

Name: \_\_\_\_\_ Section: \_\_\_\_\_ Score: \_\_\_\_\_/20

1. Very small identical metal spheres A and B are on glass stands placed 0.3 m apart as in Fig. 1.

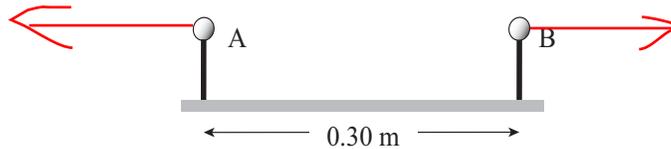


Figure 1:

(a) Initially, A has  $-3 \mu\text{C}$  and B has  $-1 \mu\text{C}$ . What is the force acting on A due to B? Compute its magnitude and draw its direction in the figure with an arrow. [5]

The force is repulsive, and its magnitude is

$$|F| = (9 \times 10^9) (3 \times 10^{-6}) (1 \times 10^{-6}) / (0.3)^2 = 3 \times 10^{9-12+2} = 0.3 \text{ N}$$

(b) After A and B are connected with a conducting wire, they are again isolated as before without moving them. What is the force acting on B due to A? Compute its magnitude and draw its direction in the figure with an arrow. [5]

The total charge - 4 microC is evenly distributed between A and b, so they have -2 microC each. The force is repulsive and its magnitude is

$$|F| = (9 \times 10^9) (2 \times 10^{-6}) (2 \times 10^{-6}) / (0.3)^2 = 4 \times 10^{9-12+2} = 0.4 \text{ N}$$

2. On a line are two points A and B as shown in Fig. 2. At A is charge  $-3 \mu\text{C}$ , and at Q and B are unknown charges.

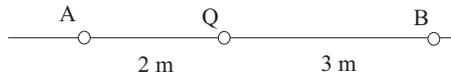


Figure 2:

(a) The force on the charge at A due to that at Q is 25 N to the left. Compute the charge at Q. [5]

Let the unknown charge be  $q$ . The force between A and Q is repulsive, so we must conclude that  $q < 0$ .

$$|F| = k|q_A q|/r^2 = (9 \times 10^9) (3 \times 10^{-6}) |q|/2^2 = (27/4) 10^3 |q| = 25.$$

Therefore,  $q = -25 \times 4 / (27 \times 10^3) = -1/270 = -3.7 \text{ mC}$ .

(b) There is no net force on the charge at Q. What is the charge at B? [5]

Since the forces from A and from B must cancel, the charge at B must have the same sign as that at A.

$$kq_A q / 2^2 = kq_B q / 3^2 \text{ or } q_A / 4 = q_B / 9$$

Therefore,

$$q_B = 9q_A / 4 = -27/4 = -6.75 \text{ microC}.$$