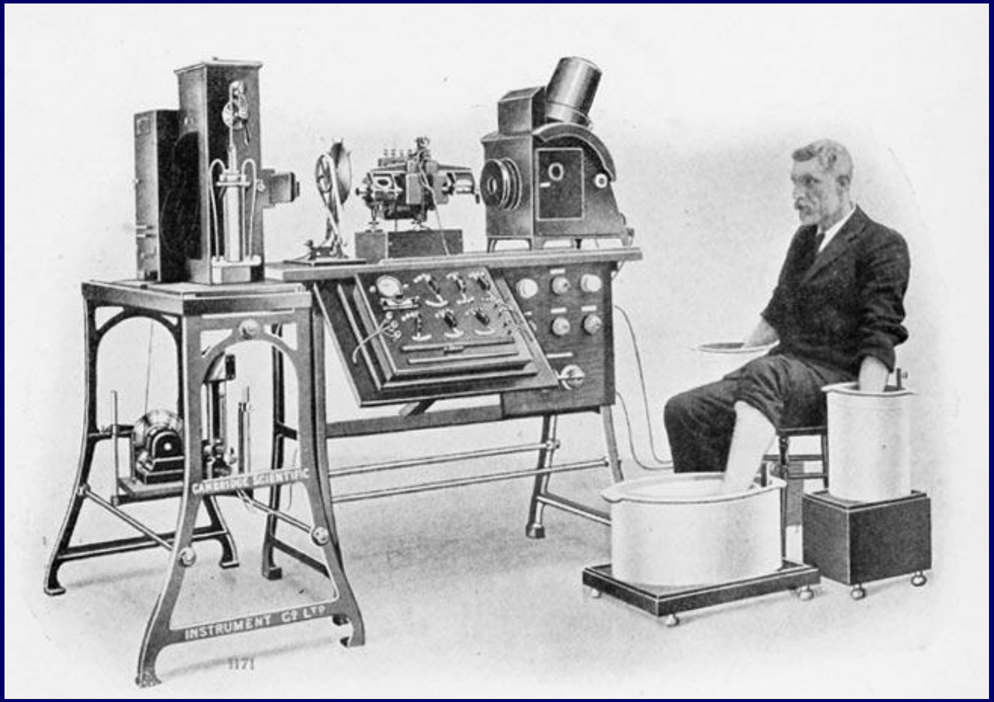
Physics 102: Lecture 3

Electric Potential Energy & Electric Potential



Overview for Today's Lecture

- Electric Potential Energy & Work
  - Uniform fields
  - Point charges

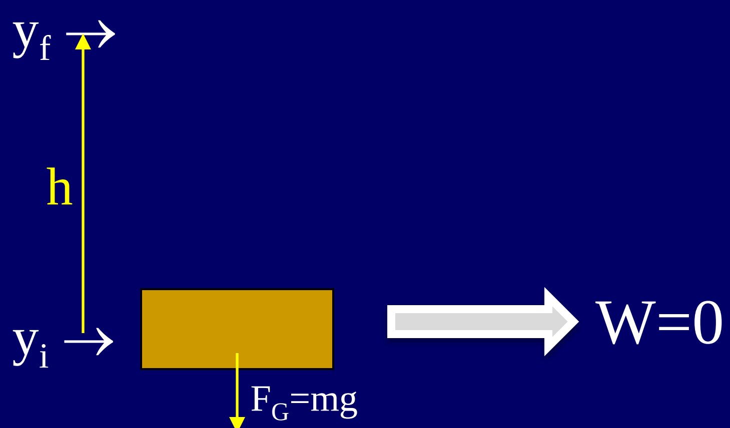
- Electric Potential (like height)
  - Uniform fields
  - Point charges

Work

$$W = F\, d \cos(\theta)$$

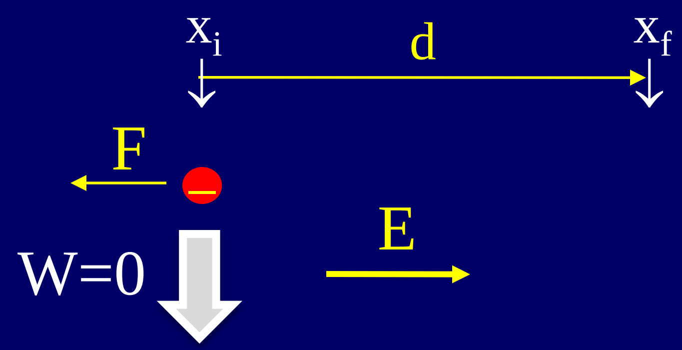
Gravity

- Brick raised $y_i \rightarrow y_f$
  - $F_G = mg$ **(down)**
  - $W_G = -mgh$
  - $W_{you} = mgh$

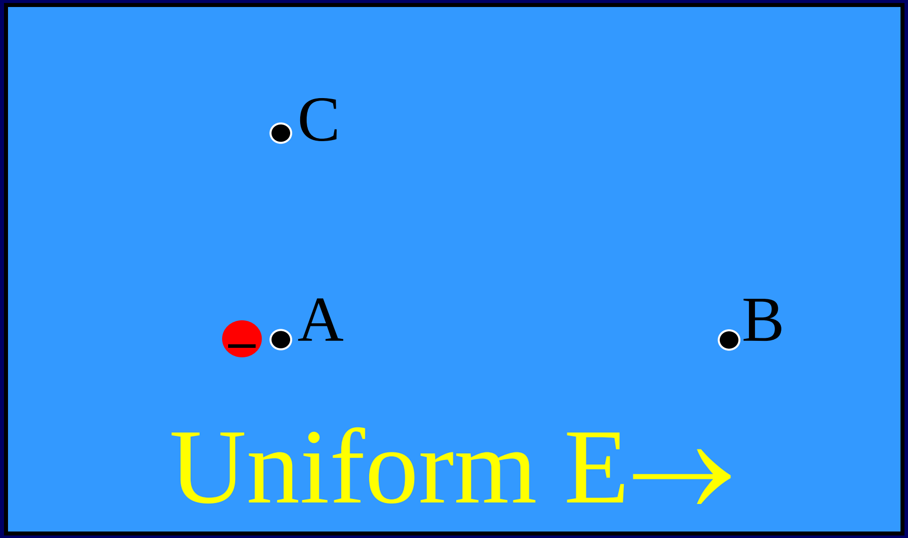


Electric

- Charge moved $x_i \rightarrow x_f$
  - $F_E = qE$ **(left)**
  - $W_E = -qEd$
  - $W_{you} = qEd$



CheckPoint 1.1



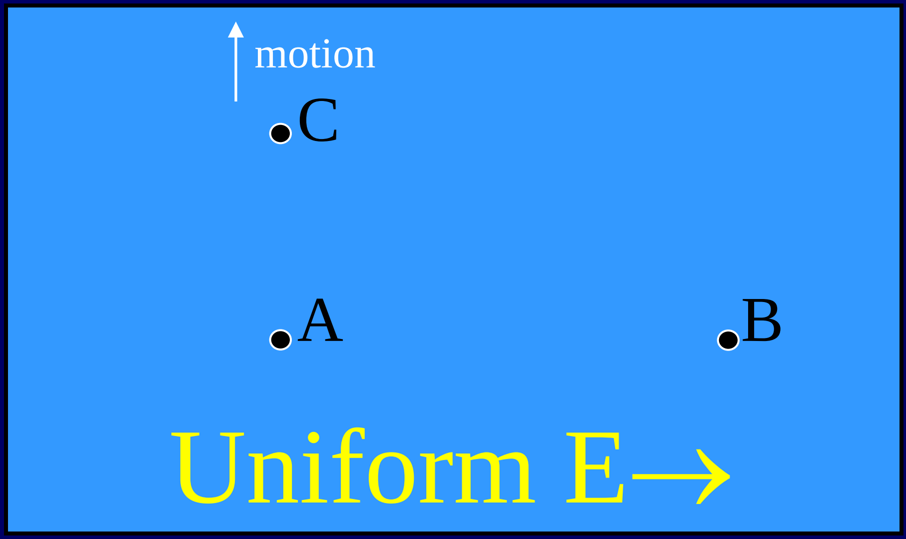
In what direction does the force on a negative charge at point A point?

1) left

2) right

3) up

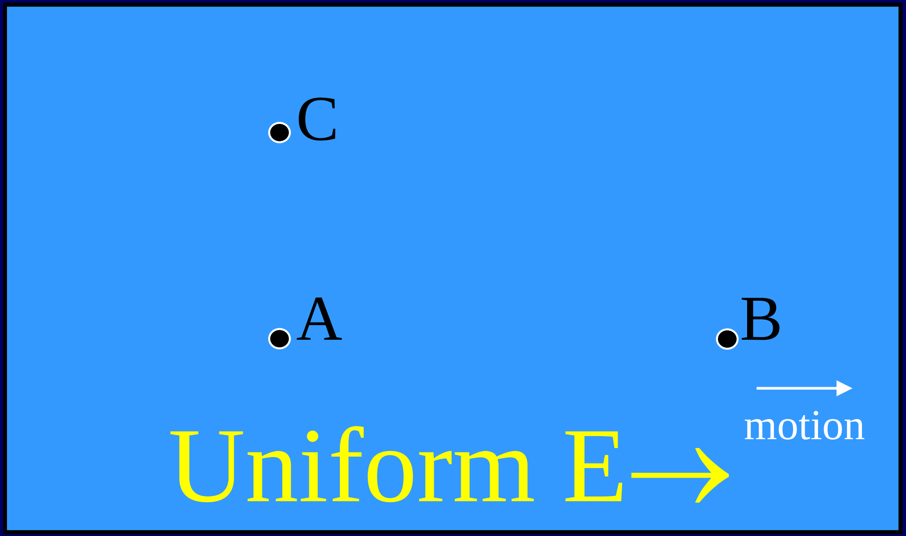
CheckPoint 1.2



When a negative charge is moved from A to C the ELECTRIC force does

1) positive work.
2) zero work.
3) negative work.

CheckPoint 1.3



When a negative charge is moved from A to B the ELECTRIC force does

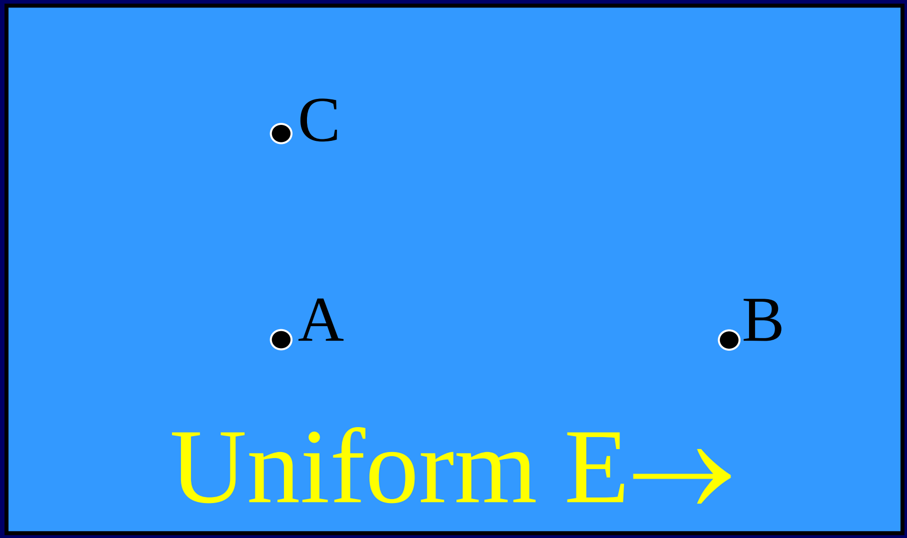
1) positive work.

2) zero work.

3) negative work.

ACT: Work

$W_{A\text{-}B}$ = work done by F_E moving charge from A to B



The negative charge is moved from A to C to B. Is the work done by the electric force:

A) Greater than $W_{A\text{-}B}$

B) Same as $W_{A\text{-}B}$

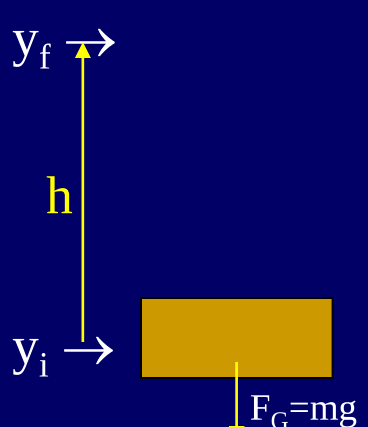
C) Less than $W_{A\text{-}B}$

Work and Δ Potential Energy

$$W_F = F\, d \cos(\theta) = -\Delta U$$

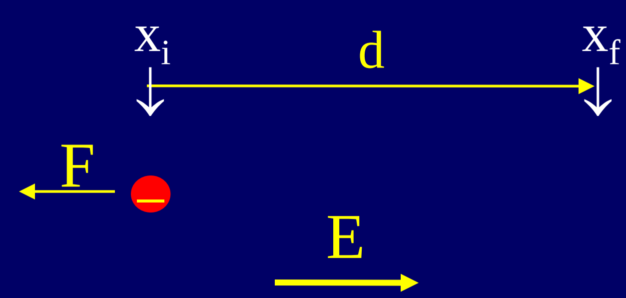
Gravity

- Brick raised $y_i \rightarrow y_f$
  - $F_G = mg$ **(down)**
  - $W_G = -mgh$
  - $\Delta U_G = +mgh$



Electric

- Charge moved $x_i \rightarrow x_f$
  - $F_E = qE$ **(left)**
  - $W_E = -qEd$
  - $\Delta U_E = +qEd$



E.P.E. for point charges

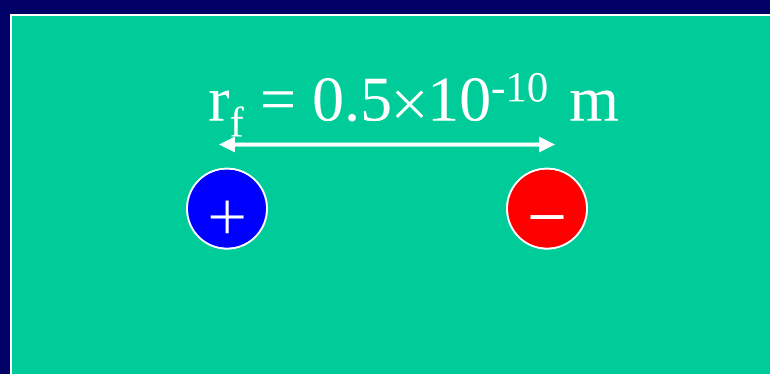
E.P.E. of two charges q_1 and q_2 separated a distance r:

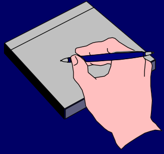
Example

$$U_E = k\frac{q_1 q_2}{r}$$

What is the <u>electric potential energy</u> of an electron a distance $r = 0.53\times10^{-10}$ m from a proton (H atom)?

$U_E = (9\times10^{9})(+1.6\times10^{-19})(-1.6\times10^{-19})/0.53\times10^{-10} = -4.35\times10^{-18}$J





Example

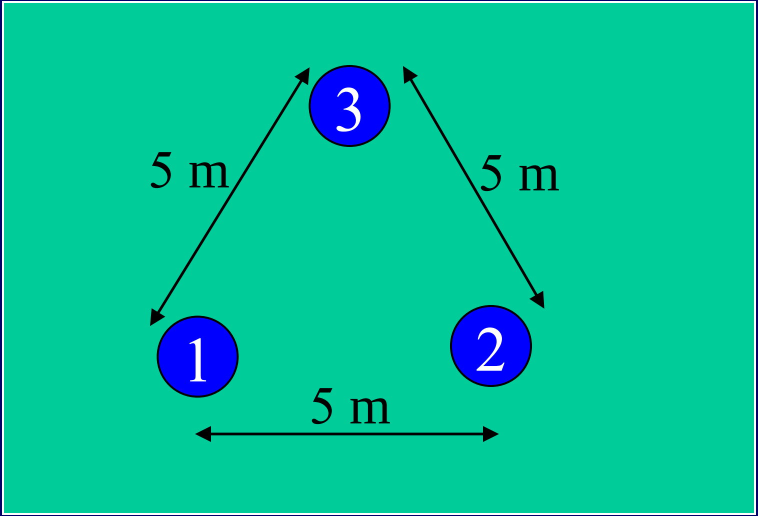
Work done by YOU to assemble 3 + charges

- $W_1 = 0$
- $W_2 = k\ q_1\ q_2\ /r$ $=(9\times10^9)(1\times10^{-6})(2\times10^{-6})/5$ $=3.6$ mJ
- $W_3 = k\ q_1\ q_3/r + k\ q_2\ q_3/r$

  $(9\times10^9)(1\times10^{-6})(3\times10^{-6})/5 + (9\times10^9)(2\times10^{-6})(3\times10^{-6})/5 = 16.2$ mJ

- $W_{total} = +19.8$ mJ
- $W_E = -19.8$ mJ
- $\Delta U_E = +19.8$ mJ

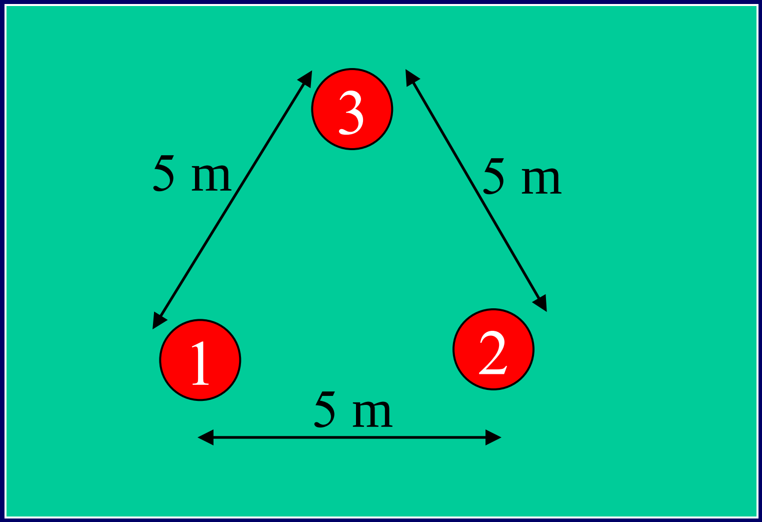
(watch signs!)



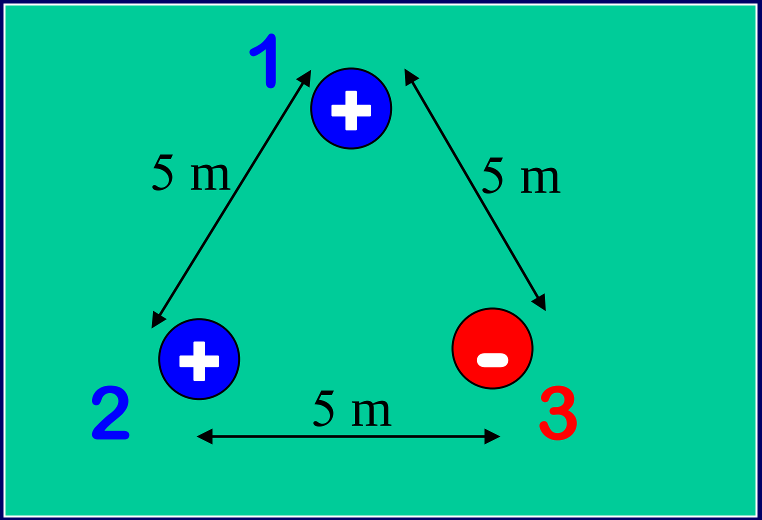
ACT: Work done by YOU to assemble 3 negative charges

How much work would it take YOU to assemble 3 negative charges?

A) W = +19.8 mJ
B) W = 0 mJ
C) W = -19.8 mJ



CheckPoint 2.1



The total work required by you to assemble this set of charges is:

(1) positive

(2) zero

(3) negative

Electric Potential

$$V \equiv U_E/q$$

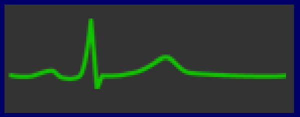
Electric potential energy per charge

- Units:

  Joules/Coulomb ≡ Volts

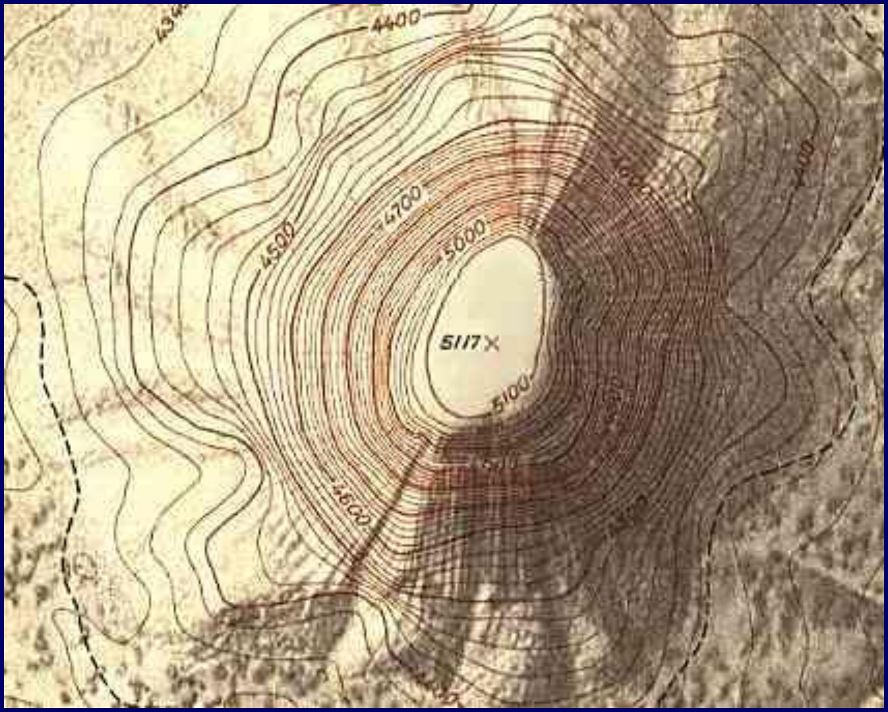
- Examples:
  - Batteries
  - EKG
- Only potential differences matter

1.5 J/C more energy!



Electric Potential (like height)

Devil's Tower

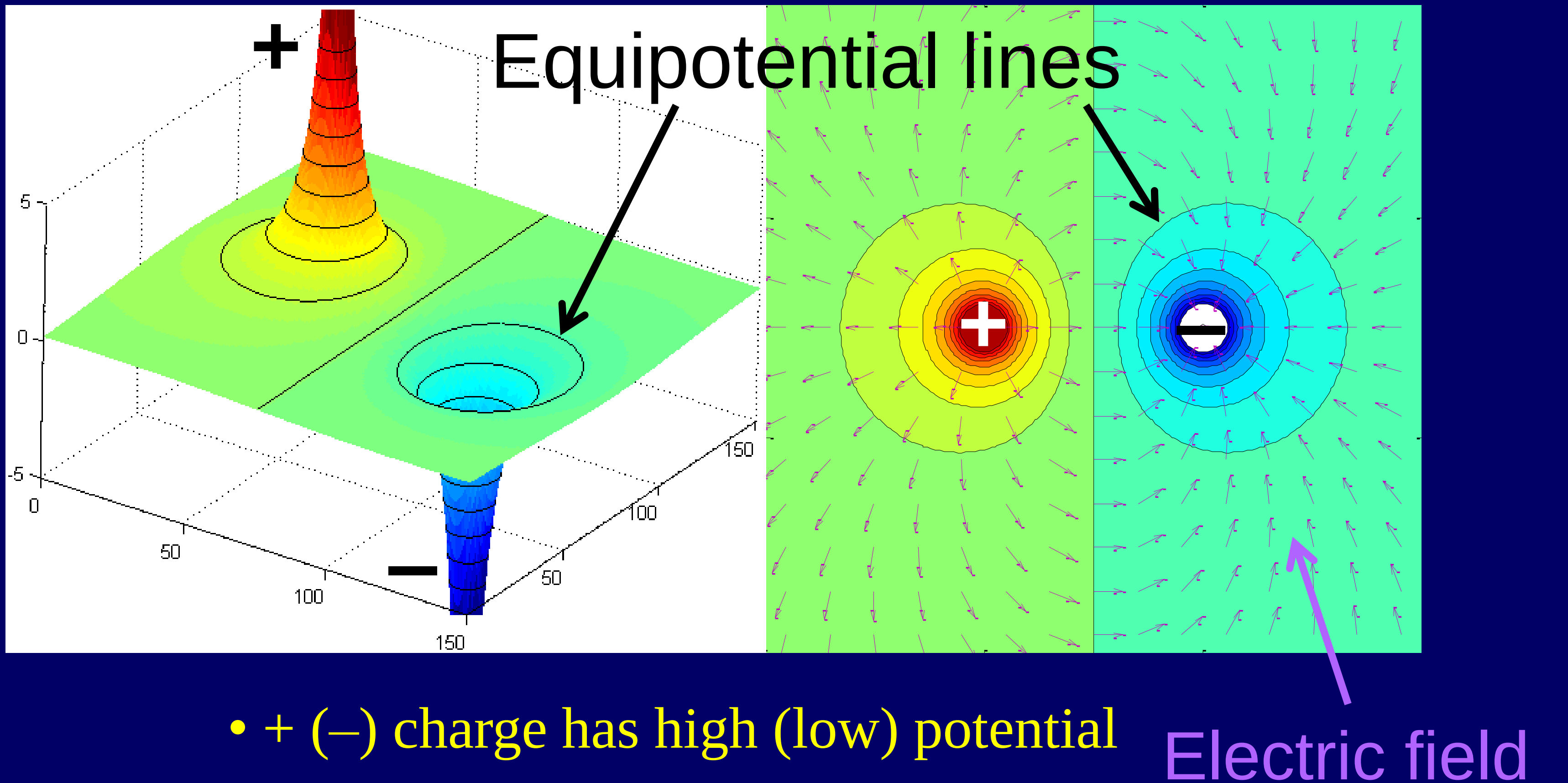


Topographical map

Moving to higher potential ⇔ moving uphill

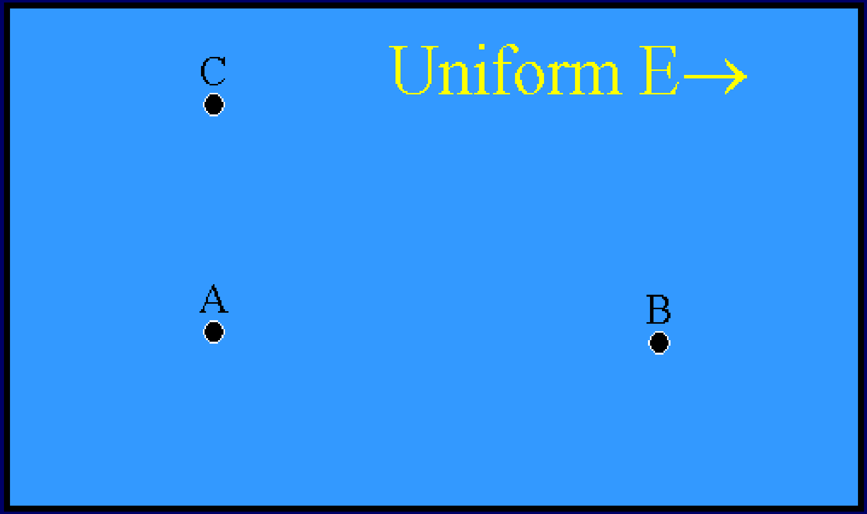
Demo: electric potential

Recall electric dipole



- + (–) charge has high (low) potential
- Equipotential lines at same “height”
- Electric field lines point “downhill”

CheckPoint 1.7



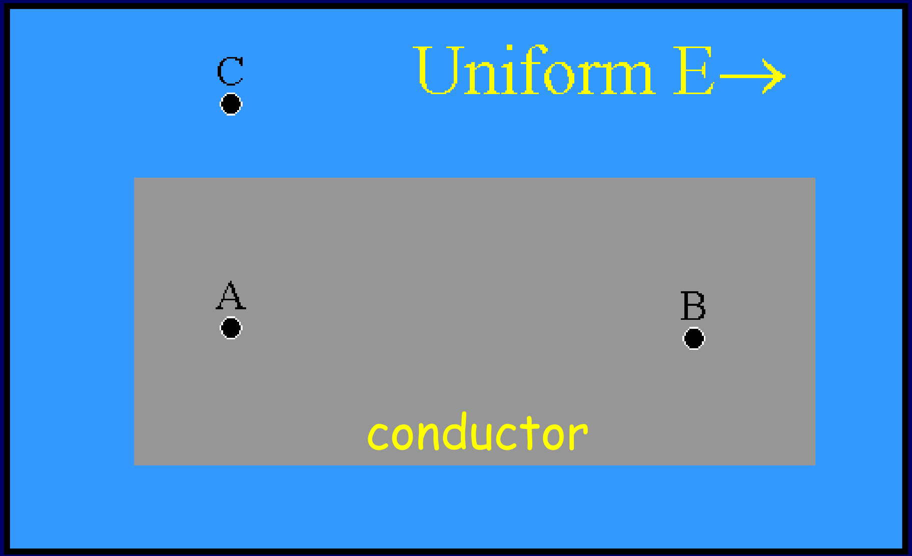
The electric potential at point A is _______ at point B

1) greater than

2) equal to

3) less than

ACT



Now points A and B lie inside a conductor…

The electric potential at point A is ________ at point B

A) greater than

B) equal to

C) less than

Potential for Point charges

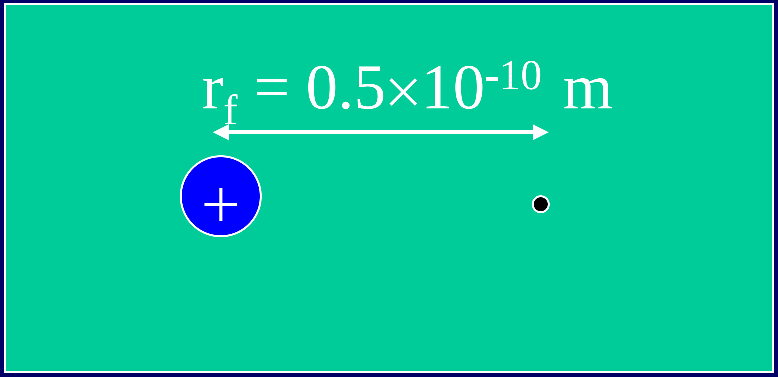
Electric potential a distance r from a charge q:

$$V \equiv U_E/q \qquad\qquad V = k\frac{q}{r}$$

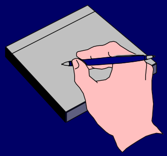
Example

What is the <u>electric potential</u> a distance $r = 0.53\times10^{-10}$ m from a proton? $(V(\infty)=0)$

$V = U_E/q = k\,q/r = (9\times10^{9})(1.6\times10^{-19})/0.53\times10^{-10} = 27.2$ Volts

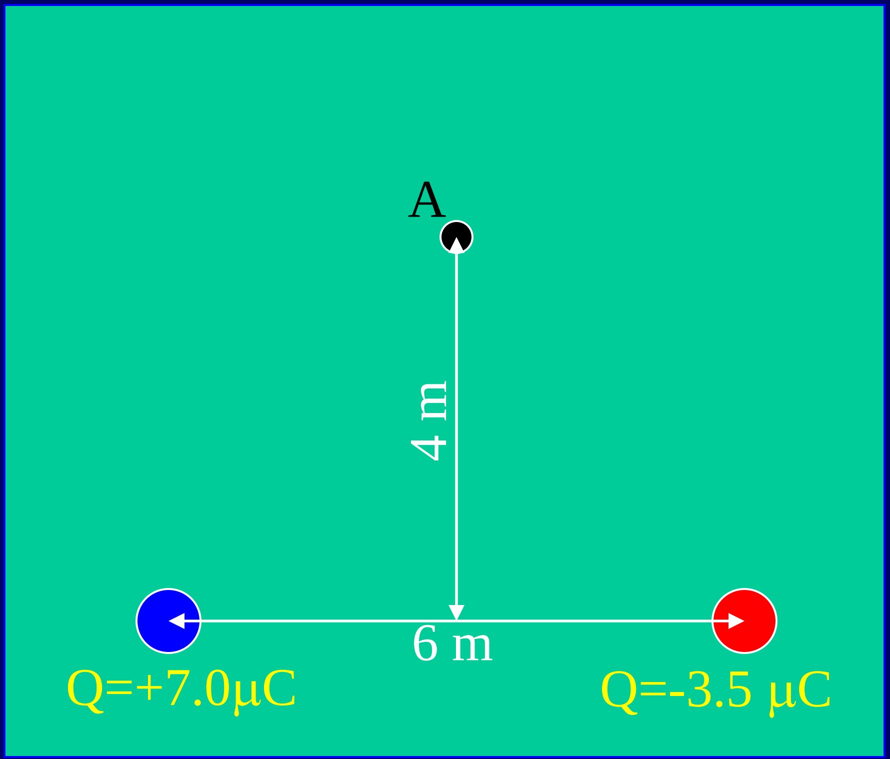


Example



Two Charges

- Calculate electric potential at point A due to charges
  - Calculate V from +7μC charge
  - Calculate V from –3.5μC charge
  - Add (EASY! NO VECTORS)



$V = kq/r$

$V_7 = (9\times10^9)(7\times10^{-6})/5 = 12.6\times10^3 V$

$V_3 = (9\times10^9)(-3.5\times10^{-6})/5 = -6.3\times10^3 V$

$V_{total} = V_7+V_3 = +6.3\times10^3 V$

How much work do you have to do to bring a 2 μC charge from far away to point A?

$W=\Delta U=Vq$

$= (+6.3\times10^3 V)(2\mu C)$

$= +12.6 \text{ mJ}$

Comparison:
Electric *Potential Energy* vs. Electric *Potential*

- Electric Potential Energy (U) - the energy of a charge at some location.
- Electric Potential (V) - found for a location only – tells what the EPE *would be* if a charge were located there (usually talk about potential differences between two locations):

$$U = Vq$$

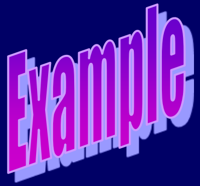
- Neither has direction, just value.

  Sign matters!

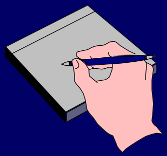
Relationship between F, E, U_E, V

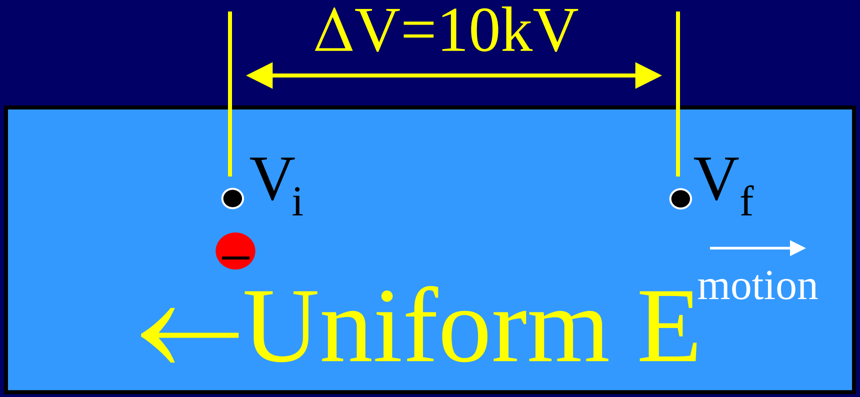
	Vector	Number ("scalar")
Property of interacting charges	**F** [N] Ex: $F = k\frac{q_1 q_2}{r^2}$	**U_E** [J] Ex: $U_E = k\frac{q_1 q_2}{r}$
Property of point in space	**E** [N/C]=[V/m] $E \equiv F/q$ Ex: $E = k\frac{q}{r^2}$	**V** [J/C]=[V] $V \equiv U_E/q$ Ex: $V = k\frac{q}{r}$

Why so many ways to describe electric force?



Electron microscope





- What is the final velocity of the electron?
- Solve by conservation of energy:

$$K.E._i + P.E._i = K.E._f + P.E._f$$

$$0 + -eV_i = \tfrac{1}{2}mv^2 + -eV_f$$

$$v = \sqrt{\frac{2e\Delta V}{m}} = \sqrt{\frac{2(1.6\times10^{-19})(1\times10^{4})}{9.1\times10^{-31}}}$$

$$= 5.9\times10^{7}\, m/s$$

Could solve this using F=ma & kinematic equations (Phys 101) TRY AT HOME! (HARDER)