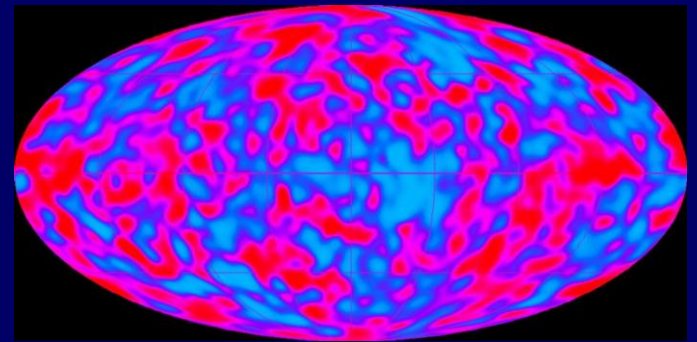


Physics 102: Lecture 22

Single Slit Diffraction
and Resolving Power

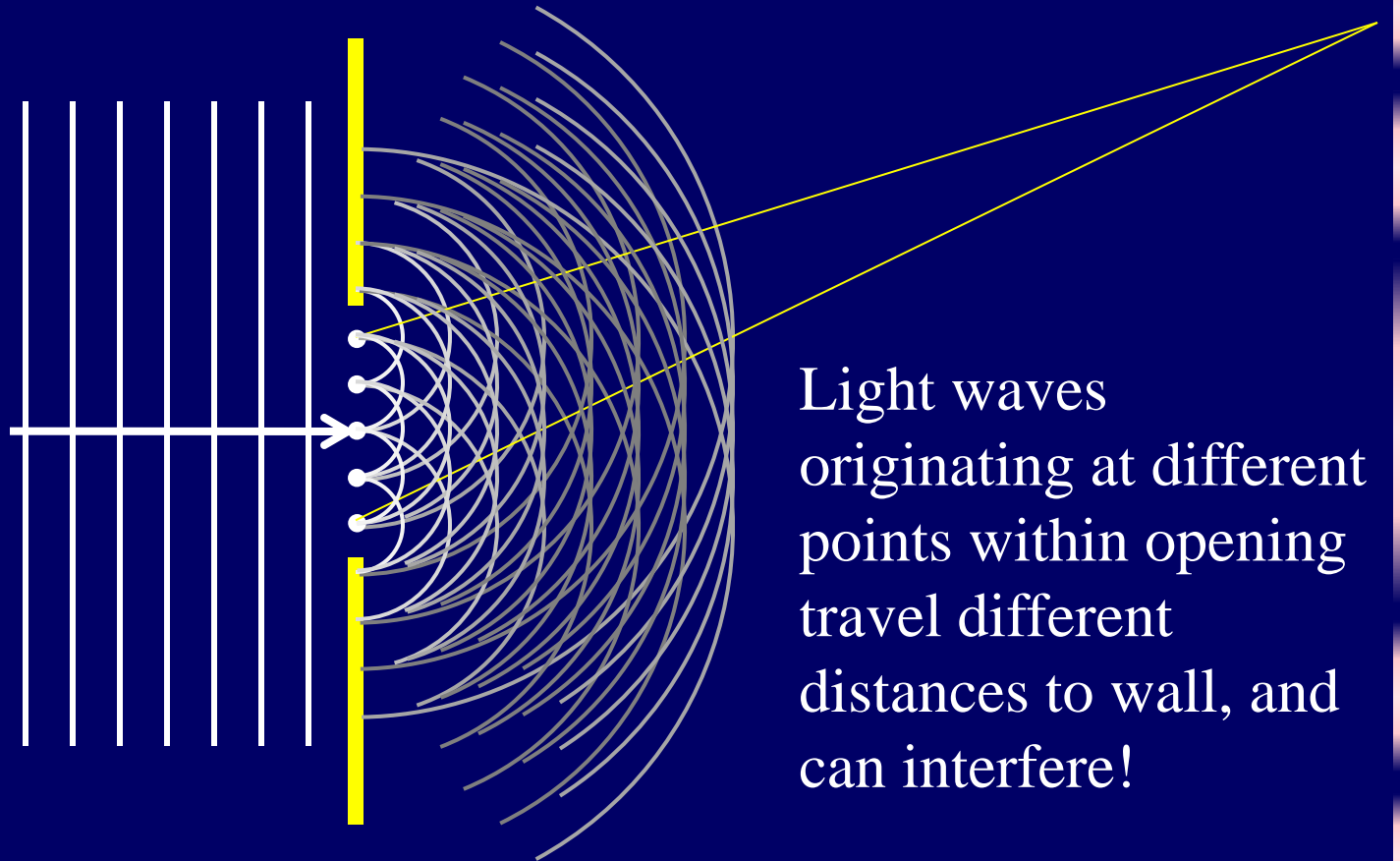


Quantum Mechanics:
Blackbody Radiation &
Photoelectric Effect

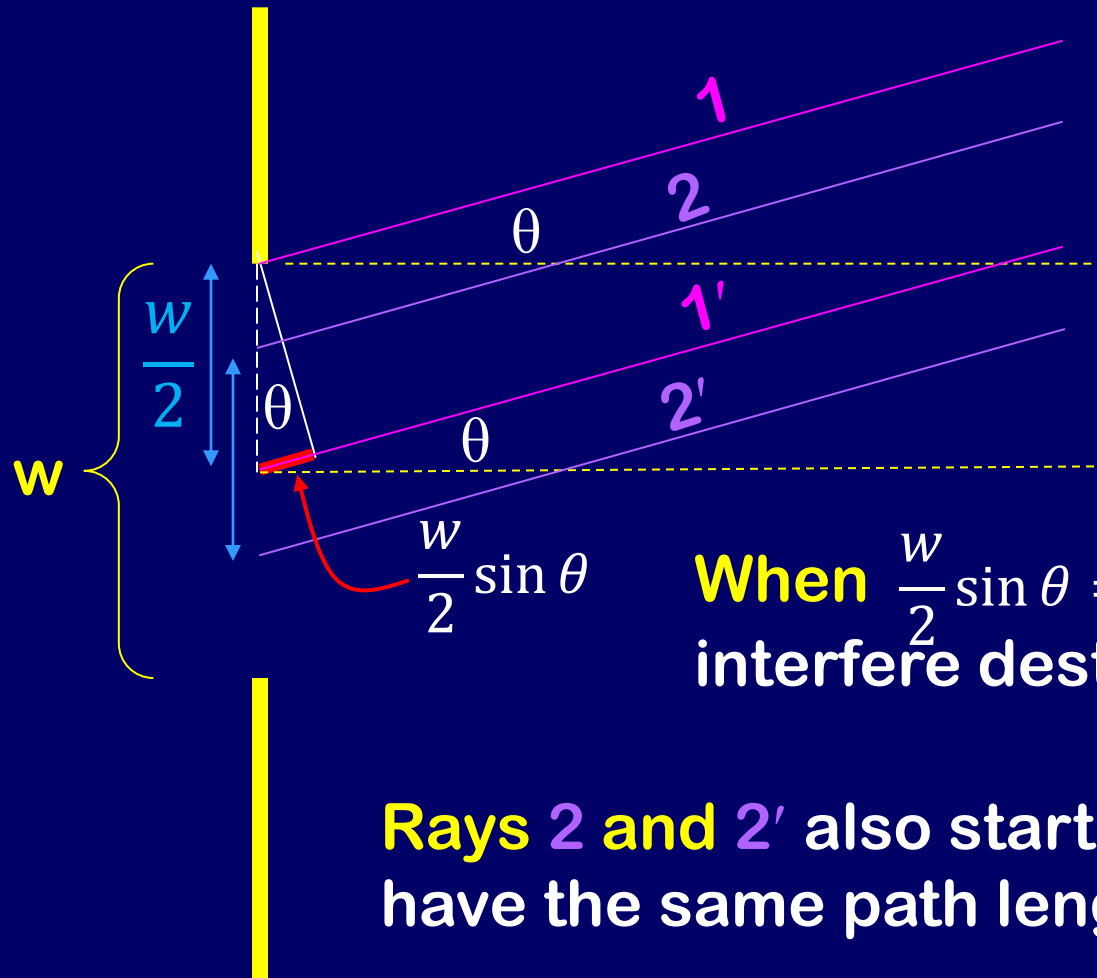
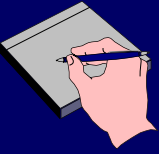


Diffraction/Huygens' principle

Huygens: Every point on a wave front acts as a source of tiny wavelets that move forward.



Single Slit Diffraction



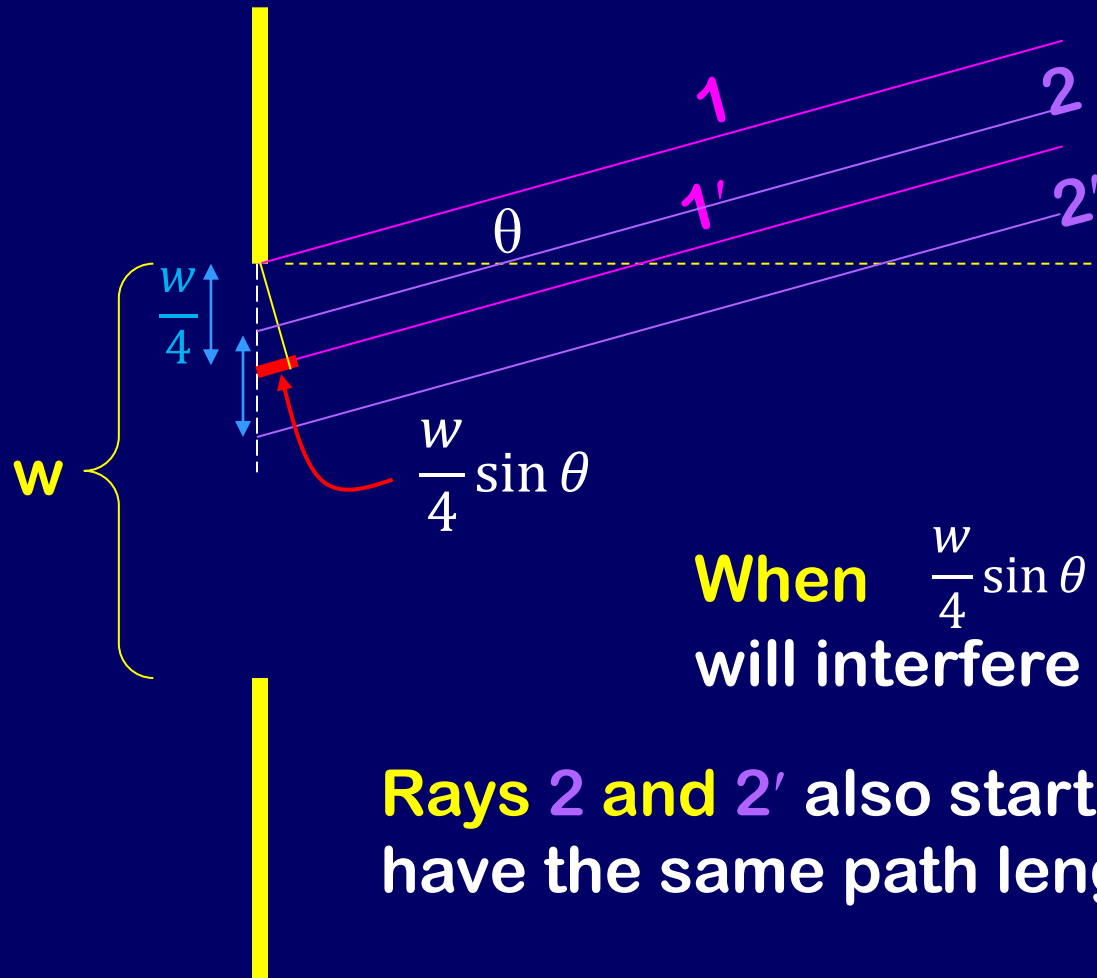
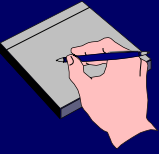
When $\frac{w}{2} \sin \theta = \frac{\lambda}{2}$ **rays 1 and 1'** interfere destructively.

Rays 2 and 2' also start $w/2$ apart and have the same path length difference.

Under this condition, every ray originating in top half of slit interferes destructively with the corresponding ray originating in bottom half.

1st minimum at $\sin \theta = \lambda/w$

Single Slit Diffraction



When $\frac{w}{4} \sin \theta = \frac{\lambda}{2}$ **rays 1 and 1'**
will interfere destructively.

Rays 2 and 2' also start $w/4$ apart and
have the same path length difference.

Under this condition, every ray originating in top quarter of slit interferes destructively with the corresponding ray originating in second quarter.

Single Slit Diffraction Summary

Condition for **halves** of slit to destructively interfere

$$\sin \theta = \frac{\lambda}{w}$$

Condition for **quarters** of slit to destructively interfere

$$\sin \theta = 2 \frac{\lambda}{w}$$

Condition for **sixths** of slit to destructively interfere

$$\sin \theta = 3 \frac{\lambda}{w}$$

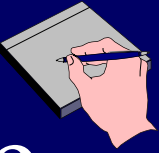
All together... $\sin \theta = m \frac{\lambda}{w}$ (**m = ±1, ±2, ±3, ...**)

THIS FORMULA LOCATES MINIMA!!

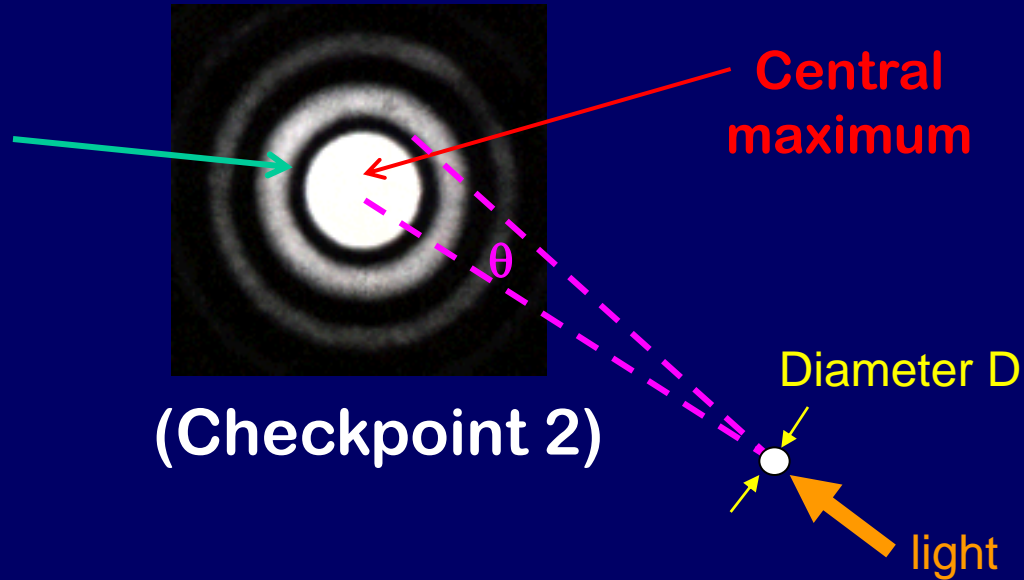
Narrower slit => broader pattern

Note: interference only occurs when $w > \lambda$

Diffraction from Circular Aperture



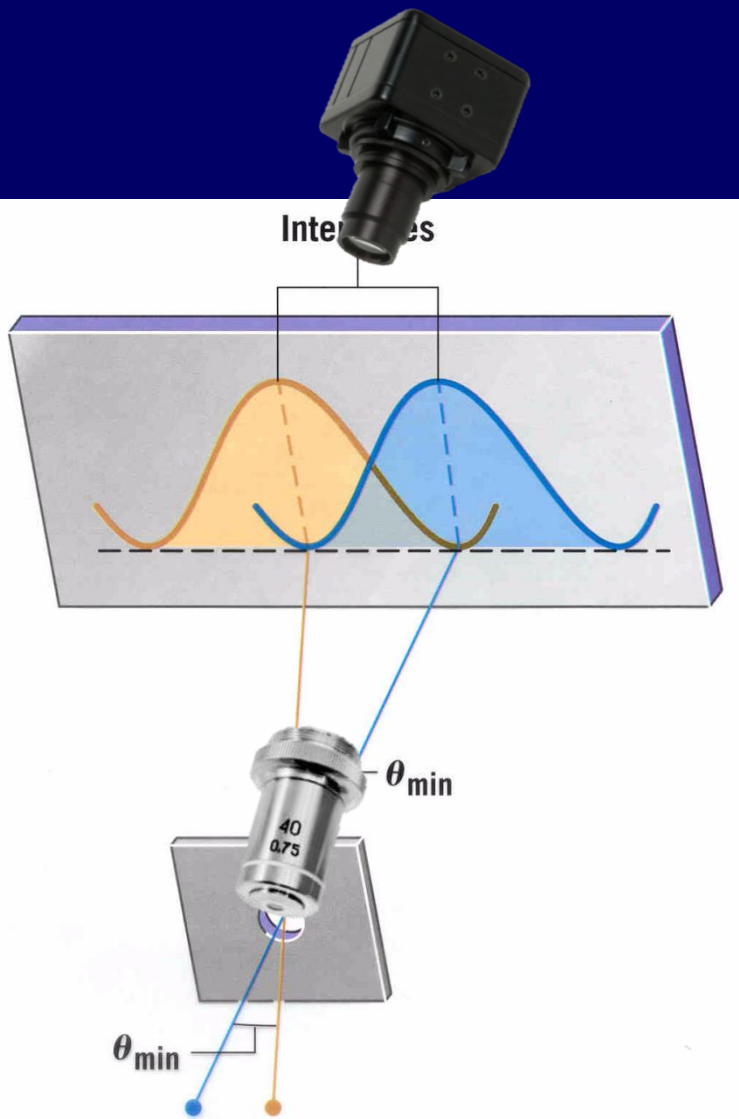
1st diffraction minimum



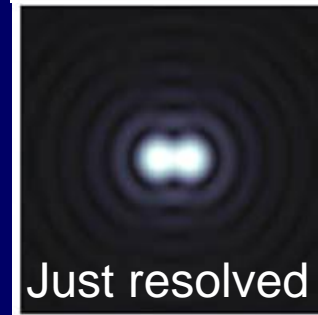
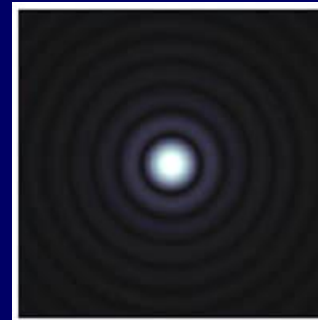
Maxima and minima will be a series of bright and dark rings on screen

First diffraction minimum is at $\sin \theta = 1.22 \frac{\lambda}{D}$

Demo: Resolving Power



Larger spacing
↓



Two objects are just resolved when the maximum of one diffraction pattern is at the minimum of the other.

These objects are *just* resolved

Resolving Power



To see two objects distinctly, need $\theta_{\text{objects}} > \theta_{\text{min}}$

θ_{objects} is angle between objects measured at aperture:

$$\theta_{\text{objects}} \approx \tan^{-1}(d/y)$$

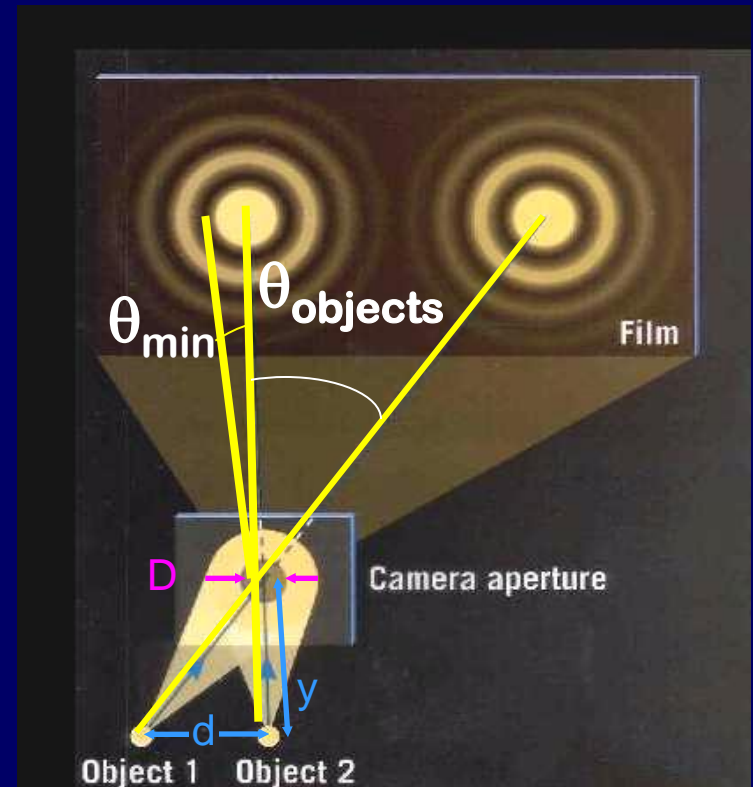
$$\theta_{\text{objects}} \approx d/y$$

(if d much smaller than y and θ in radians)

θ_{min} is minimum angular separation that aperture can resolve:

$$\sin \theta_{\text{min}} \approx \theta_{\text{min}} = 1.22 \lambda/D$$

$$d = 1.22 \lambda y/D \quad \text{Just resolved!}$$



Improve resolution by increasing D or decreasing



ACT: Resolving Power

How does the maximum resolving power of your eye change when the brightness of the room is decreased?

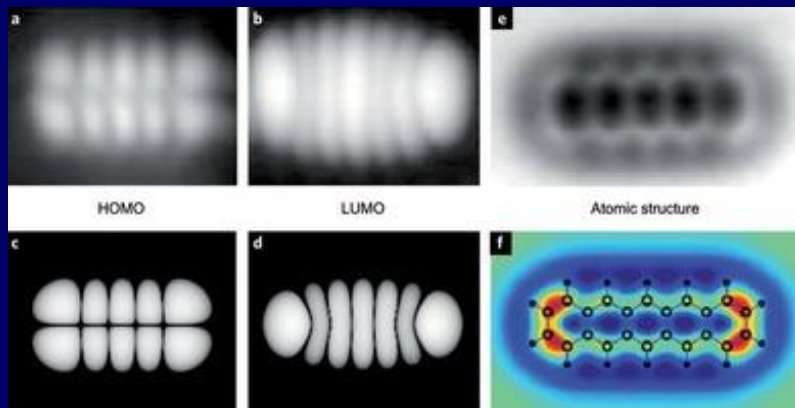
1) Increases

2) Constant

3) Decreases

Quantum Mechanics

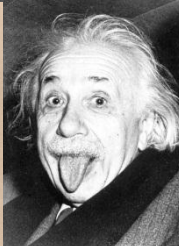
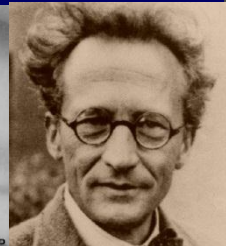
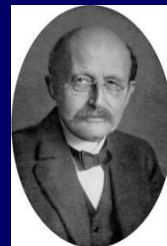
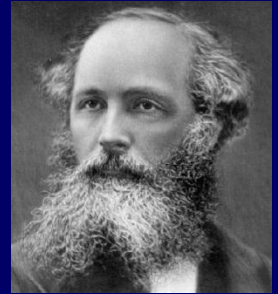
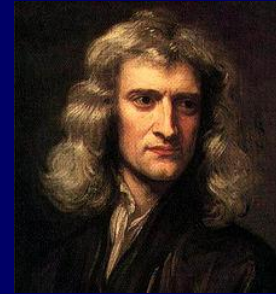
- At very small sizes the world is VERY different!
 - Energy can be discrete
 - Processes are probabilistic
 - Particles are in many places at the same time
 - Looking at something changes how it behaves



Measured & predicted electron distributions around pentacene!

State of Late 19th Century Physics

- **Two great theories** “Classical physics”
 - Newton’s laws of mechanics, including gravity
 - Maxwell’s theory of electricity & magnetism, including propagation of electromagnetic waves
- **But...some unsettling experimental results calls into question these theories**
 - The quantum revolution
 - Einstein and relativity

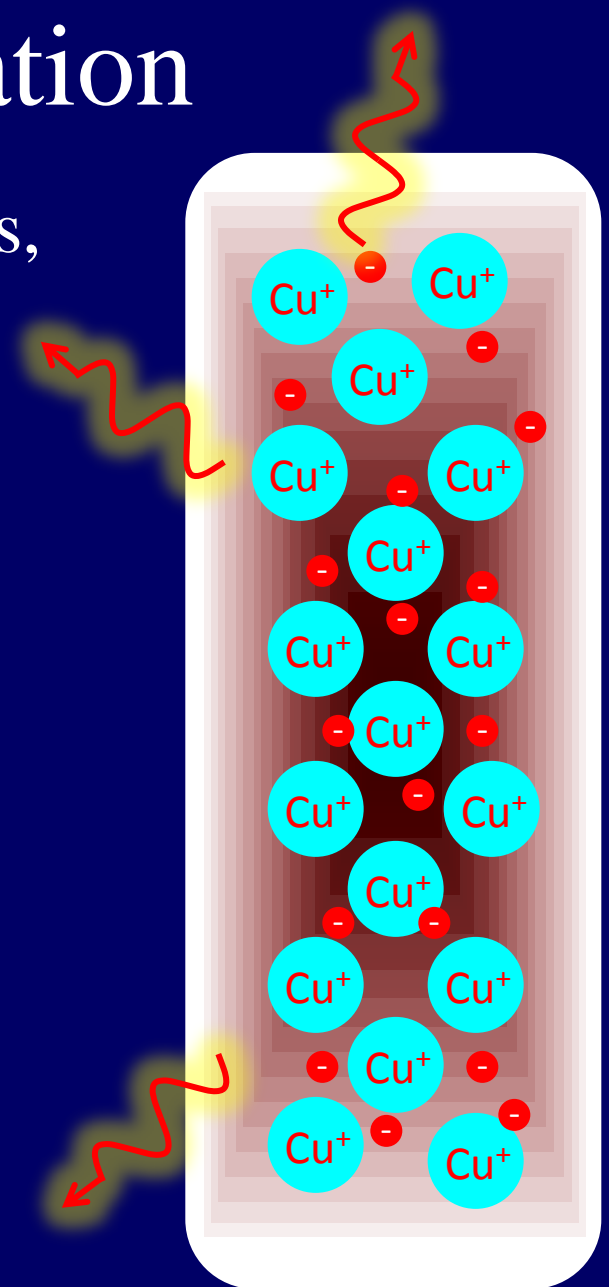


Three Early Indications of Problems with Classical Physics

- Blackbody radiation
 - Photoelectric effect
 - Wave-particle duality
- Today
- Next Lecture

Blackbody Radiation

Hot objects glow (toaster coils, light bulbs, the sun).

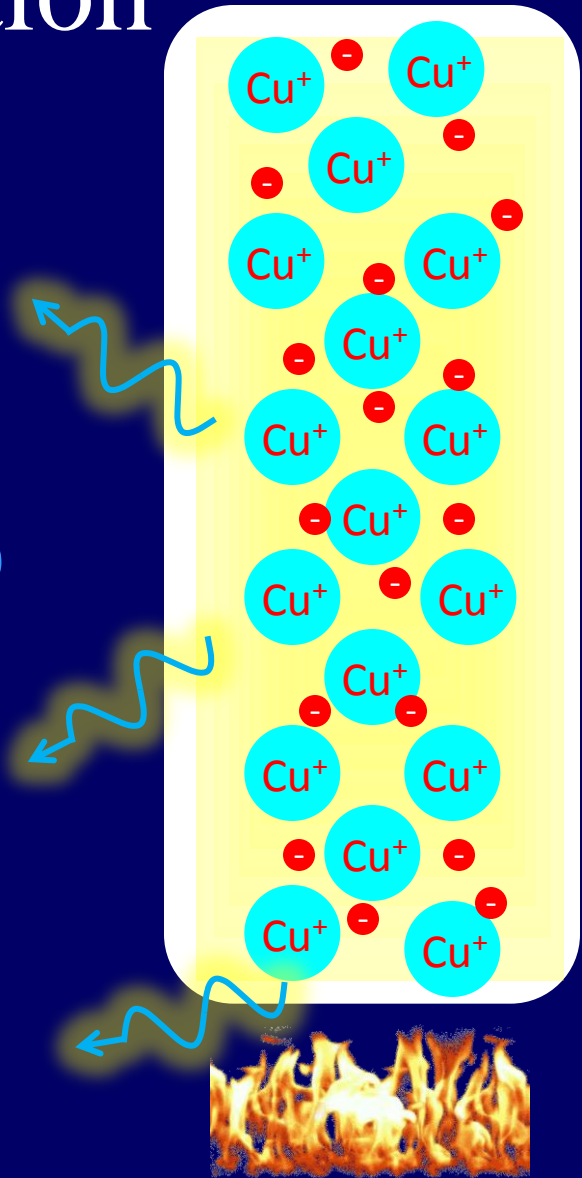


Blackbody Radiation

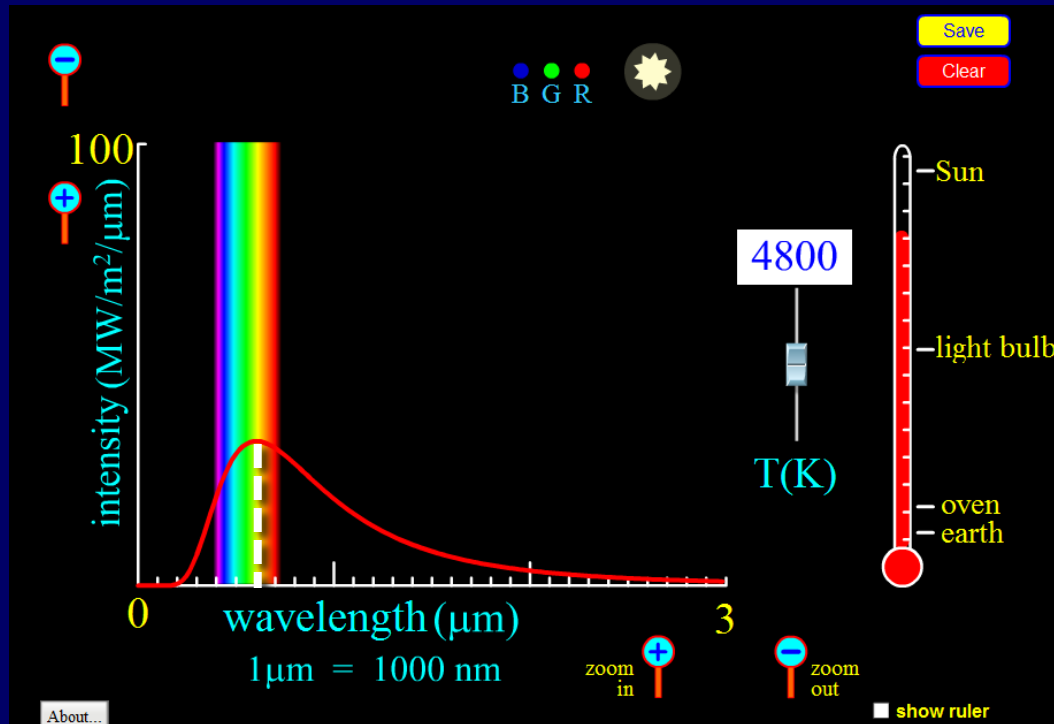
Hot objects glow (toaster coils, light bulbs, the sun).

As the temperature increases the color shifts from **Red (700 nm)** to **Blue (400 nm)**

The classical physics prediction was completely wrong! (It said that an infinite amount of energy should be radiated by an object at finite temperature)



Blackbody Radiation Spectrum



http://phet.colorado.edu/sims/blackbody-spectrum/blackbody-spectrum_en.html

Higher temperature: peak intensity at shorter λ

Wien's Displacement Law:

$$\lambda_{\max} T = 2.898 \times 10^{-3} \text{ m} \cdot \text{K}$$

λ_{\max} : wavelength for peak intensity

Blackbody Radiation: First evidence for Q.M.

Max Planck found he could explain these curves if he assumed that electromagnetic energy was radiated in discrete chunks, rather than continuously.

The “quantum” of electromagnetic energy is called the photon.

Energy carried by a single photon is

$$E = hf = hc/\lambda$$

Planck's constant: $h = 6.626 \times 10^{-34}$ Joule sec



Checkpoint 5

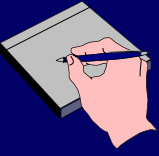
A series of light bulbs are colored red, yellow, and blue.
Which bulb emits photons with the most energy?

The least energy?

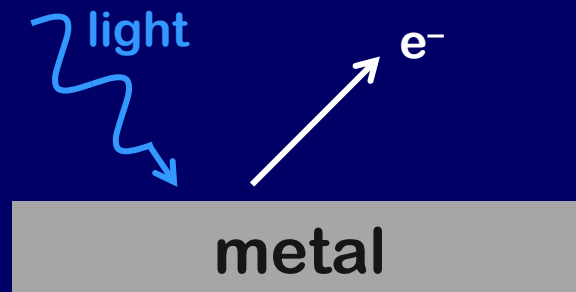
Which is hotter?

- (1) stove burner glowing red
- (2) stove burner glowing orange

Photoelectric Effect



- Light shining on a metal can “knock” electrons out of atoms.
- Light must provide energy to overcome Coulomb attraction of electron to nucleus
- Light Intensity gives power/area (i.e. Watts/m²)
 - Recall: Power = Energy/time (i.e. Joules/sec.)



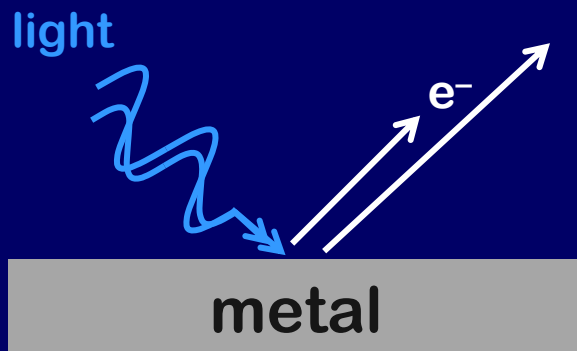
Photoelectric Effect: Light Intensity



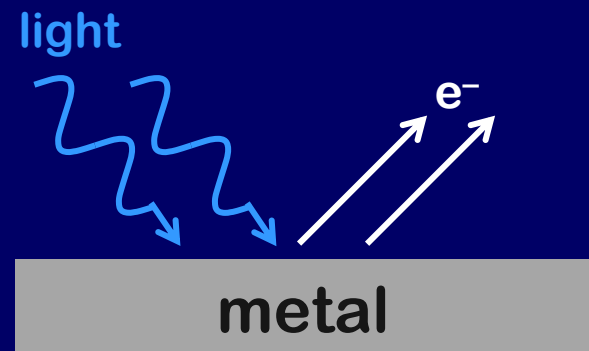
When the brightness is increased...

Rate of electron emission increases

Maximum kinetic energy of electrons unchanged



Classical



Quantum

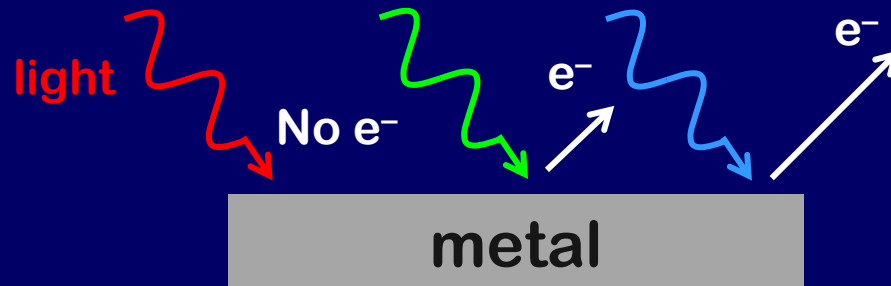


Photoelectric Effect: Light Frequency

When the frequency of the light is changed...

Emission rate unchanged, but...
electron emission only for $f > f_{\text{min}}$

Maximum electron KE increases



Photoelectric Effect Summary

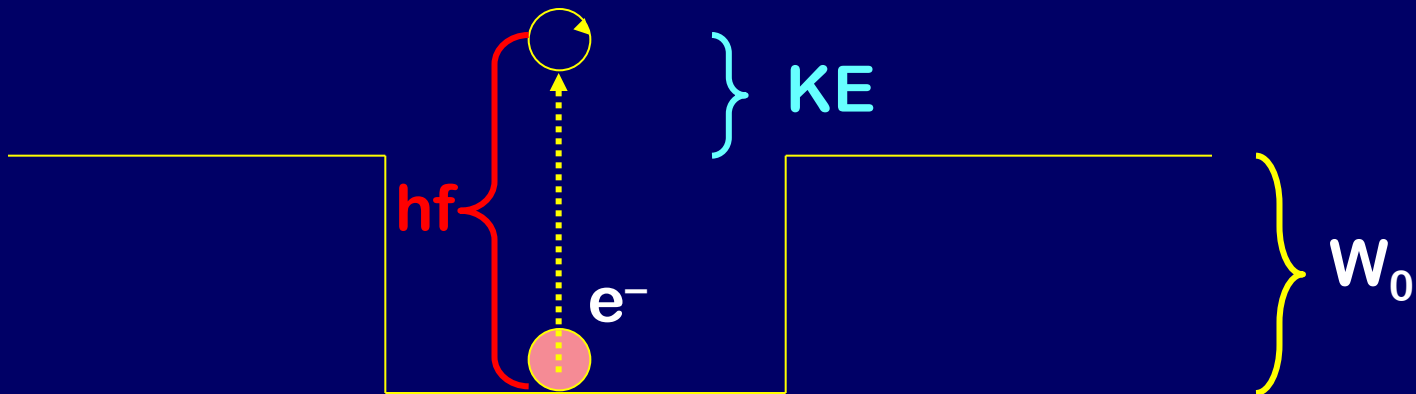
- Each metal has “Work Function” (W_0) which is the minimum energy needed to free electron from atom.
- Light comes in packets called Photons

$$E = hf$$

$$h = 6.626 \times 10^{-34} \text{ Joule sec}$$

- Maximum kinetic energy of released electrons

$$K.E. = hf - W_0$$





ACT: Photon

A red and green laser each emit 2.5mW. Which one produces more photons/second?

1) Red

2) Green

3) Same

Quantum Physics and the Wave-Particle Duality

I. Is Light a Wave or a Particle?

- Wave

- Electric and Magnetic fields act like waves
- Superposition: Interference and Diffraction

- Particle

- Photons (blackbody radiation)
- Collision with electrons in photo-electric effect

BOTH Particle AND Wave Behavior