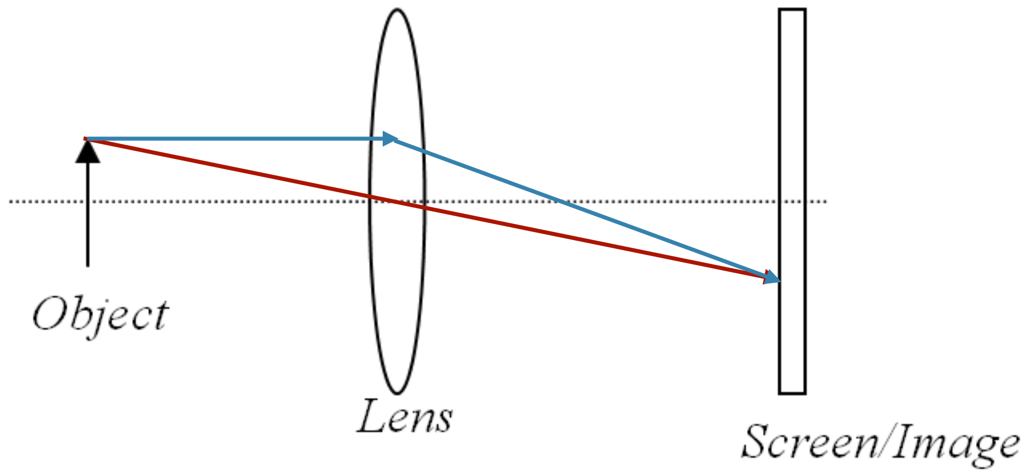
image is:
virtual
upright
bigger



$$\frac{1}{S} + \frac{1}{S'} = \frac{1}{f}$$

$$M = -\frac{S'}{S}$$

CheckPoint 1a



A converging lens is used to project the image of an arrow onto a screen as shown above

The image is:
A. Real
B. Virtual

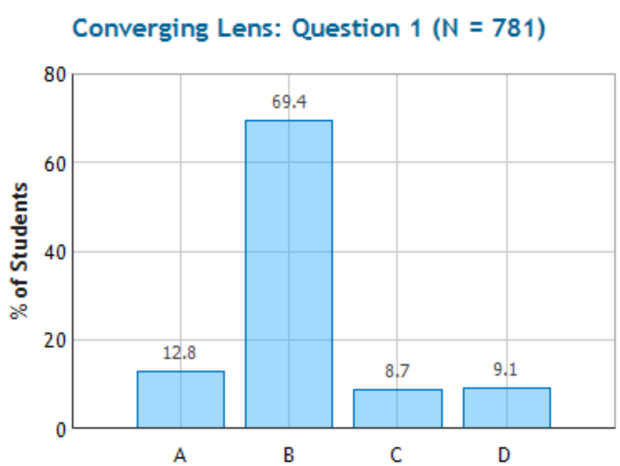
The image is:
A. Inverted
B. Upright

Image on screen

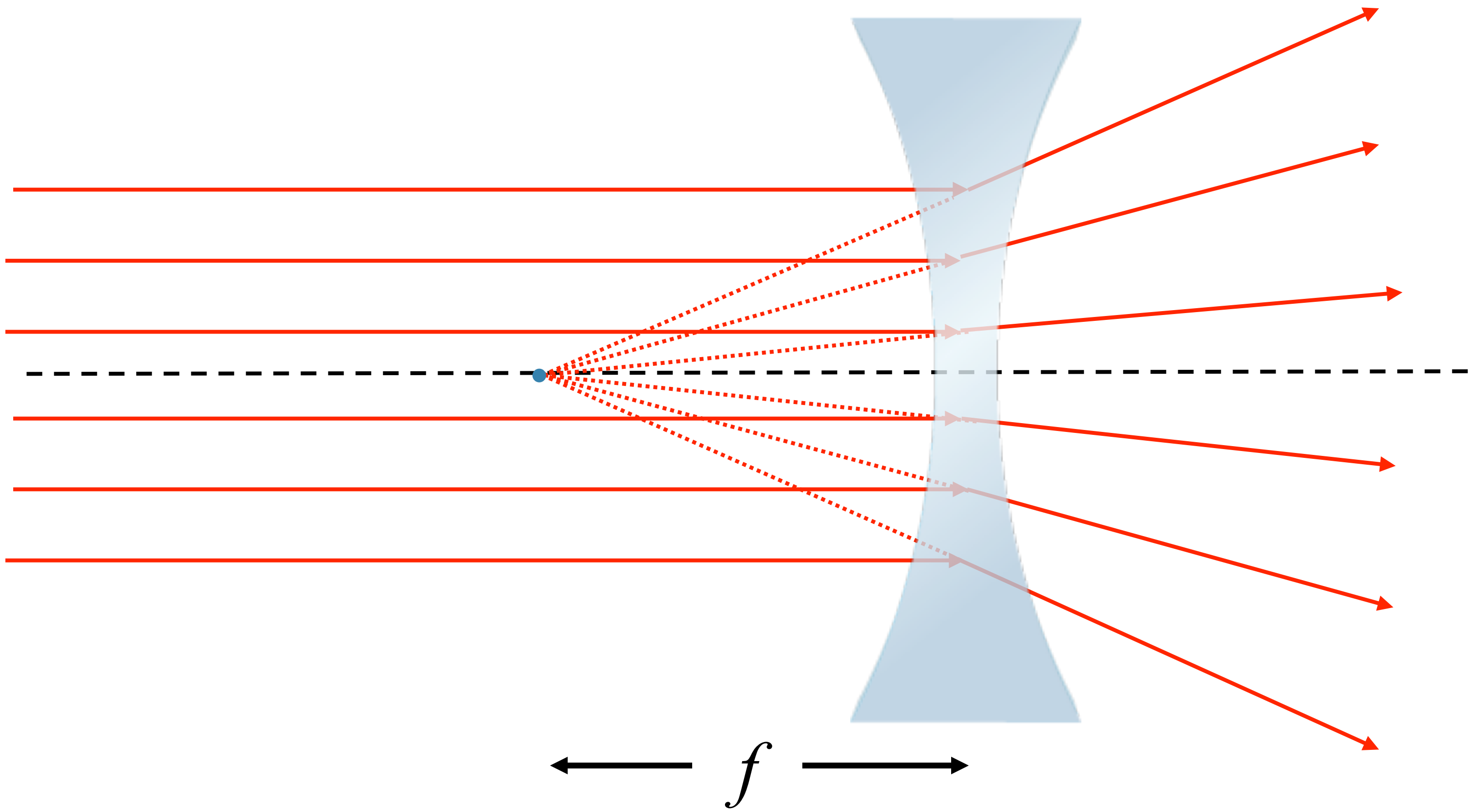
MUST BE REAL

$\rightarrow s' > 0$

$$\frac{1}{s} + \frac{1}{s'} = \frac{1}{f} \qquad M = -\frac{s'}{s}$$



Diverging Lens: Consider the case where the shape of the lens is such that light rays parallel to the axis of the lens all diverge but appear to come from a common spot a distance f in front of the lens:

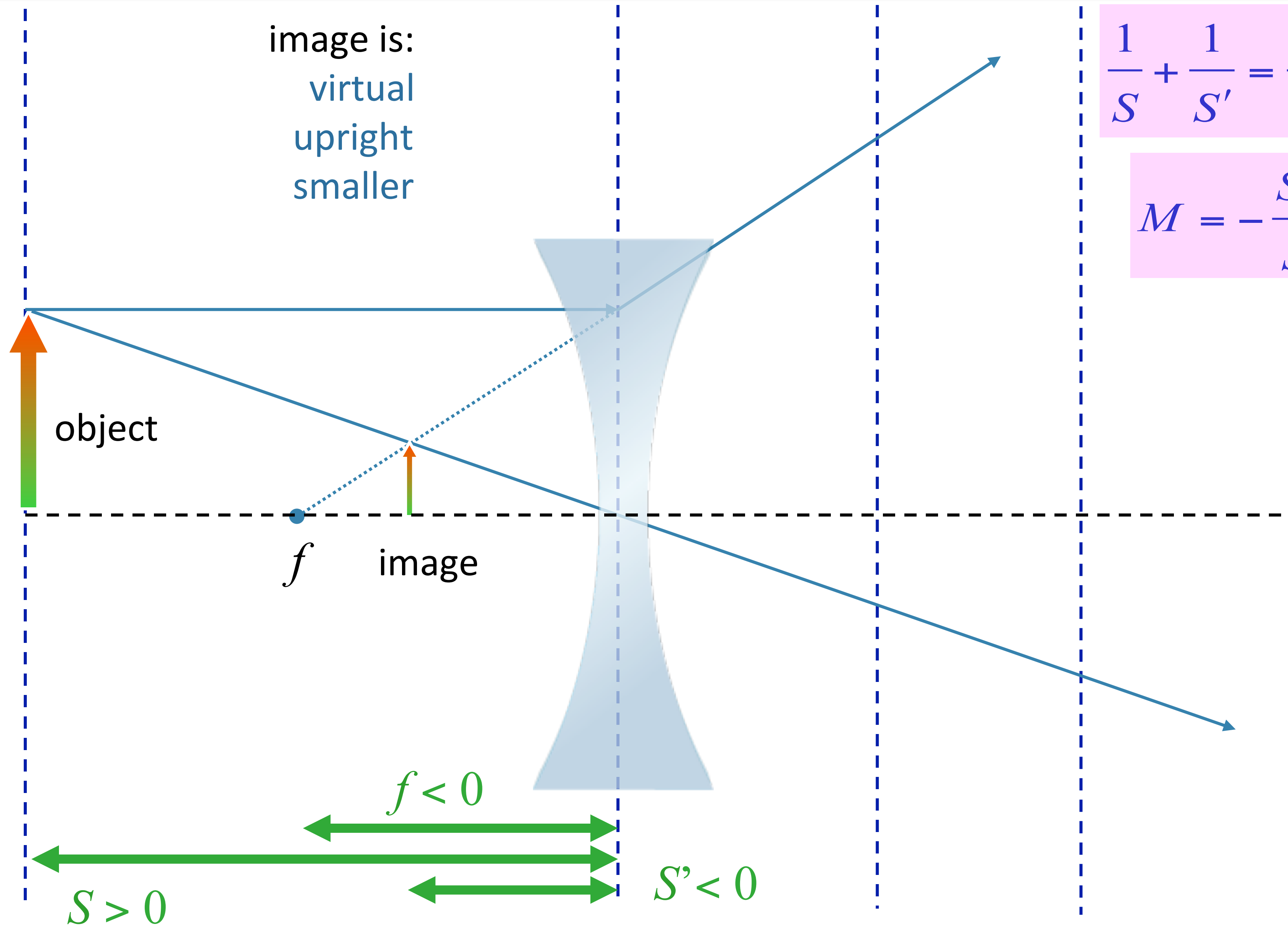


Example

image is:
virtual
upright
smaller

$$\frac{1}{S} + \frac{1}{S'} = \frac{1}{f}$$

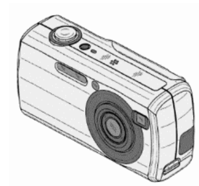
$$M = -\frac{S'}{S}$$

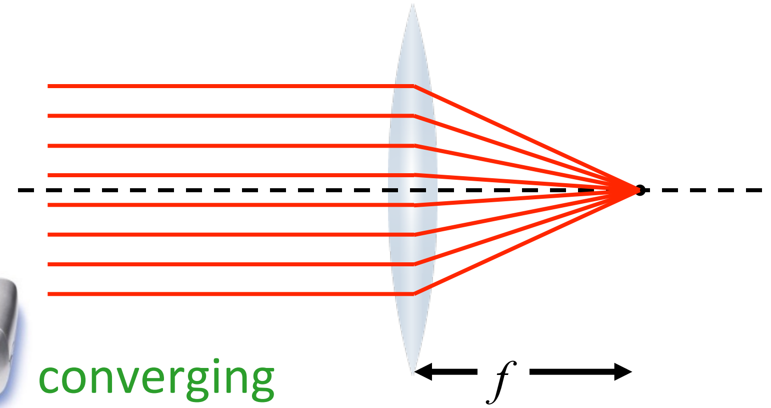


Executive Summary - Lenses

$S > 2f$

real
inverted
smaller





$2f > S > f$

real
inverted
bigger

converging

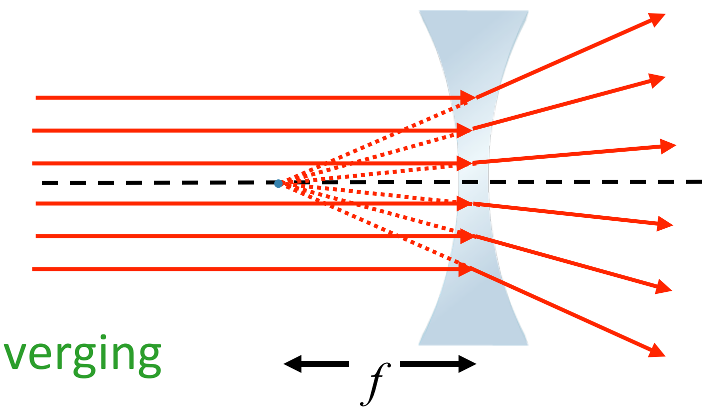
$f > S > 0$

virtual
upright
bigger

$$\frac{1}{s} + \frac{1}{s'} = \frac{1}{f} \qquad M = -\frac{s'}{s}$$

$S > 0$

virtual
upright
smaller



diverging

It's Always the Same:

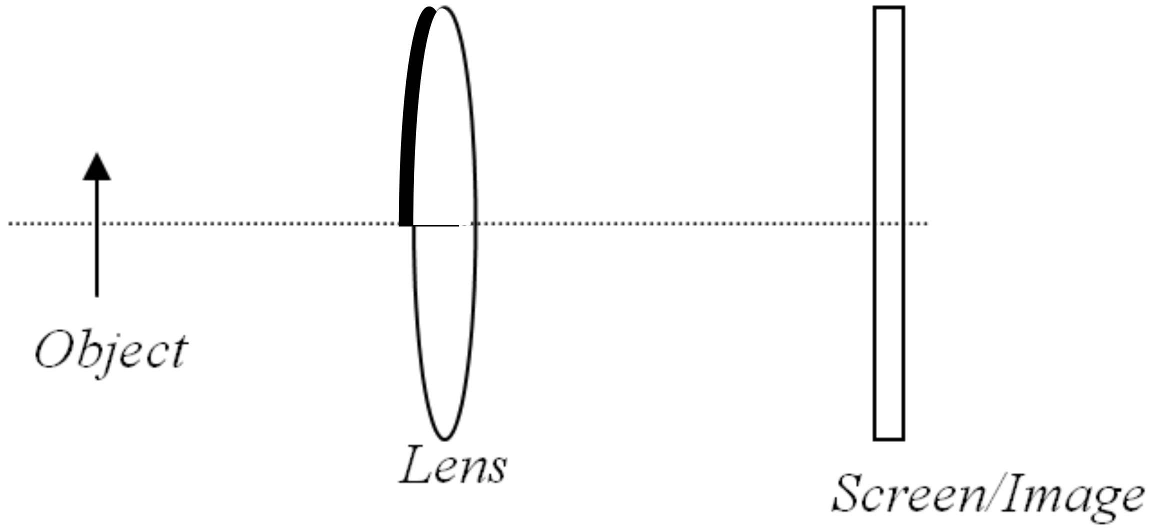
$$\frac{1}{s}+\frac{1}{s'}=\frac{1}{f} \qquad M=-\frac{s'}{s}$$

You just have to keep the signs straight:

The sign conventions

S: positive if object is "upstream" of lens
S': positive if image is "downstream" of lens
f: positive if converging lens

CheckPoint 1b



A converging lens is used to project the image of an arrow onto a screen as shown above

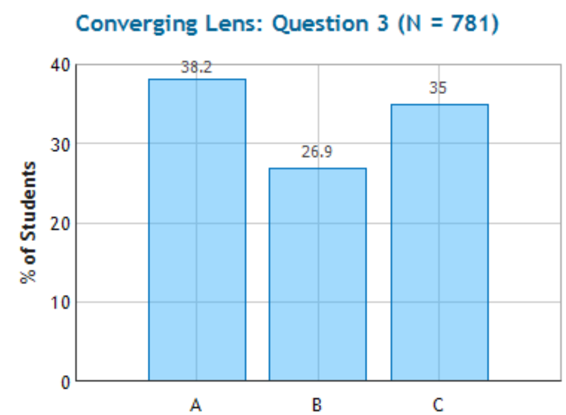
A piece of black tape is now placed over the upper half of the lens. Which of the following is true?

A. Only the lower half of the object will show on the screen
B. Only the upper half of the object will show on the screen
C. The whole object will show on the screen

(A) "The light from the top half that would have been refracted down no longer passes through the lens."

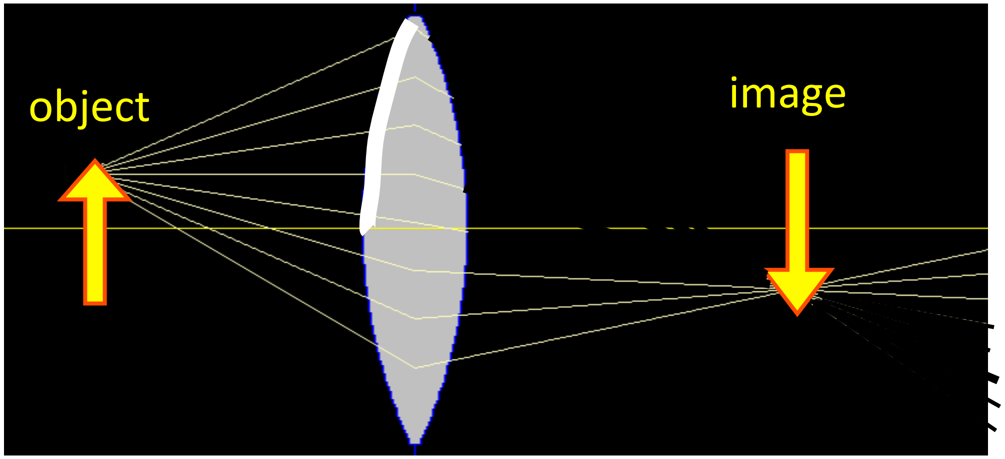
(B) "Blocking out the top of the lens will block out the lower tail of the arrow so that only the arrow head is shown."

(C) "While some of the rays are blocked by the tape, every ray emanating from any point on the object that passes through the lens converges to the corresponding point in the image, and there are no points on the object for which multiple rays do not make it through the lens, so an image is formed just as before."



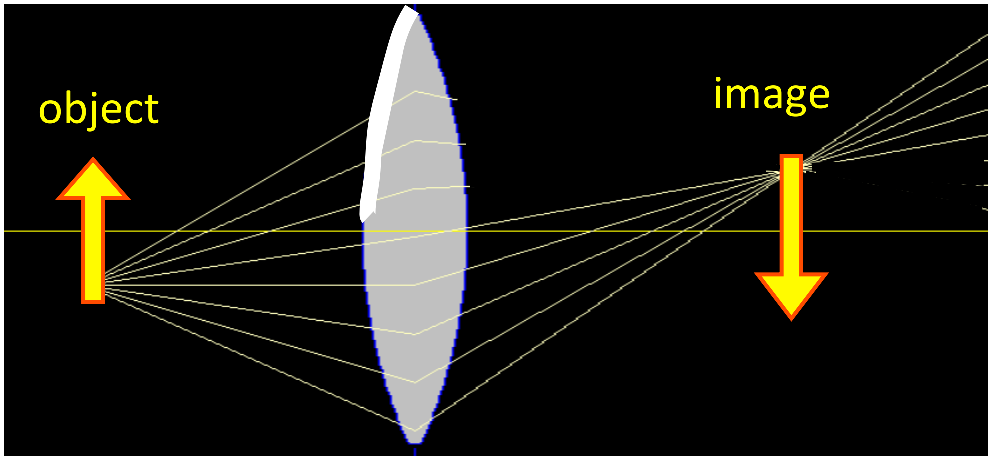
Cover top half of lens

Light from top of object



Cover top half of lens

Light from bottom of object



What's the Point?

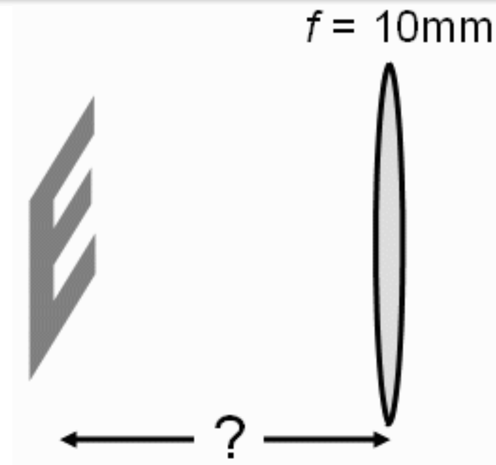
The rays from the bottom half still focus
The image is there, but it will be dimmer!

A. Only the lower half of the object will show on the screen
B. Only the upper half of the object will show on the screen
C. The whole object will show on the screen

Calculation

A magnifying glass is used to read the fine print on a document. The focal length of the lens is 10mm.

At what distance from the lens must the document be placed in order to obtain an image magnified by a factor of 5 that is not inverted?



Conceptual Analysis

Lens Equation: $1/s + 1/s' = 1/f$

Magnification: $M = -s'/s$

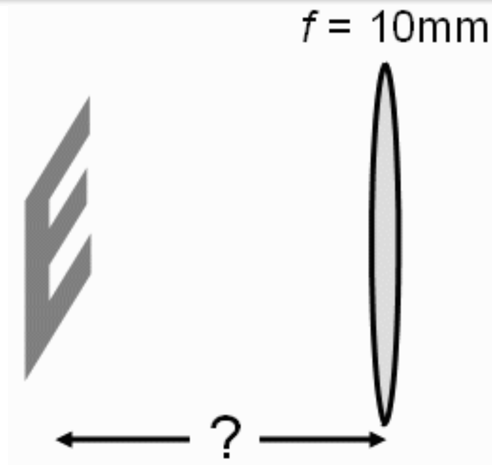
Strategic Analysis

Consider nature of image (real or virtual?) to determine relation between object position and focal point

Use magnification to determine object position

A magnifying glass is used to read the fine print on a document. The focal length of the lens is 10mm.

At what distance from the lens must the document be placed in order to obtain an image magnified by a factor of 5 that is not inverted?

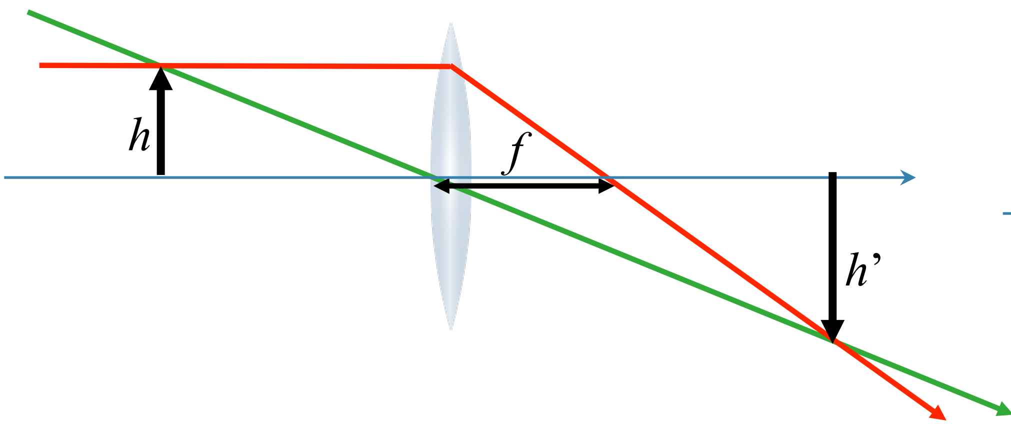


Is the image real or virtual?

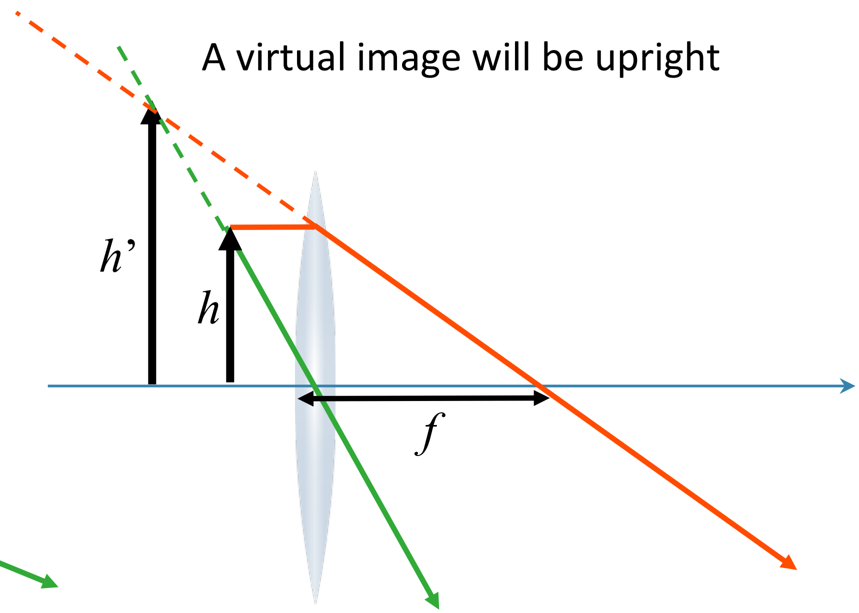
A) REAL

B) VIRTUAL

A real image would be inverted



A virtual image will be upright



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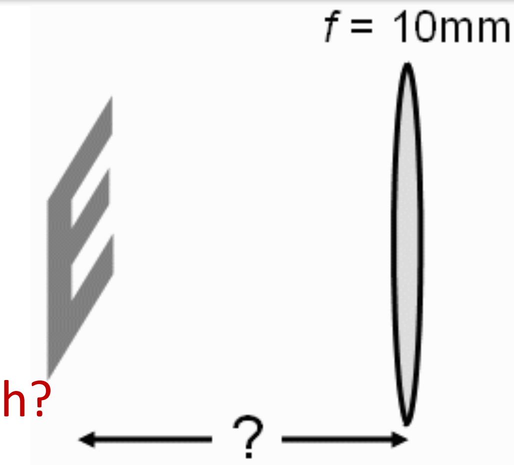
At what distance from the lens must the document be placed in order to obtain an image magnified by a factor of 5 that is not inverted?



How does the object distance compare to the focal length?

A) $|s| < |f|$

B) $|s| = |f|$

C) $|s| > |f|$

Lens equation → $$\frac{1}{S'} = \frac{1}{f} - \frac{1}{S}$$

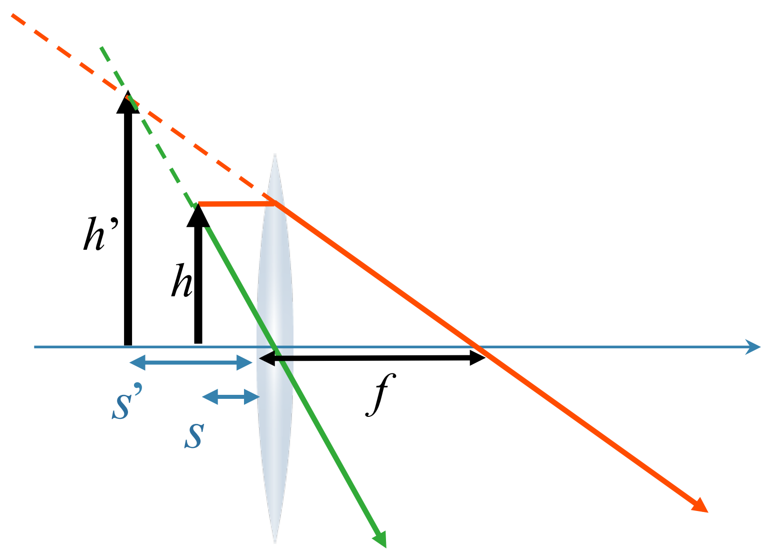
→ $$S' = \frac{f\,S}{S - f}$$

Virtual Image ⇒ $s' < 0$

Real object ⇒ $s > 0$

Converging lens ⇒ $f > 0$

$$S - f < 0$$



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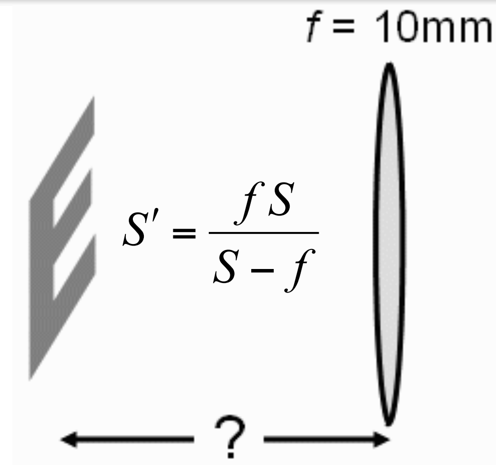


What is the magnification M in terms of s and f?

A) $M = \frac{s-f}{f}$

B) $M = \frac{f-s}{f}$

C) $M = \frac{-f}{s-f}$

D) $M = \frac{f}{s-f}$

Lens equation:

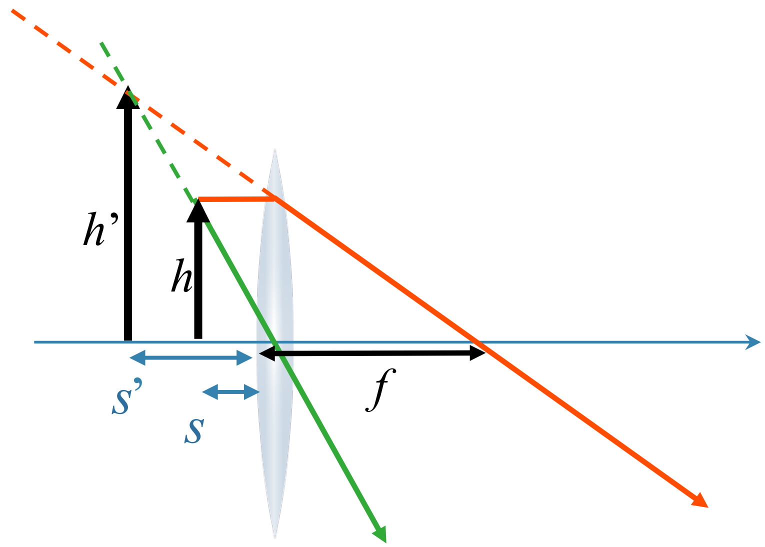
$$\frac{1}{S'} = \frac{1}{f} - \frac{1}{S}$$

$$S' = \frac{f\,S}{S-f}$$

Magnification equation:

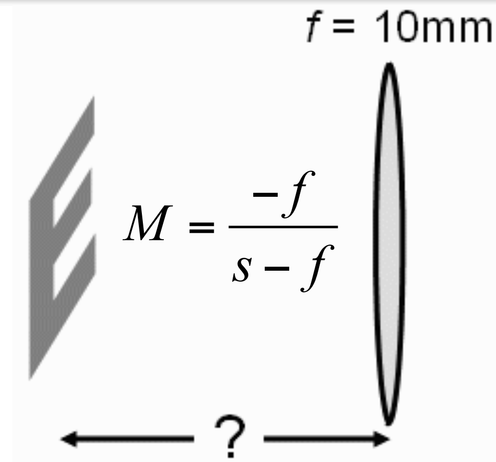
$$M = -\frac{s'}{s}$$

$$M = \frac{-f}{s-f}$$



A magnifying glass is used to read the fine print on a document. The focal length of the lens is 10mm.

At what distance from the lens must the document be placed in order to obtain an image magnified by a factor of 5 that is not inverted?



A) 1.7mm

B) 6mm

C) 8mm

D) 40 mm

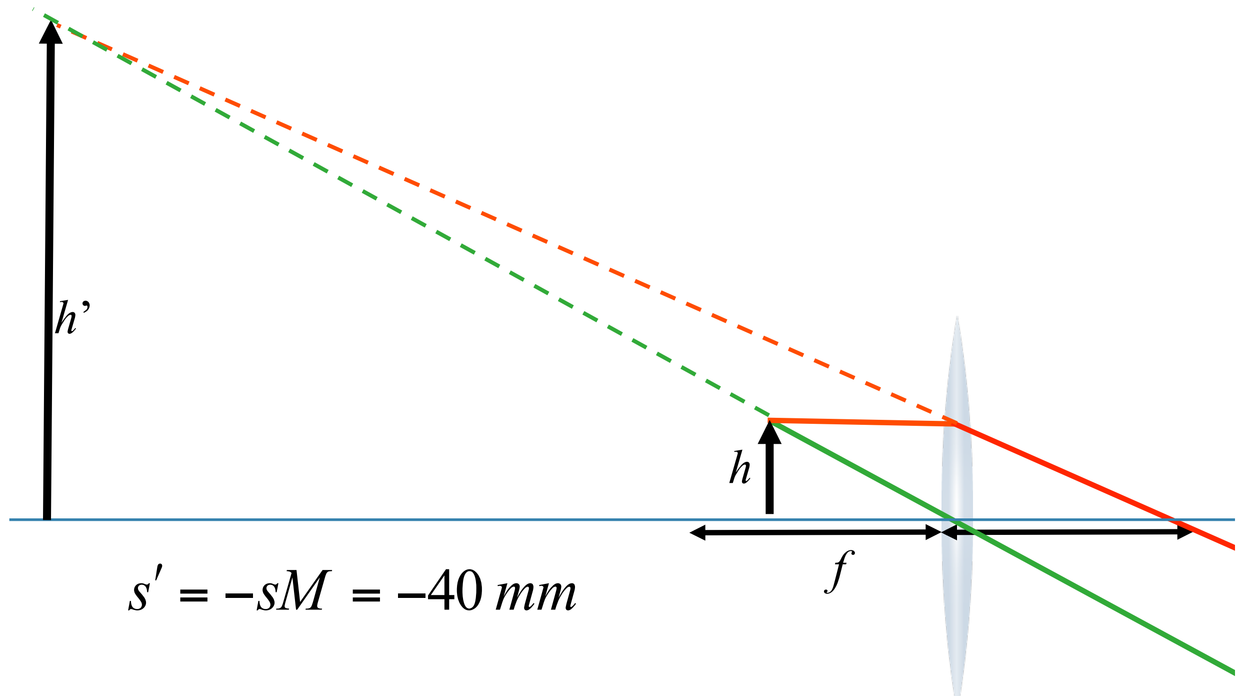
E) 60 mm

$$M = +5$$

$$f = +10\,mm$$

$$M = \frac{-f}{s-f} \;\rightarrow\; s = f\,\frac{(M-1)}{M}$$

$$\rightarrow\; s = \frac{4}{5}f = 8\,mm$$

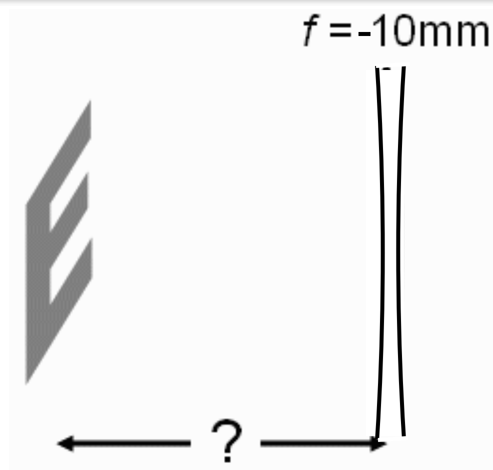


$$s' = -sM = -40\,mm$$

Follow Up

Suppose we replace the converging lens with a diverging lens with focal length of 10mm.

If we still want to get an image magnified by a factor of 5 that is not inverted, how does the object s_{div} compare to the original object distance s_{conv}?



A) $s_{div} < s_{conv}$ B) $s_{div} = s_{conv}$ C) $s_{div} > s_{conv}$ D) s_{div} doesn't exist

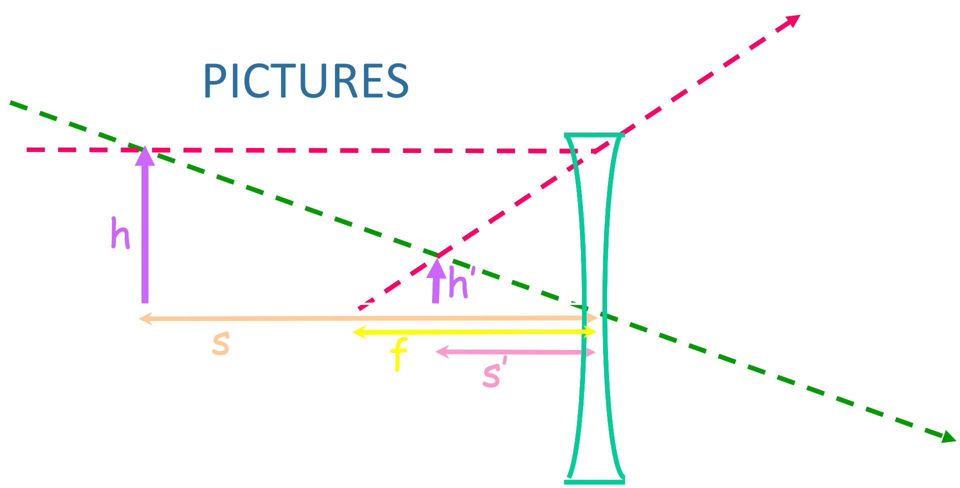
EQUATIONS

$$M = \frac{-f}{s-f} \rightarrow s = f\frac{(M-1)}{M}$$

$$M = +5$$
$$f = -10mm$$
$$\rightarrow s = \frac{4}{5}f = -8mm$$

s negative ⊠ not real object

PICTURES



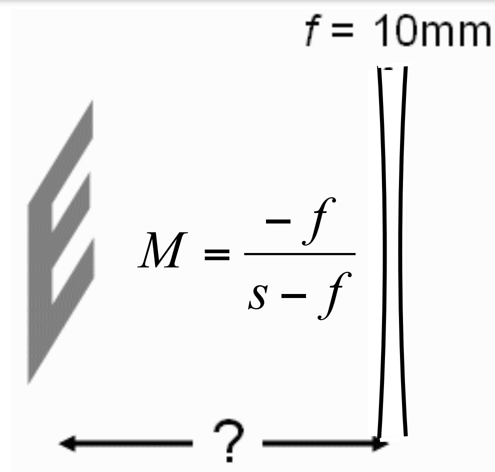
Draw the rays: s' will always be smaller than s

Magnification will always be less than 1

Follow Up

Suppose we replace the converging lens with a diverging lens with focal length of 10mm.

What is the magnification if we place the object at $s = 8\text{mm}$?



A) $M = \frac{1}{2}$ B) $M = 5$ C) $M = \frac{3}{8}$ **D) $M = \frac{5}{9}$** E) $M = \frac{4}{5}$

EQUATIONS

$$M = \frac{-f}{s-f}$$

$$s = 8\,mm$$

$$f = -10\,mm$$

$$M = -\frac{-10}{8-(-10)} = \frac{10}{18} = \frac{5}{9}$$

PICTURES