

Name: \_\_\_\_\_ Section: \_\_\_\_\_ Score: \_\_\_\_\_/20

1. Very small metal spheres A and B are on glass stands placed 0.3 m apart as in Fig. 1.

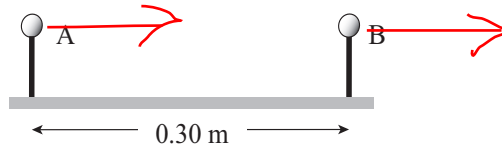


Figure 1:

- (a) Initially, A has  $5 \mu\text{C}$  and B has  $-1 \mu\text{C}$  charges. What is the force acting on A due to B? Compute its magnitude and indicate its direction in the figure with an arrow [5].

The charges have opposite signs, so the Coulomb force between A and B is attractive, and its magnitude is  $kq_Aq_B/L^2$ , where  $k = 9 \times 10^9$ ,  $L = 0.3$ , etc:

$$|F| = (9 \times 10^9) (5 \times 10^{-6}) (1 \times 10^{-6}) / (0.3)^2 = 5 \times 10^{9-12+2} = 0.5 \text{ N}.$$

- (b) After A and B are connected with a conducting wire, they are again isolated and 0.3 m apart as before. What is the force acting on B due to A? Compute its magnitude and indicate its direction in the figure with an arrow. [5]

The total charge is 4 microC, so they are evenly distributed to A and B (because charges wish to be as evenly apart as possible), 2 microC each. Now, the Coulomb force is repulsive and its magnitude is

$$|F| = (9 \times 10^9) (2 \times 10^{-6}) (2 \times 10^{-6}) / (0.3)^2 = 4 \times 10^{9-12+2} = 0.4 \text{ N}.$$

2. Look at the configuration of three charges in the figure 2. A and C have  $2 \mu\text{C}$  and B  $-2 \mu\text{C}$ .

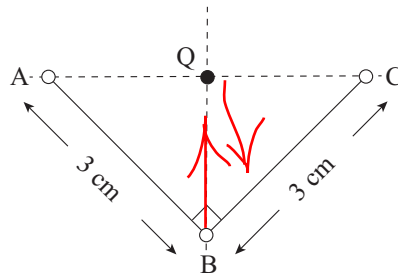


Figure 2:

(a) What is the total force acting on B from the other charges? Compute the magnitude and indicate its direction in the figure 2 with an arrow [5].

Recall the superposition principle. The x-components of the forces cancel each other, so you have only to consider the y-components. The forces are attractive, so the total force must be in the +y direction. The magnitude of the force due to A on B is

$$|F| = (9 \times 10^9) (2 \times 10^{-6}) (2 \times 10^{-6}) / (0.03)^2 = 4 \times 10^{(9-12+4)} = 40 \text{ N},$$

$$\text{Therefore, } 2 \times 40 \cos(45^\circ) = 40 \times 1.414 = 56.6 \text{ N}$$

(b) Q is the point equidistant from all three points A-C and on the line connecting A and C. What is the total force acting on a  $2 \mu\text{C}$  charge placed at Q? Compute the magnitude and indicate its direction in the figure 2 [5].

The forces due to A and C kill each other, so we have only to consider B. The force is attractive, and its magnitude is

$$|F| = (9 \times 10^9) (2 \times 10^{-6}) (2 \times 10^{-6}) / (0.03 \cos(45^\circ))^2 = 8 \times 10^{(9-12+4)} = 80 \text{ N}.$$