

Name: \_\_\_\_\_ Section: \_\_\_\_\_ Score: \_\_\_\_\_/20

1. Very small and identical metal spheres A and B are with glass handles as in Fig. 1. Initially, A has no net charge and B has a net charge  $Q$ . After the metal spheres are connected, they are separated and placed as in the right-lower figure.

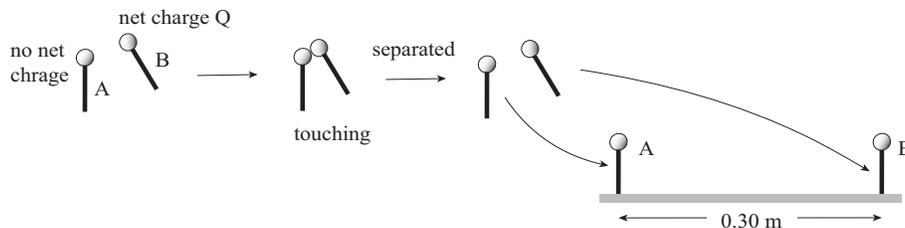


Figure 1:

(a) The magnitude of the force acting on charge at A is 10 N. What is the original net charge  $Q$  on B before touching with A? [5]

In terms of  $Q$ , the force between A and B satisfies

$$|F| = k(Q/2)^2/(0.3)^2 = (Q^2/4) \times 10^{11} = 10.$$

Therefore,  $Q^2 = 4 \times 10^{-10}$ , or  $Q = 2 \times 10^{-5} = 20 \text{ microC}$ .

We cannot determine its sign.

(b) If the above experiment is repeated with a doubled  $Q$ , what is the magnitude of the force acting on A? [5]

$F$  is proportional to the product of charges,  $F$  , must be quadrupled, or 40 N.

3. Look at the configuration of three charges in the figure 2. A and C have  $-2 \mu\text{C}$  and B  $-3 \mu\text{C}$ .

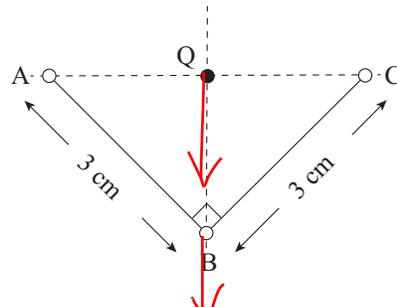


Figure 2:

(a) What is the total force acting on B from the other charges A and C? Compute its magnitude and indicate its direction in the figure 2. [5]

The x-components of the forces cancel each other, so we have only to consider the y-component. The forces are repulsive, so the resultant force must be in the -y-direction.

The magnitude of the force between A and B is

$$|F| = (9 \times 10^9) (2 \times 10^{-6}) (3 \times 10^{-6}) / (0.03)^2 = 6 \times 10^{9-12+4} = 60 \text{ N.}$$

Therefore,  $60 \times 2 \cos(45^\circ) = 60 \times 1.414 = 84.9 \text{ N}$  (downward).

(b) Q is the point equidistant from all three points A-C and on the line connecting A and C. What is the total force acting on a  $2 \mu\text{C}$  charge placed at Q? Compute its magnitude and indicate its direction in the figure 2. [5]

By symmetry forces due to A and C cancel each other, so we have only to consider the effect of B on Q. These charges have opposite signs, so the force is attractive and Q is sucked downward. Its magnitude is

$$|F| = (9 \times 10^9) (2 \times 10^{-6}) (3 \times 10^{-6}) / (0.03 \cos(45^\circ))^2 = 12 \times 10^{9-12+4} = 120 \text{ N.}$$