

Name: \_\_\_\_\_ Section: \_\_\_\_\_ Score: \_\_\_\_\_/20

1. A  $12 \mu\text{C}$  positive point charge **A** is fixed in the space.

(1) You bring another positive charge **B** of  $8 \mu\text{C}$  from infinity to a point P which is 0.3 m away from charge **A**. What is the work you have to do? (Assume there are only these two charges.) [5]

The final potential energy is

$$kQAQB/r = (9 \times 10^9) (12 \times 10^{-6}) (8 \times 10^{-6})/0.3 \\ = 2880 \times 10^{9-6-6} = 2.88 \text{ J}$$

This is +, so you must do this much of work to the charge system.

(2) Now, charge **B** is gently released from P and moves to a point 1.2 m away from the fixed **A**. Its speed is 5.2 m/s. What is the mass of the charged particle **B**? (Assume there are only these two charges.) [5]

The initial potential energy is 2.88 J as computed in (1).

The final electrical potential energy is

$$kQAQB/r' = (9 \times 10^9) (12 \times 10^{-6}) (8 \times 10^{-6})/1.2 = 0.72 \text{ J}$$

This is  $2.88 \times (0.3/1.2)$ .

Energy conservation tells us the difference must be the kinetic energy:

$$\text{initial pot energy} + 0 \text{ kinetic energy} = \text{final pot energy} + (1/2)mv^2$$

so

$$(1/2) m v^2 = 2.88 - 0.72 = 2.16.$$

Hence.

$$m = 2 \times 2.16/(5.2^2) = 0.1598 \approx 0.16 \text{ kg}.$$

2. There are four charges A - D on the plane. The equipotential curves are described in the following figure.

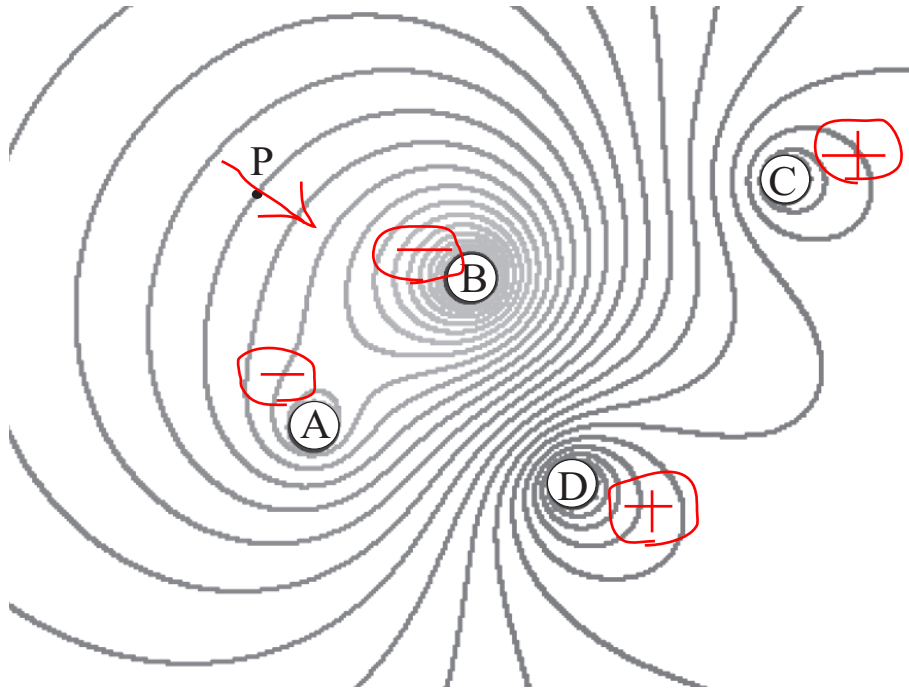


Figure 1:

(1) Suppose A is negatively charged. State the signs of all the remaining charges B - D.

(2) Which charge has the largest magnitude?

B

(3) Indicate the direction of the electric field at P. You must explain your choice succinctly.

Since A and B are negative, the right side of P should be with lower electrical potential.