Your Comments

Directions of ALLLLL the induced things

I'm getting confused on which direction defines the flux and the magnetic field from the induced current. Does the magnetic field from the induced current opposed the original flux, because that's what I got out of the prelecture, but I'm not sure if that's right.

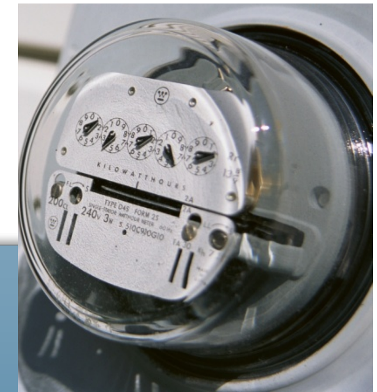
How do you tell which direction flux is increasing in?

In the flux through rotating loop prelecture slides, the dot product is calculated with sin instead of cos. how does this work?

Please go over the Generator its hard to make sense of it all.

I am still confused why the ε is equal to the negative of d fi over dt.

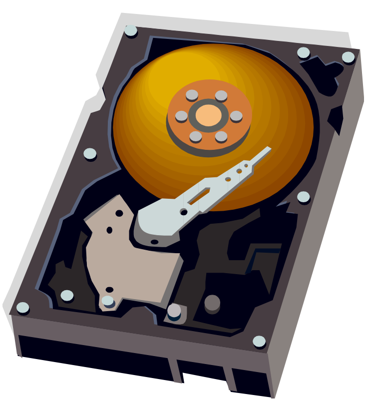
You know you're in college when your easiest class is physics...



Physics 212
Lecture 17

Today's Concept:

Faraday's Law



$$emf = \oint \vec{E} \cdot d\vec{\ell} = -\frac{d\Phi_B}{dt}$$

Faraday's Law

Faraday's Law: $\boxed{emf = \oint \vec{E} \cdot d\vec{\ell} = -\frac{d\Phi_B}{dt}}$ where $\boxed{\Phi_B \equiv \int \vec{B} \cdot d\vec{A}}$

Looks scary but it's not – its amazing and beautiful!

↓

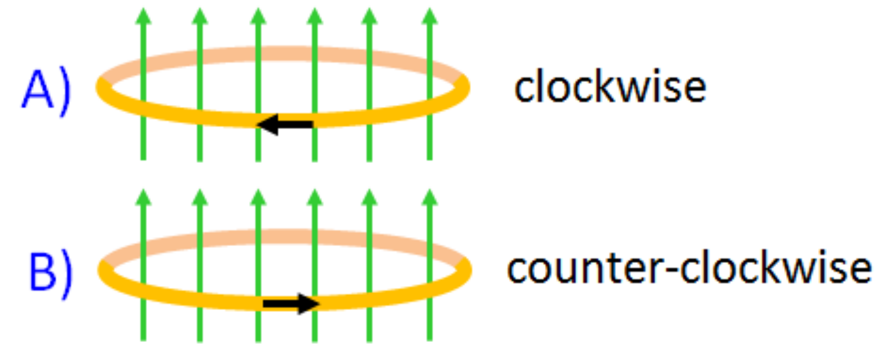
A changing magnetic flux produces an electric field.

↓

Electricity and magnetism are deeply connected.

Checkpoint 1

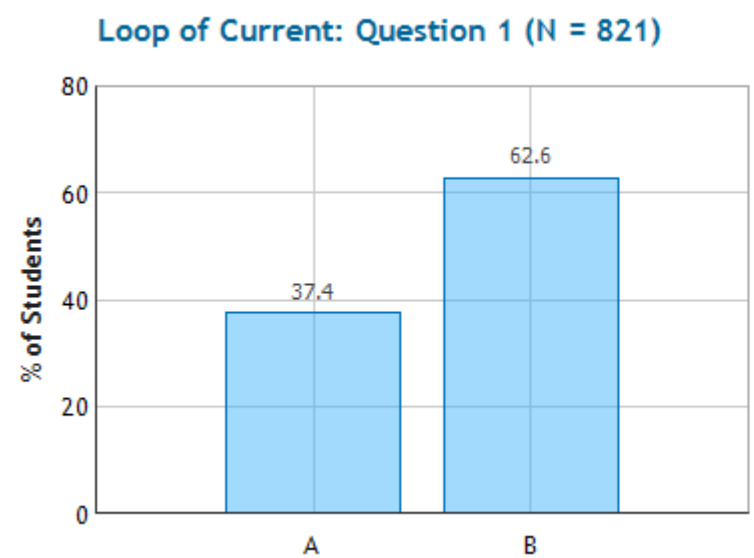
Suppose a current flows in a horizontal conducting loop in such a way that the magnetic flux produced by this current points upward.



As viewed from above, in which direction is this current flowing?

A. clockwise ***B.*** counterclockwise

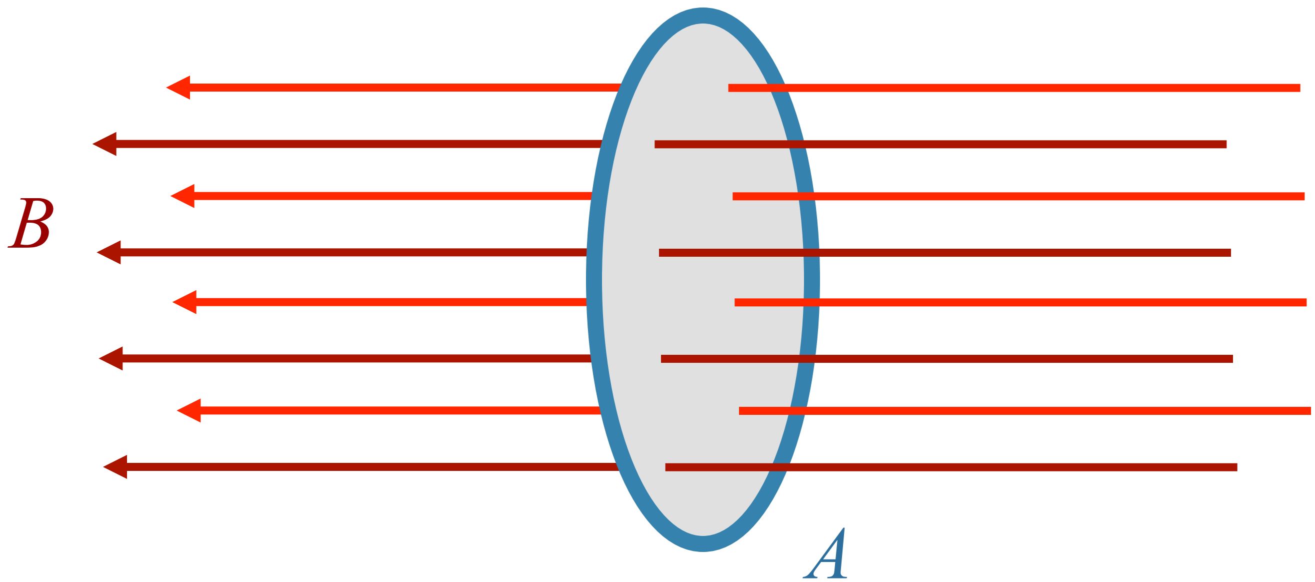
Right hand rule. B field created by current points upwards.



Faraday's Law: $\boxed{emf = \oint \vec{E} \cdot d\vec{\ell} = -\frac{d\Phi_B}{dt}}$ where $\boxed{\Phi_B \equiv \int \vec{B} \cdot d\vec{A}}$

In Practical Words:

1) When the flux Φ_B through a loop changes, an *emf* is induced in the loop.



Flux

Show Projection

Think of Φ_B as the number of field lines passing through the surface

There are many ways to change this…

Faraday's Law: $\boxed{emf = \oint \vec{E}\cdot d\vec{\ell} = -\frac{d\Phi_B}{dt}}$ where $\boxed{\Phi_B \equiv \int \vec{B}\cdot d\vec{A}}$

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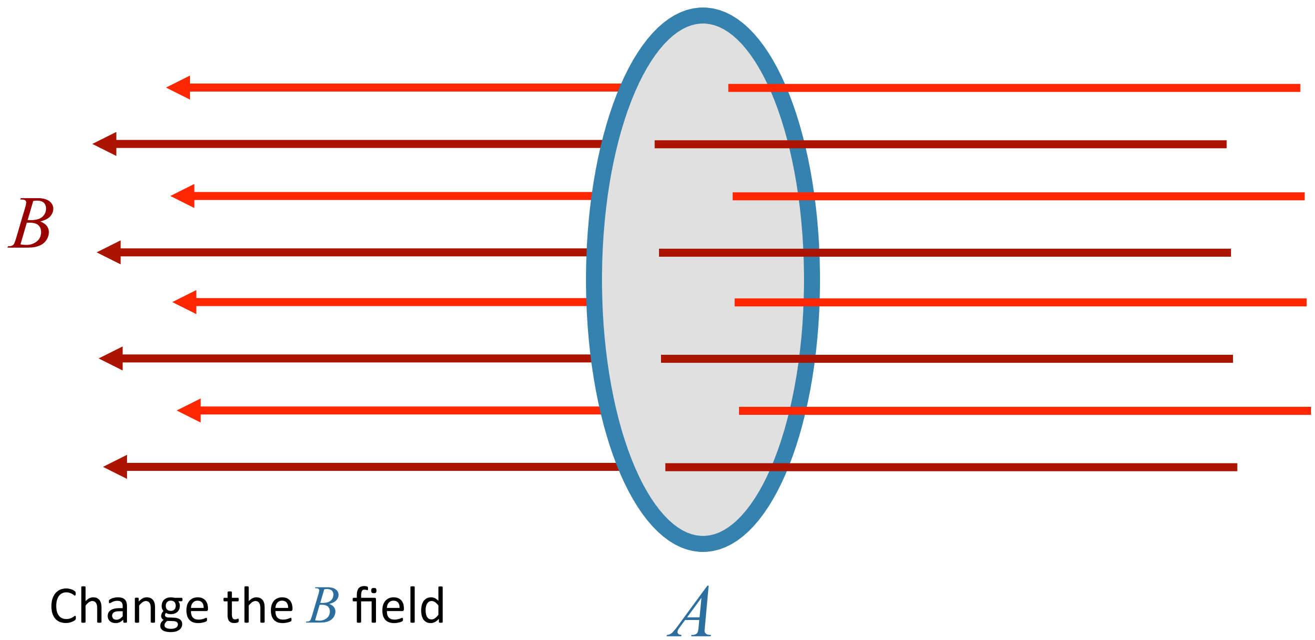

Change the B field

Faraday's Law: $\boxed{emf = \oint \vec{E} \cdot d\vec{\ell} = -\frac{d\Phi_B}{dt}}$ where $\boxed{\Phi_B \equiv \int \vec{B} \cdot d\vec{A}}$

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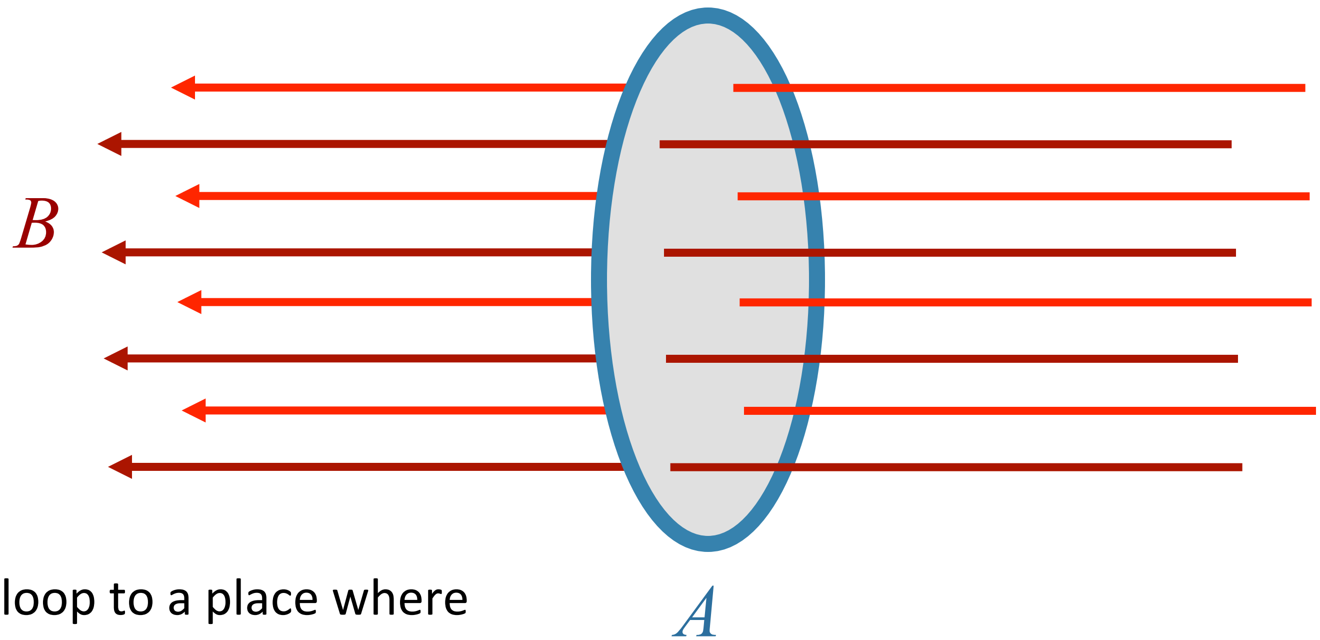

Move loop to a place where the B field is different

Faraday's Law: $\boxed{emf = \oint \vec{E} \cdot d\vec{\ell} = -\frac{d\Phi_B}{dt}}$ where $\boxed{\Phi_B \equiv \int \vec{B} \cdot d\vec{A}}$

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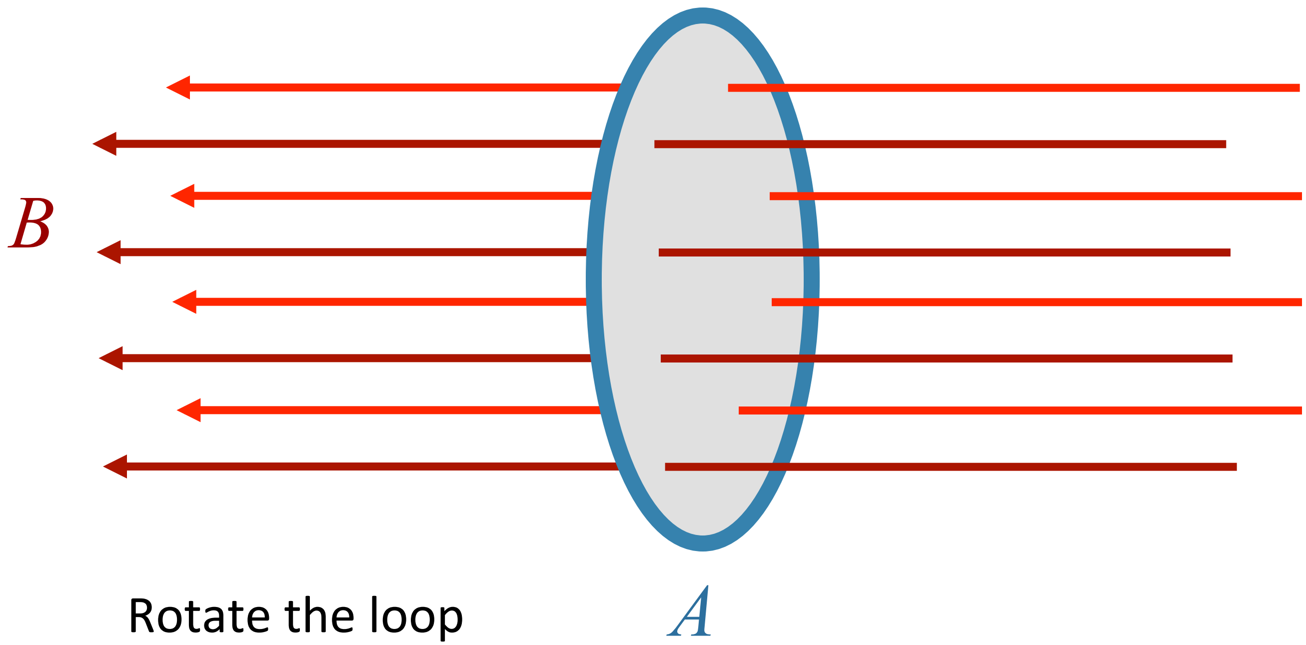

Rotate the loop

Faraday's Law: $\boxed{emf = \oint \vec{E}\cdot d\vec{\ell} = -\frac{d\Phi_B}{dt}}$ where $\boxed{\Phi_B \equiv \int \vec{B}\cdot d\vec{A}}$

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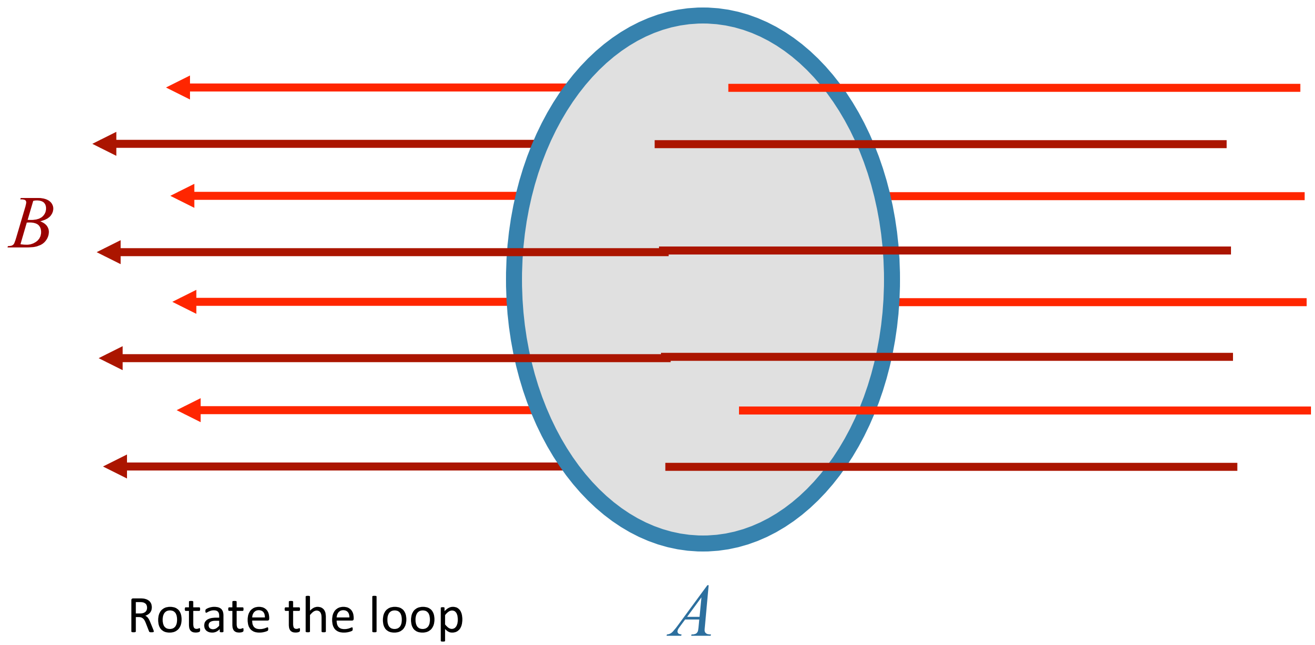

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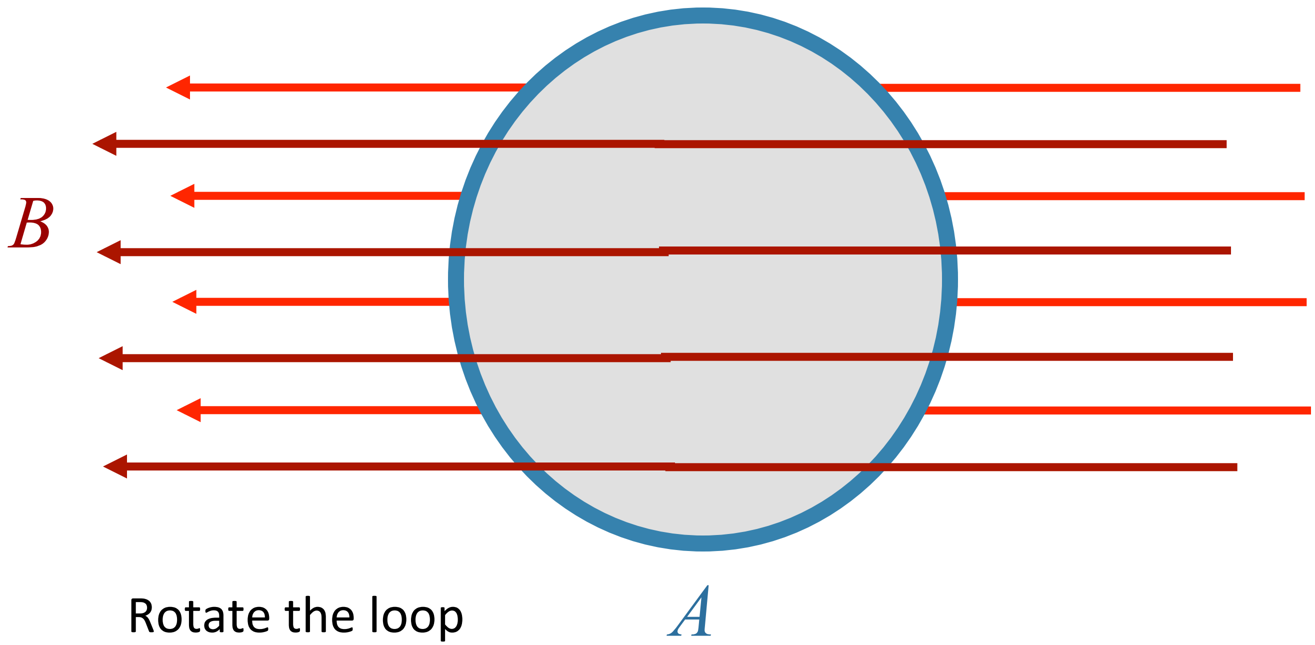

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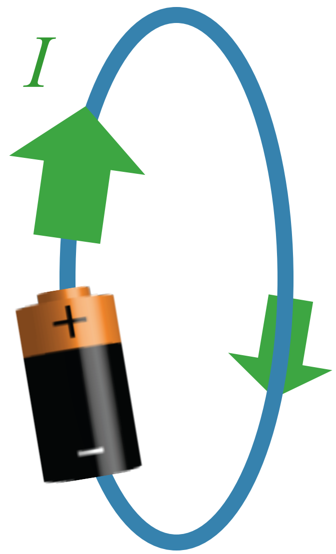
In Practical Words:

1) When the flux Φ_B through a loop changes, an *emf* is induced in the loop.

2) The *emf* will make a current flow if it can (like a battery).



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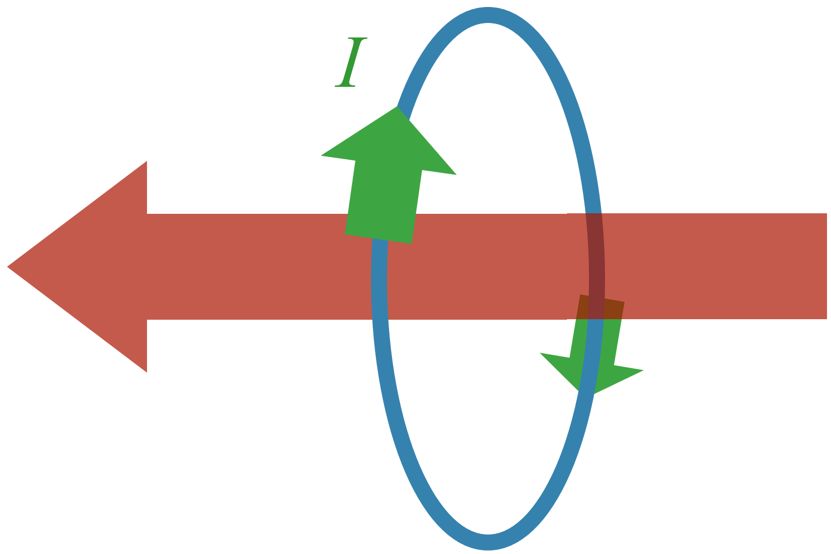
In Practical Words:

1) When the flux Φ_B through a loop changes, an emf is induced in the loop.
2) The emf will make a current flow if it can (like a battery).
3) The current that flows induces a new magnetic field.



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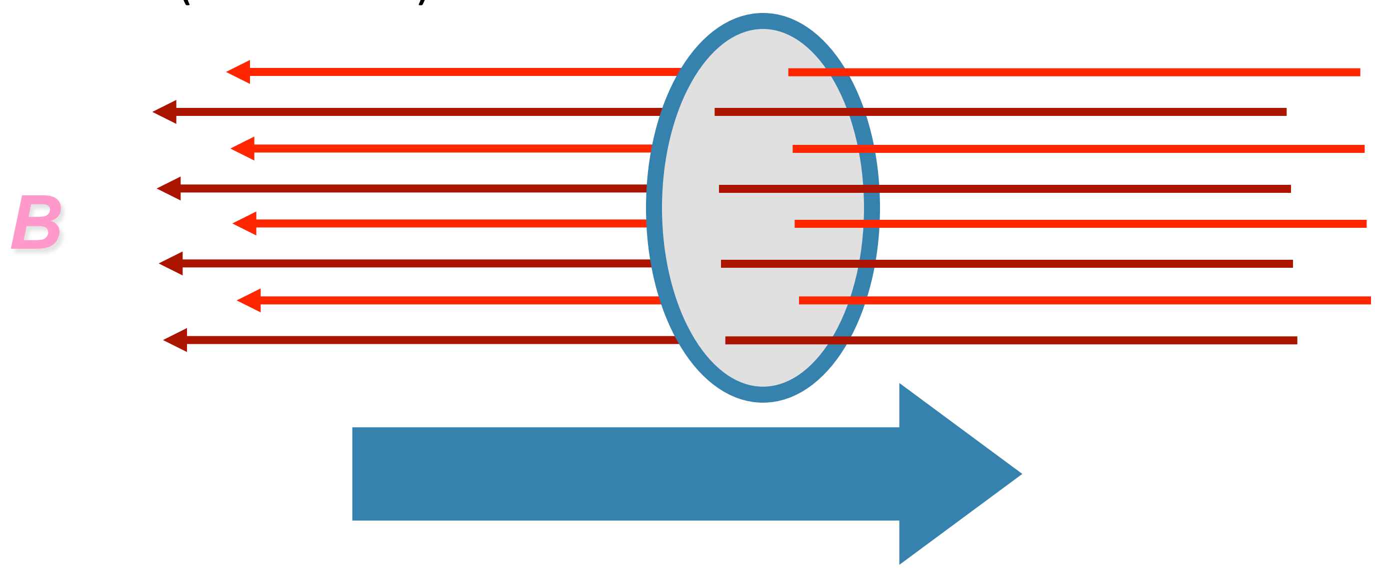
1) When the flux Φ_B through a loop changes, an *emf* is induced in the loop.

2) The *emf* will make a current flow if it can (like a battery).

3) The current that flows induces a new magnetic field.

4) The new magnetic field opposes the change in the original magnetic field that created it. (Lenz' Law)



Demo

Coil and magnet

Faraday's Law: $\boxed{emf = \oint \vec{E}\cdot d\vec{\ell} = -\frac{d\Phi_B}{dt}}$ where $\boxed{\Phi_B \equiv \int \vec{B}\cdot d\vec{A}}$

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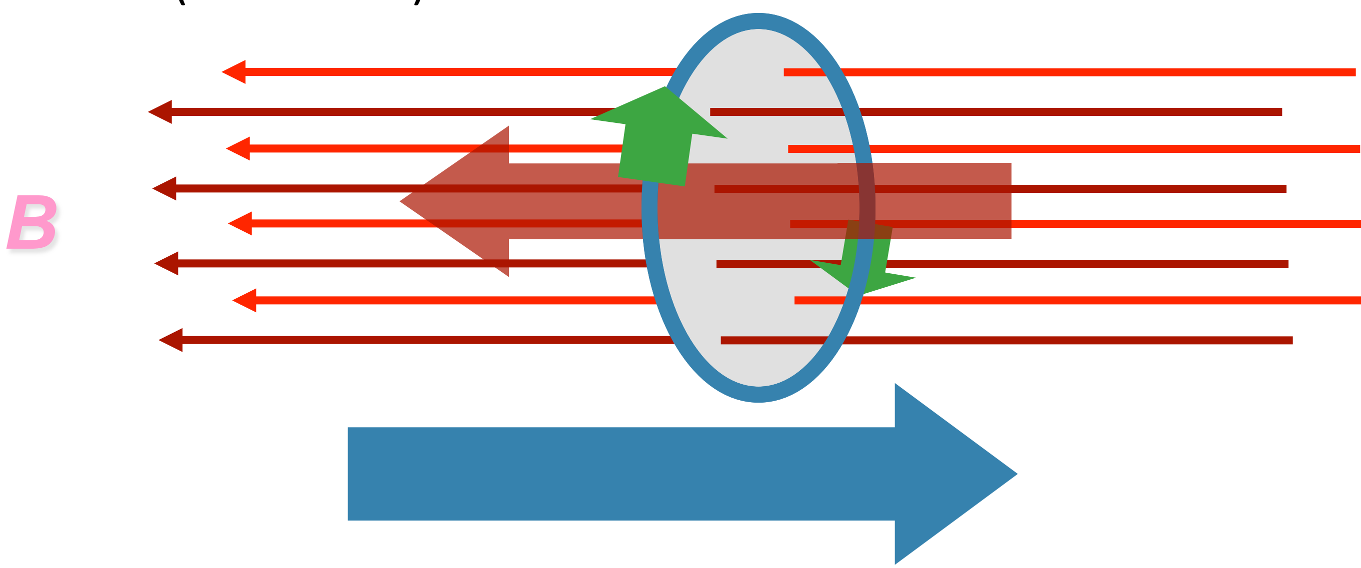


Demo

Back emf & braking

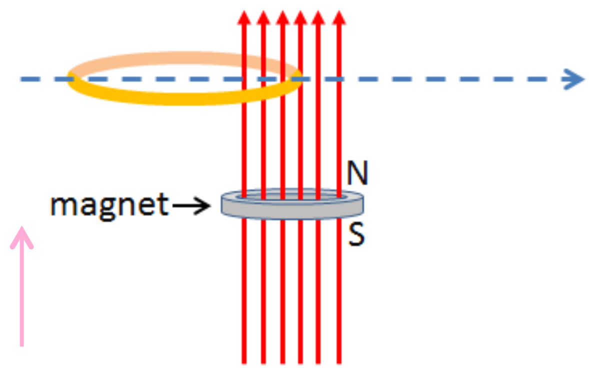
Faraday's Law: $\boxed{emf = \oint \vec{E} \cdot d\vec{\ell} = -\frac{d\Phi_B}{dt}}$ where $\boxed{\Phi_B \equiv \int \vec{B} \cdot d\vec{A}}$

Executive Summary:

$emf \rightarrow$ current $\rightarrow$ field a) induced only when flux is changing
b) opposes the change

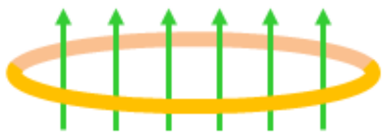
Checkpoint 2

A magnet makes the vertical magnetic field shown by the red arrows. A horizontal conducting loop is entering the field as shown.

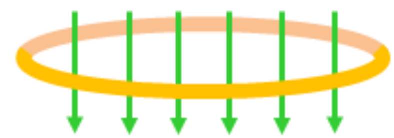


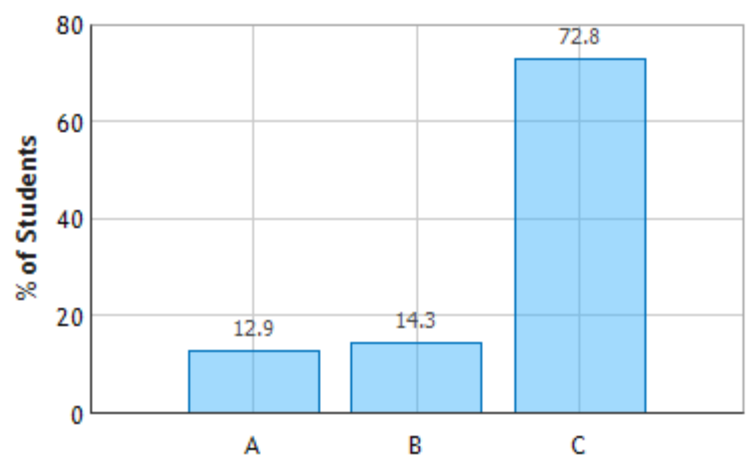
Direction of positive flux

At the instant shown above, what is the direction of the additional flux produced by the current induced in the loop?

A)  up

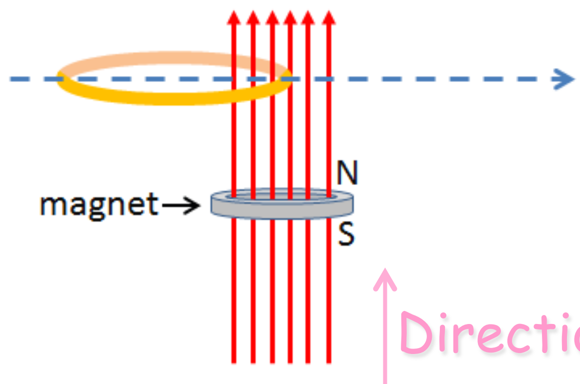
B)  zero

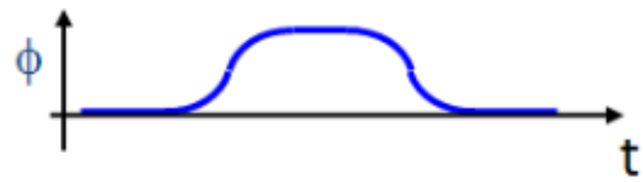
C)  down



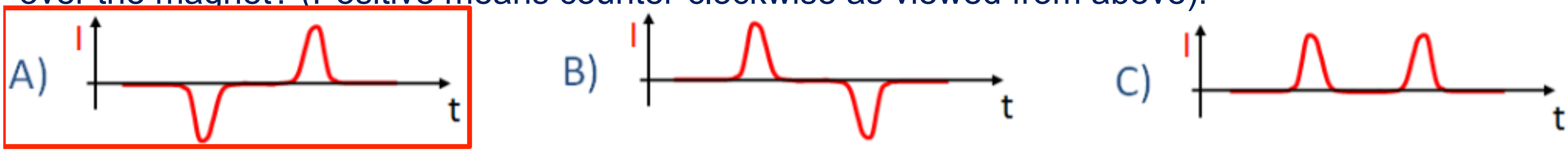
Checkpoint 3

A magnet makes the vertical magnetic field shown by the red arrows. A horizontal conducting loop is entering the field as shown.





The upward flux through the loop as a function of time is shown by the blue trace. Which of the red traces below it best represents the current induced in the loop as a function of time as it passes over the magnet? (Positive means counter-clockwise as viewed from above):

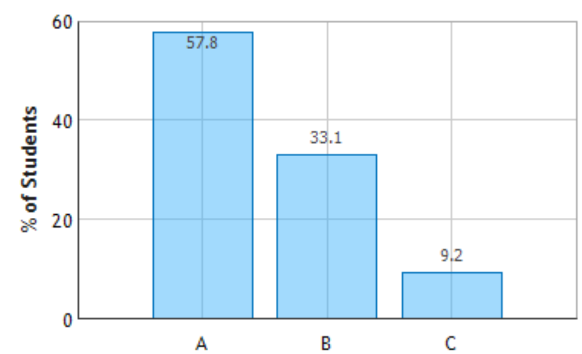


Flux is changing!

Induced flux is initially negative (opposing increasing positive flux – last checkpoint)

THEREFORE, initial *induced current* must be CW as viewed from above

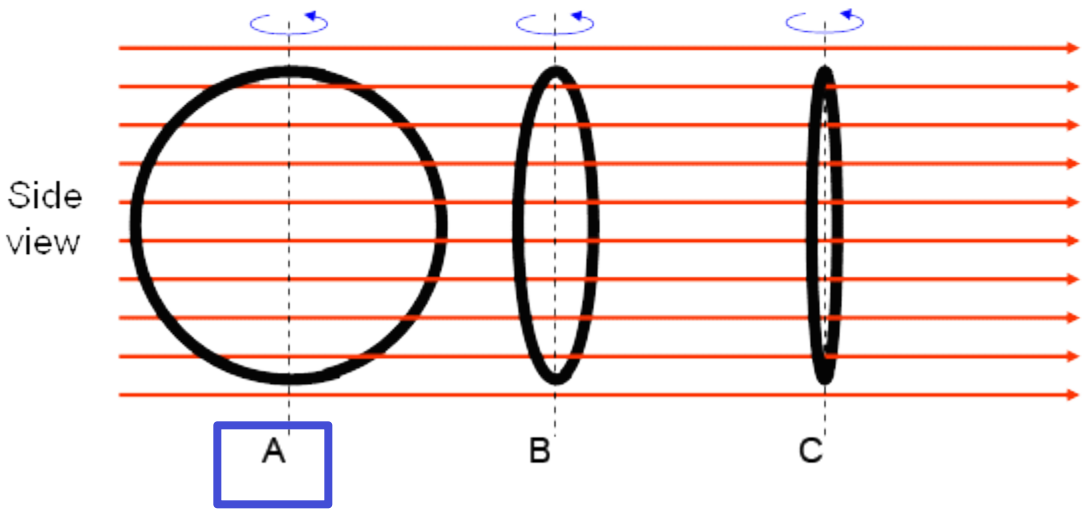
- Current direction from right-hand rule ☺



Prelecture: Faraday's Law

A circular wire loop is placed in a uniform magnetic field pointing to the right. The loop is rotated with *constant angular velocity* around a vertical axis (dashed line).

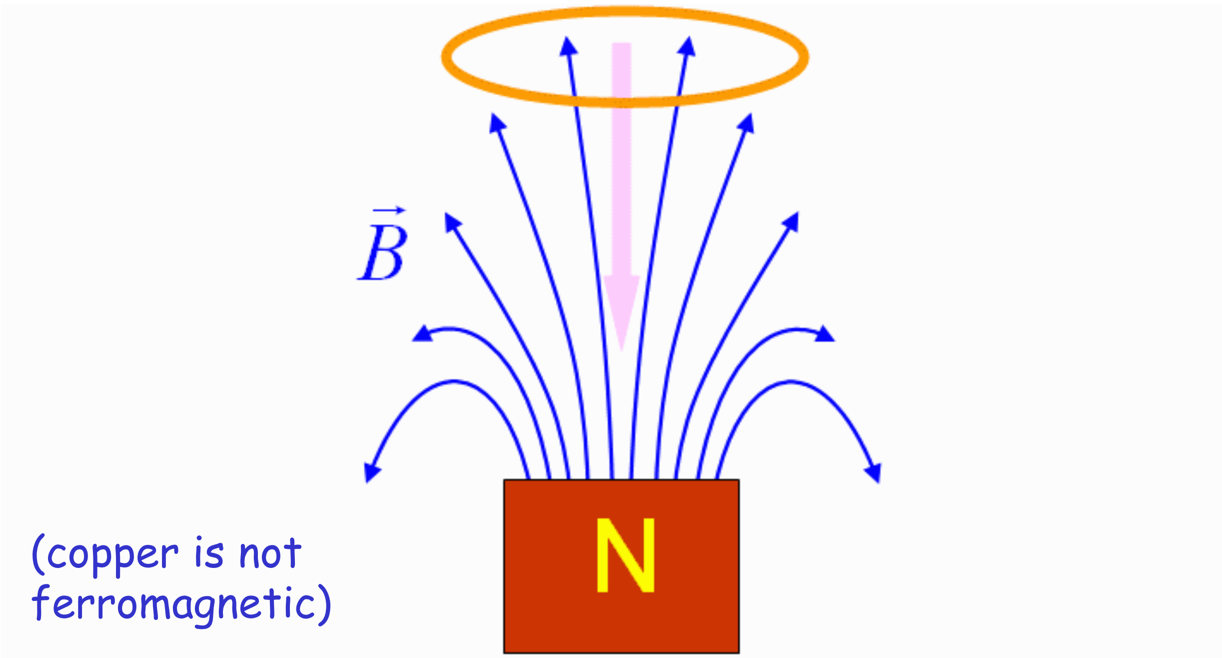
At which of the three times shown is the induced *emf* greatest?



emf = $-d\Phi/dt \rightarrow$ largest where slope of Φ vs t largest

Cool Example

A horizontal copper ring is dropped from rest directly above the north pole of a permanent magnet



As the ring falls, in which direction will the induced field point?

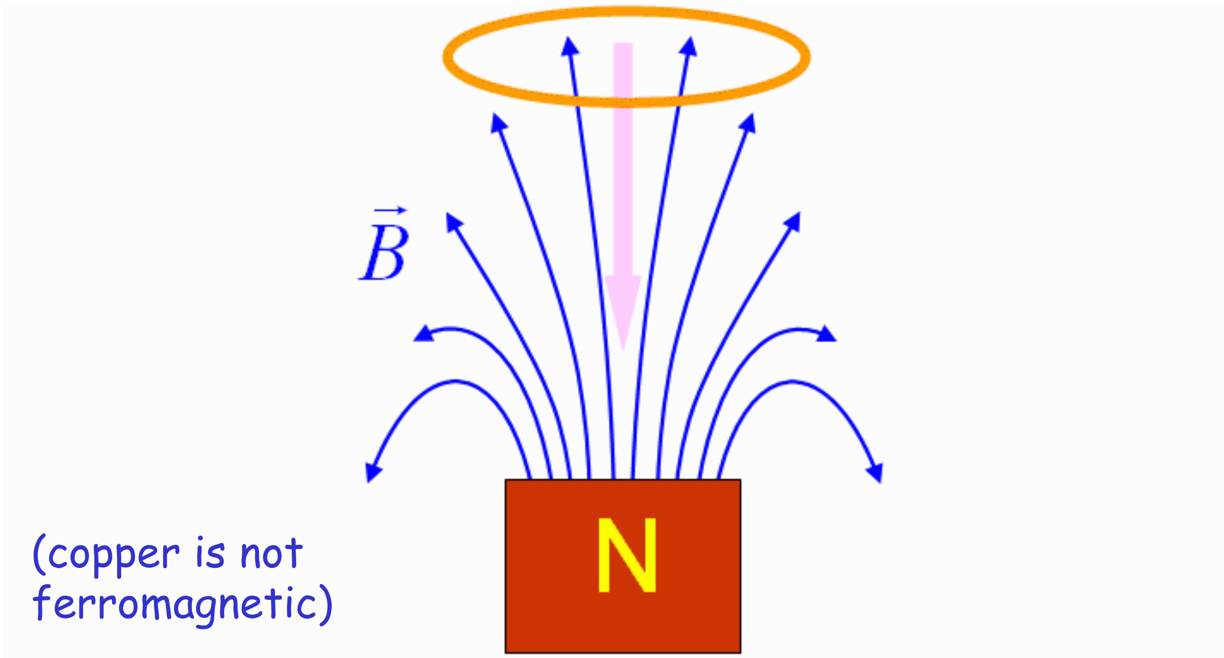
A. up ***B.*** down ***C.*** No induced field

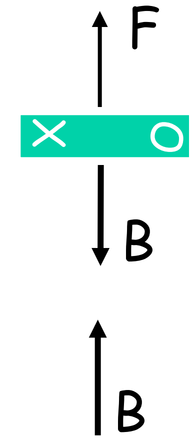
Choose direction for positive flux to be in same direction as external field (easiest), then

Increase in flux from external field is opposed by induced flux with opposite sign

Cool Example

A horizontal copper ring is dropped from rest directly above the north pole of a permanent magnet





Like poles repel

➡ $F_{total} < mg$

➡ $a < g$

Will the acceleration *a* of the falling ring in the presence of the magnet be any different than it would have been under the influence of just gravity (i.e. *g*)?

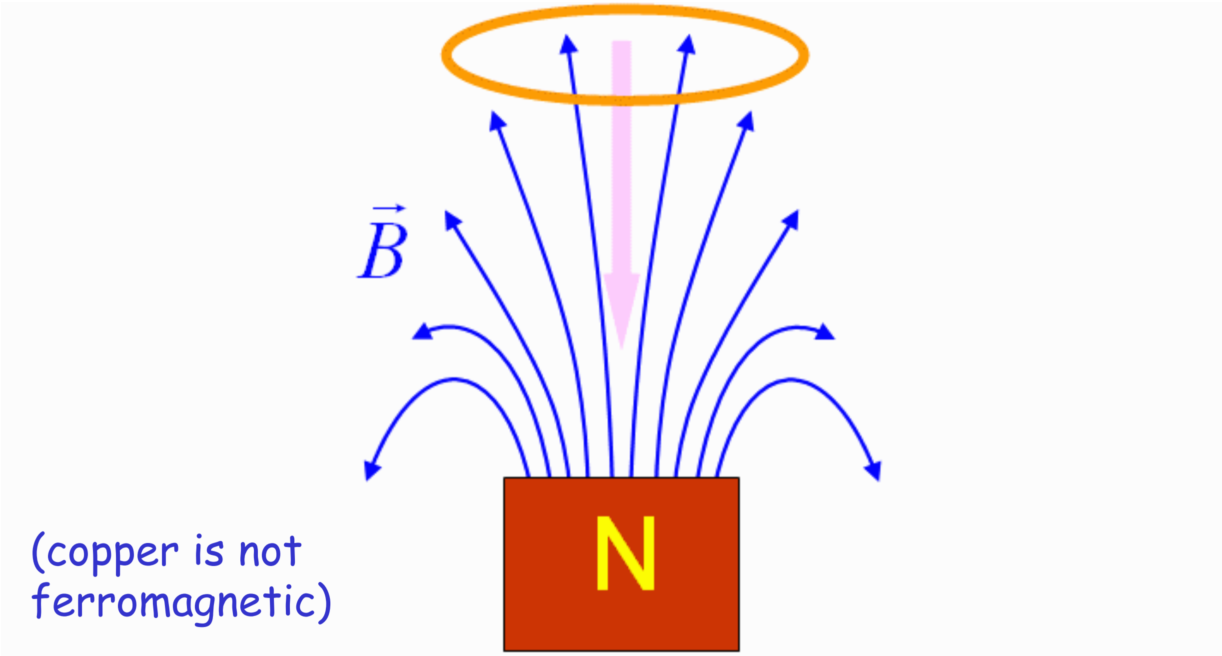
A. $a > g$ ***B.*** $a = g$ $\boxed{\textbf{C.}\ a < g}$

This one is hard !
Upward B field increases as loop falls
Clockwise current (viewed from top) is induced

Demo !
dropping magnets

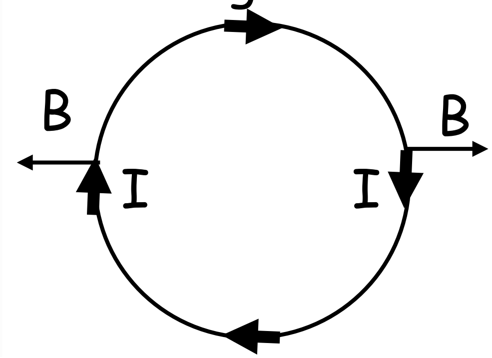
Cool Example

A horizontal copper ring is dropped from rest directly above the north pole of a permanent magnet



HOW IT WORKS

Looking down



Will the acceleration *a* of the falling ring in the presence of the magnet be any different than it would have been under the influence of just gravity (i.e. *g*)?

A. $a > g$ **B.** $a = g$ $\boxed{\textbf{C. } a < g}$

IL X B points UP

→ $F_{total} < mg$

→ $a < g$

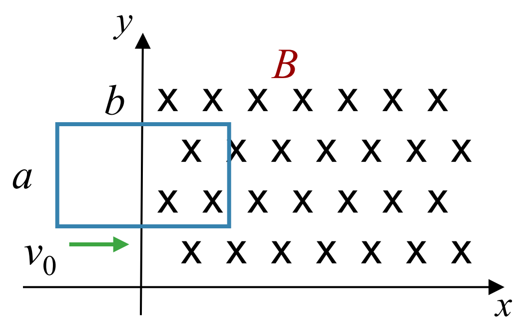
B field increases upward as loop falls
Clockwise current (viewed from top) is induced

Main Field produces horizontal forces
"Fringe" Field produces vertical force

Demo !
e-m cannon

Calculation

A rectangular loop (height = a, length = b, resistance = R, mass = m) coasts with a constant velocity v_0 in $+x$ direction as shown. At $t = 0$, the loop enters a region of constant magnetic field B directed in the $-z$ direction.



What is the direction and the magnitude of the force on the loop when half of it is in the field?

Conceptual Analysis

Once loop enters B field region, flux will be changing in time

Faraday's Law then says emf will be induced

Strategic Analysis

Find the emf

Find the current in the loop

Find the force on the current

Calculation

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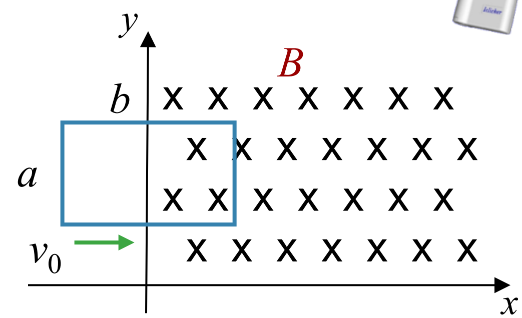
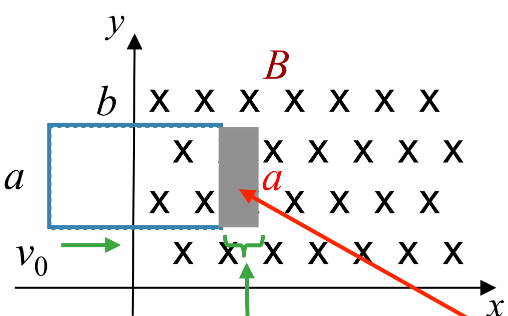


What is the magnitude of the emf induced in the loop just after it enters the field?

$$emf = -\frac{d\Phi_B}{dt}$$

A) $\varepsilon = Babv_0^2$ B) $\varepsilon = ½\, Bav_0$ C) $\varepsilon = ½\, Bbv_0$ $\boxed{\text{D) } \varepsilon = Bav_0}$ E) $\varepsilon = Bbv_0$



In a time dt
it moves by $v_0 dt$

The area in field
changes by $dA = v_0 dt\, a$

Change in Flux = $d\Phi_B = BdA = Bav_0 dt$

$$\frac{d\Phi_B}{dt} = Bav_o$$

Calculation

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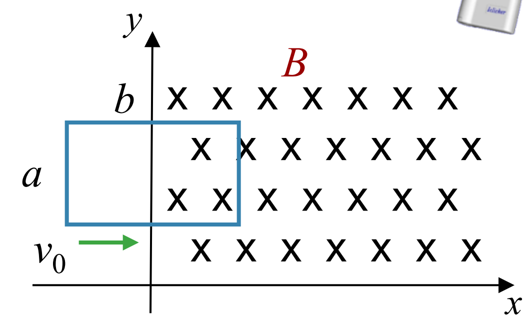


What is the direction of the current induced in the loop just after it enters the field?

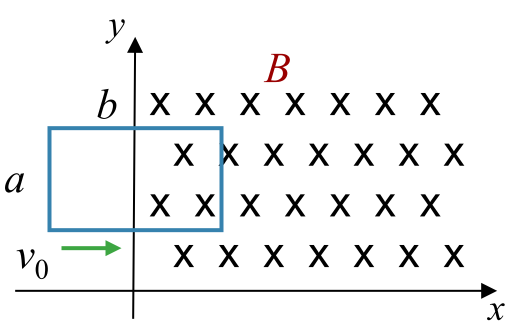
$$emf = -\frac{d\Phi_B}{dt}$$

A) clockwise

B) counterclockwise

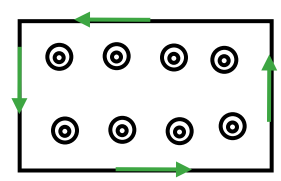
C) no current is induced

emf is induced in direction to oppose the change in flux that produced it



Flux is increasing into the screen

Induced emf produces flux out of screen



Calculation

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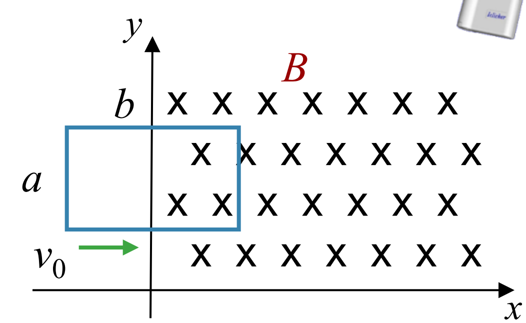
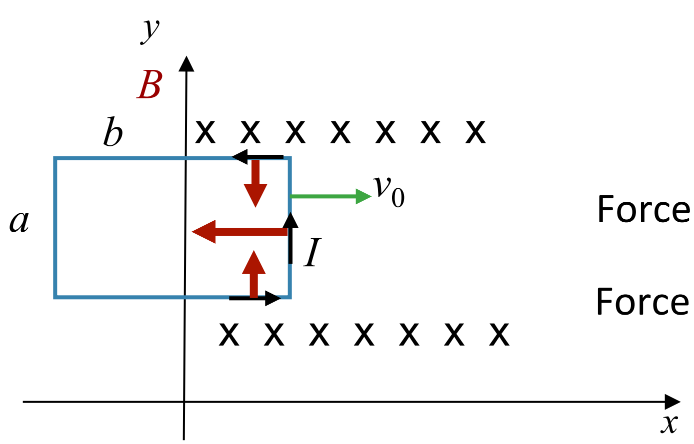


What is the direction of the net force on the loop just after it enters the field?

$$emf = -\frac{d\Phi_B}{dt}$$

A) $+y$ B) $-y$ C) $+x$ $\boxed{\text{D) } -x}$

Force on a current in a magnetic field: $\vec{F} = I\vec{L} \times \vec{B}$

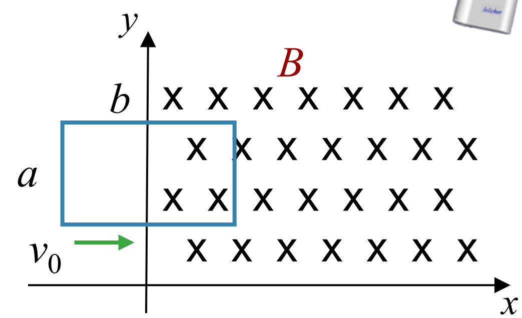


Force on top and bottom segments cancel (red arrows)

Force on right segment is directed in $-x$ direction.

Calculation

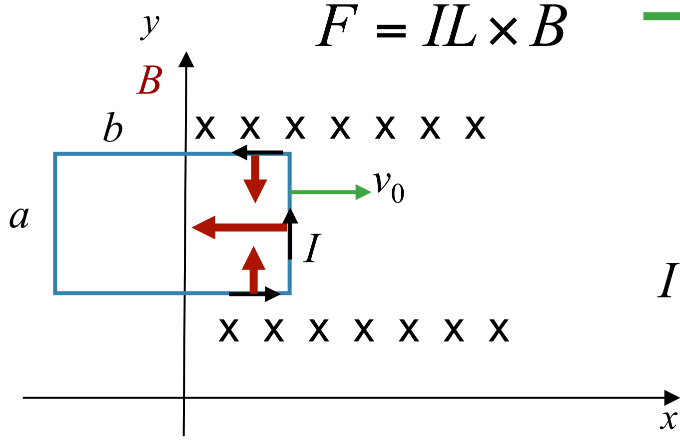
A rectangular loop (height = a, length = b, resistance = R, mass = m) coasts with a constant velocity v_0 in $+x$ direction as shown. At $t = 0$, the loop enters a region of constant magnetic field B directed in the $-z$ direction.



What is the magnitude of the net force on the loop just after it enters the field?

$$\vec{F} = I\vec{L} \times \vec{B} \qquad \varepsilon = Bav_0 \qquad emf = -\frac{d\Phi_B}{dt}$$

A) $F = 4aBv_oR$ B) $F = a^2Bv_oR$ C) $F = a^2B^2v_o^2/R$ $\boxed{\text{D) } F = a^2B^2v_o/R}$



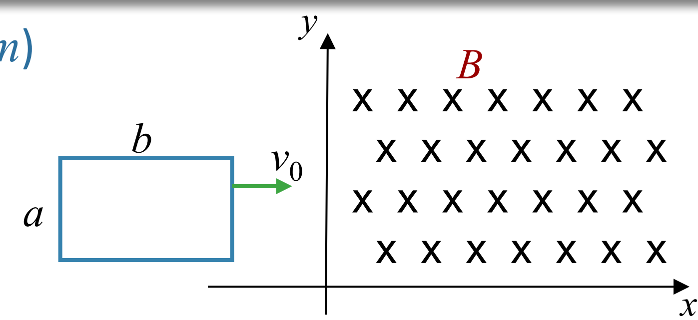
$$\vec{F} = I\vec{L} \times \vec{B} \rightarrow F = ILB \text{ since } \vec{L} \perp \vec{B}$$

$$I = \frac{\varepsilon}{R} = \frac{Bav_o}{R} \longrightarrow F = \left(\frac{Bav_o}{R}\right)aB = \frac{B^2a^2v_o}{R}$$

ILB

Follow Up

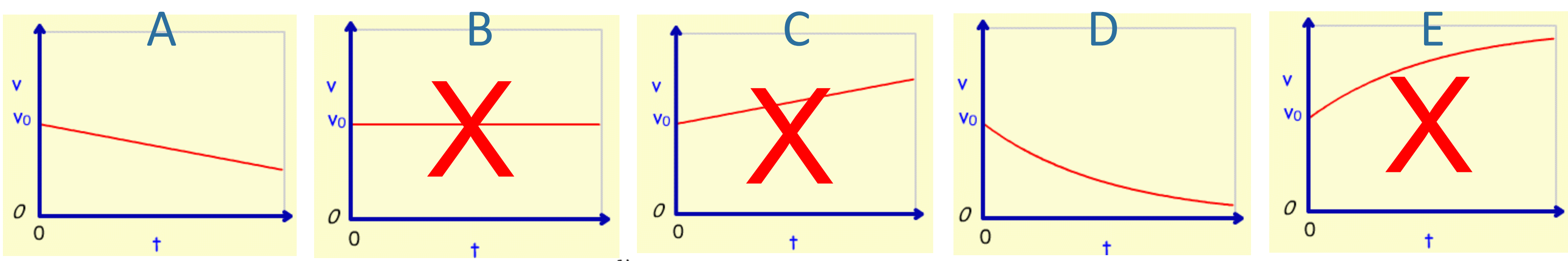
A rectangular loop (sides = a,b, resistance = R, mass = m) coasts with a constant velocity v_0 in $+x$ direction as shown. At $t = 0$, the loop enters a region of constant magnetic field B directed in the $-z$ direction.



$t = dt$: $\varepsilon = Bav_0$

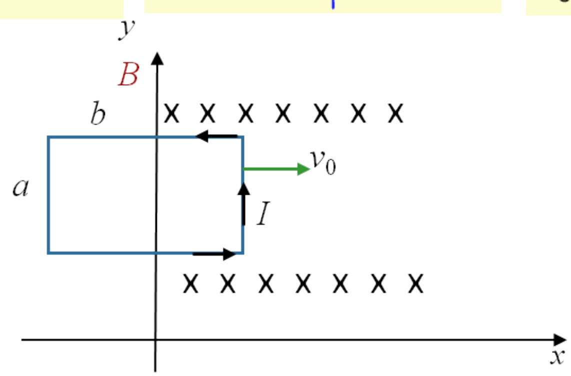
What is the velocity of the loop when half of it is in the field?

Which of these plots best represents the velocity as a function of time as the loop moves form entering the field to halfway through ?



This is not obvious, but we know v must decrease

Why?



F_{right} points to left

Acceleration negative

Speed must decrease

Follow Up

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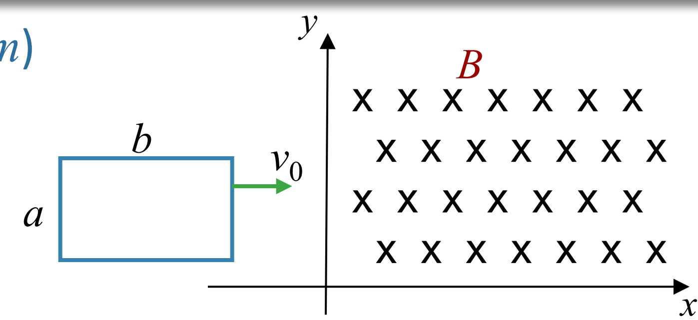
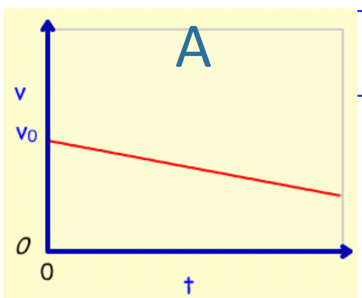
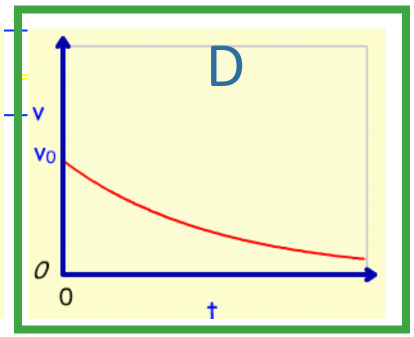


$$\varepsilon = Bav_0$$

What is the velocity of the loop when half of it is in the field?

Which of these plots best represents the velocity as a function of time as the loop moves form entering the field to halfway through ?





Why D, not A?

F is not constant, depends on v

$$F = -\frac{a^2B^2v}{R} = m\frac{dv}{dt} \quad \Rightarrow \quad v = v_o e^{-\alpha t}$$

where $\alpha = \dfrac{a^2B^2}{mR}$

Challenge: Look at energy

Claim: The decrease in kinetic energy of loop is equal to the energy dissipated as heat in the resistor. Can you verify?