

# Phys 102 – Lecture 21

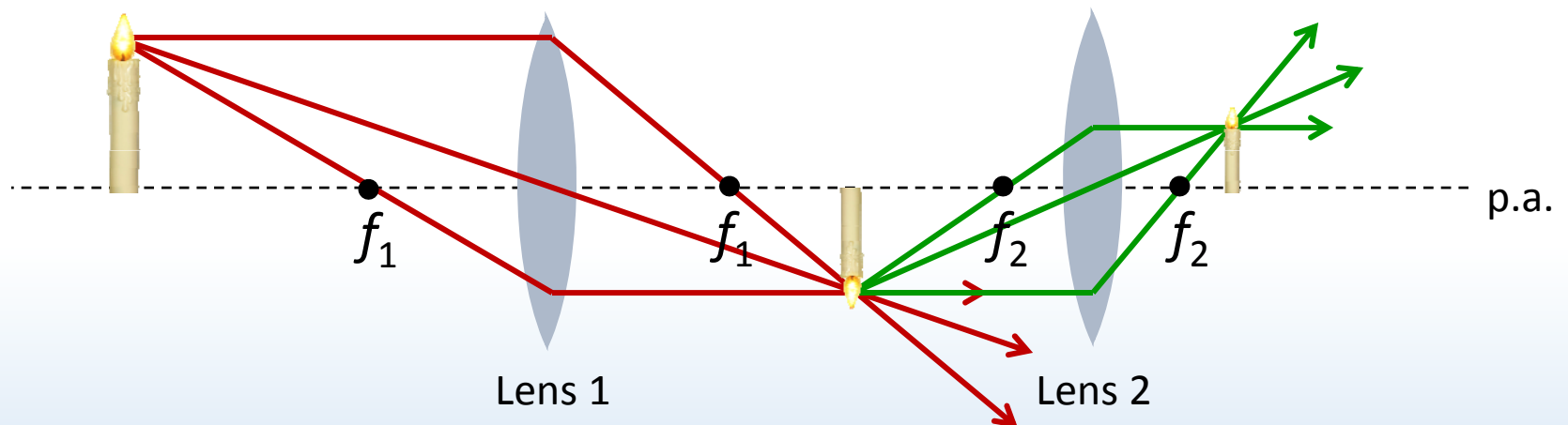
Optical instruments

# ***Today we will...***

- Learn how combinations of lenses form images  
Thin lens equation & magnification
- Learn about the compound microscope  
Eyepiece & objective  
Total magnification
- Learn about limits to resolution  
Spherical & chromatic aberrations  
Dispersion

# Checkpoint 1.1–1.2: multiple lenses

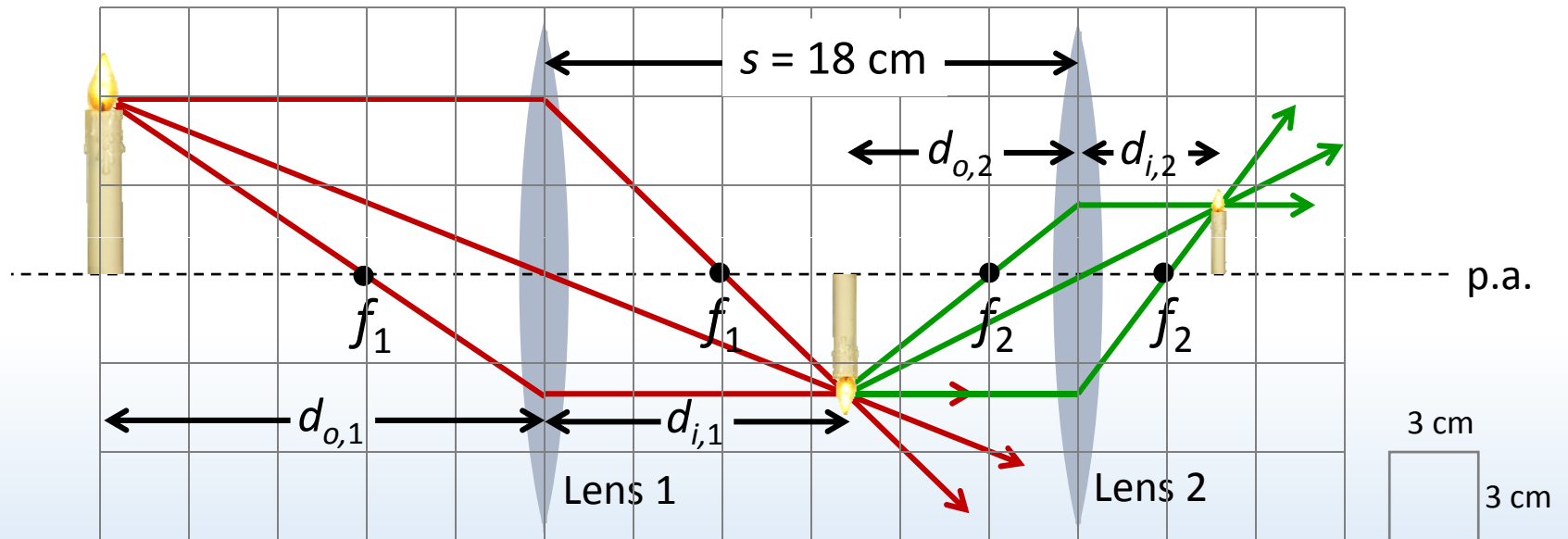
Image of first lens becomes object for second lens, etc...



DEMO

# Calculation: final image location

Determine the final image location for the 2-lens system

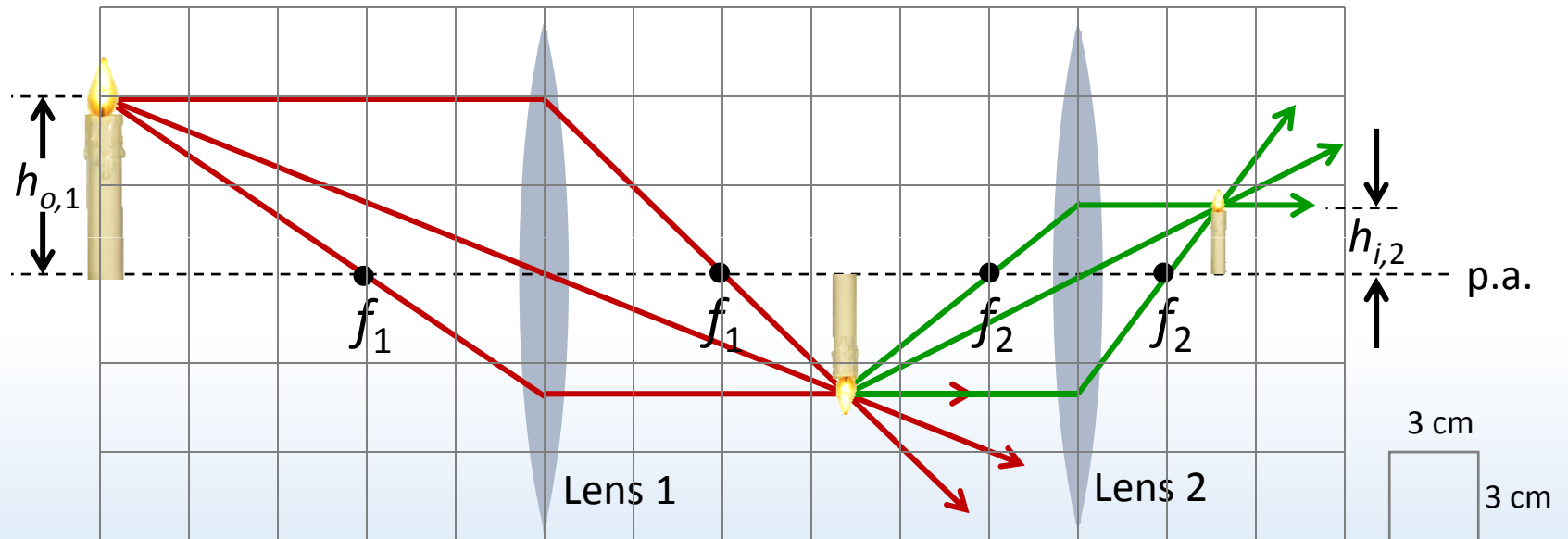


$$\frac{1}{d_{i,1}} = \frac{1}{f_1} - \frac{1}{d_{o,1}}$$

$$\frac{1}{d_{i,2}} = \frac{1}{f_2} - \frac{1}{d_{o,2}}$$

# Calculation: final magnification

Determine the final image size for the 2-lens system



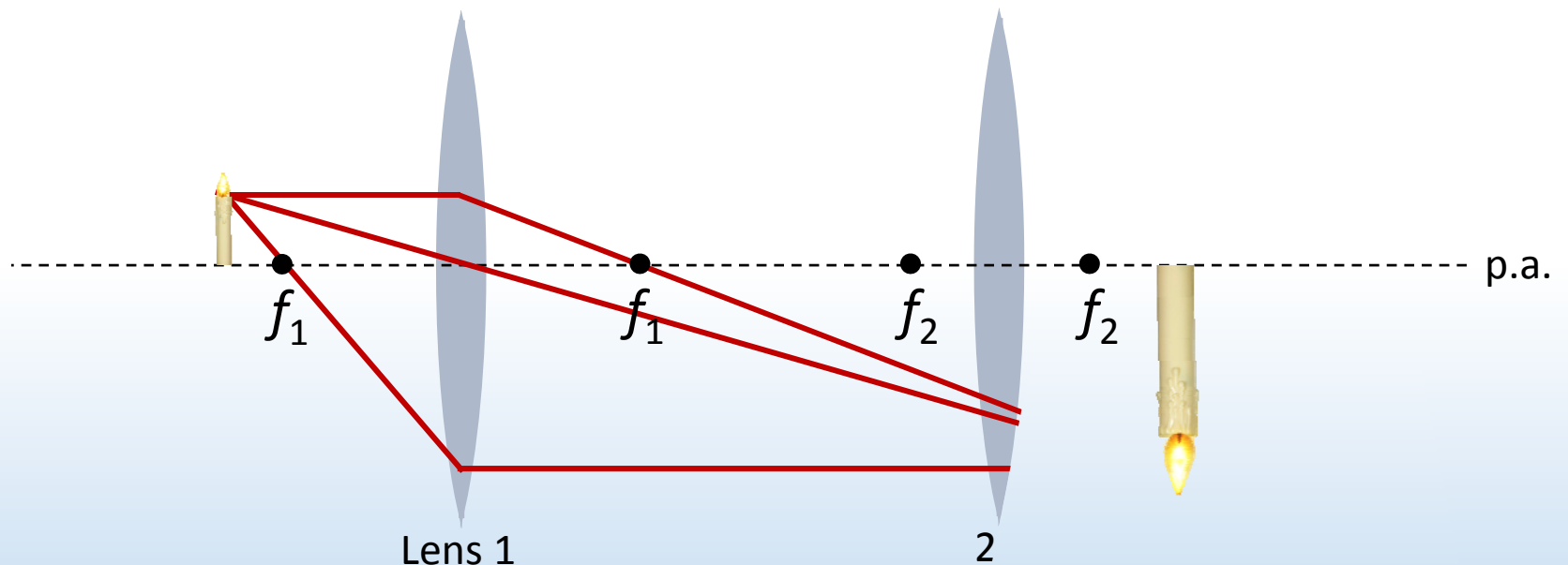
$$m_{tot} = m_1 m_2$$

$$h_{i,2} = m_{tot} h_{o,2}$$



## ACT: CheckPoint 1.3

Now, the second converging lens is placed to the left of the first lens' image.



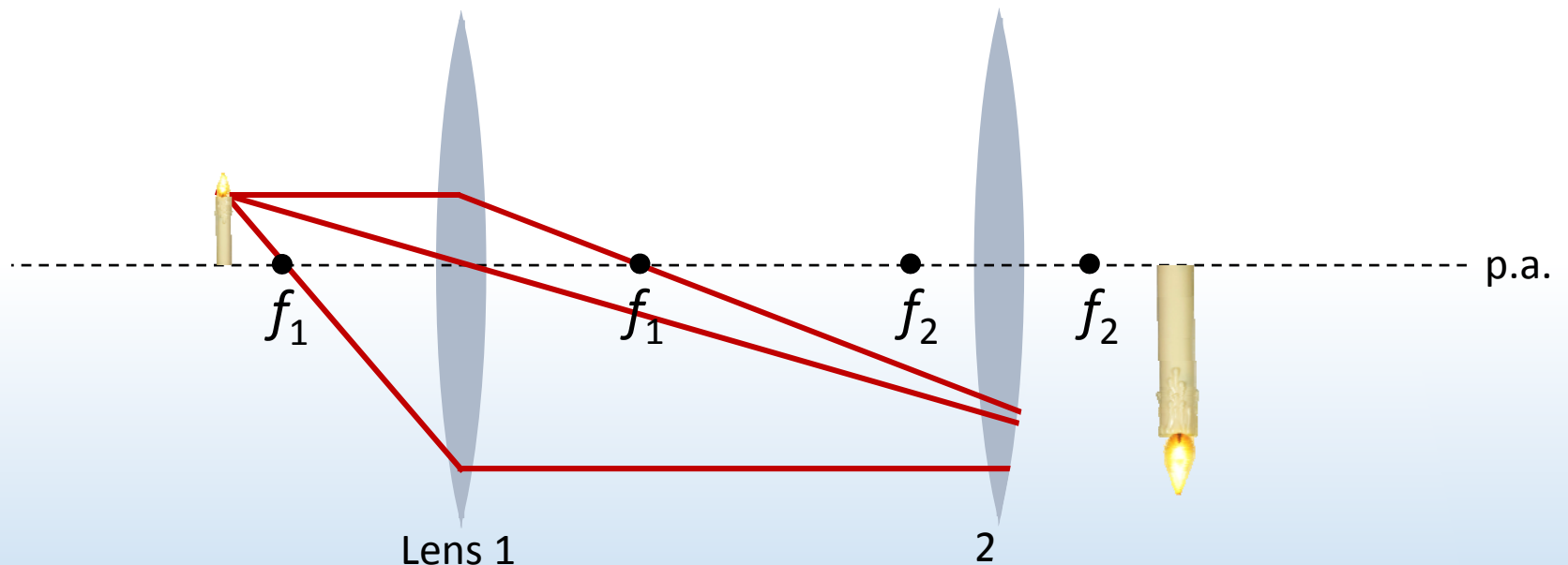
Which statement is true?

- A. Lens 2 has no object
- B. Lens 2 has a real object
- C. Lens 2 has a virtual object



## ACT: CheckPoint 1.4

Now, the second converging lens is placed to the left of the first lens' image.



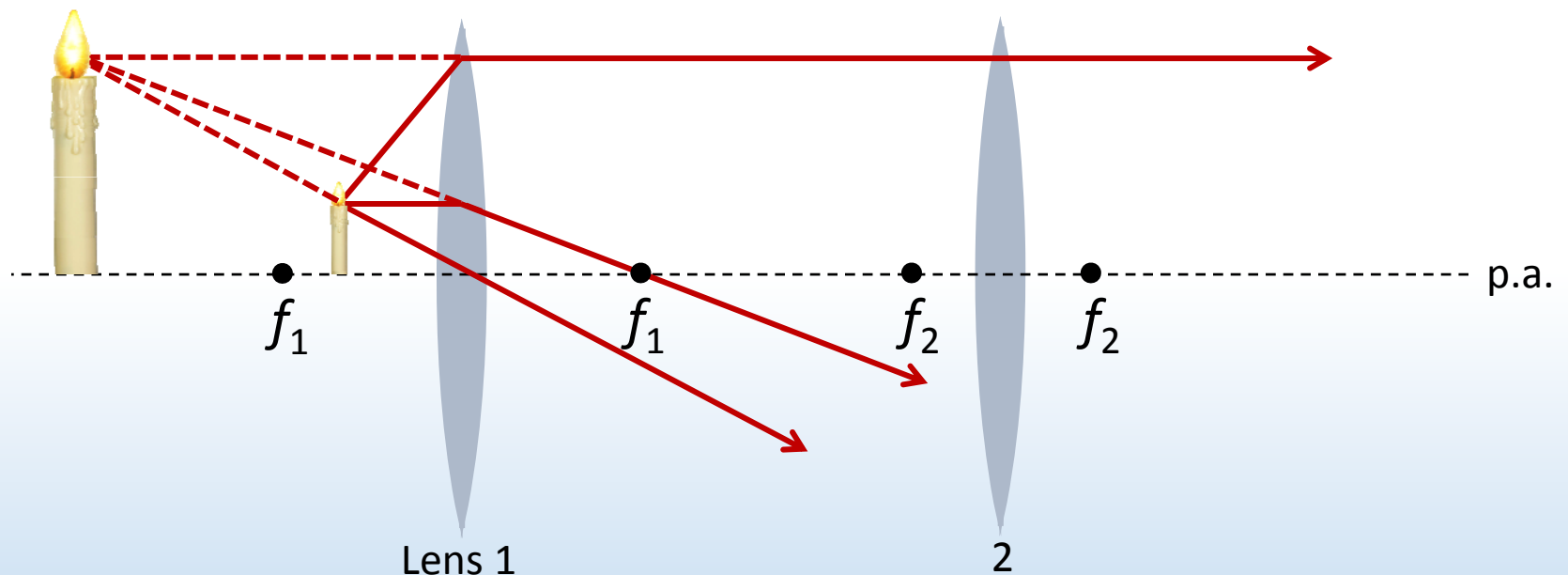
What is the image formed from lens 2?

- A. There is no image
- B. Real
- C. Virtual



# ***ACT: Multiple lenses***

A converging lens creates a virtual upright image. A second converging lens is placed after the first lens.



Which statement is true?

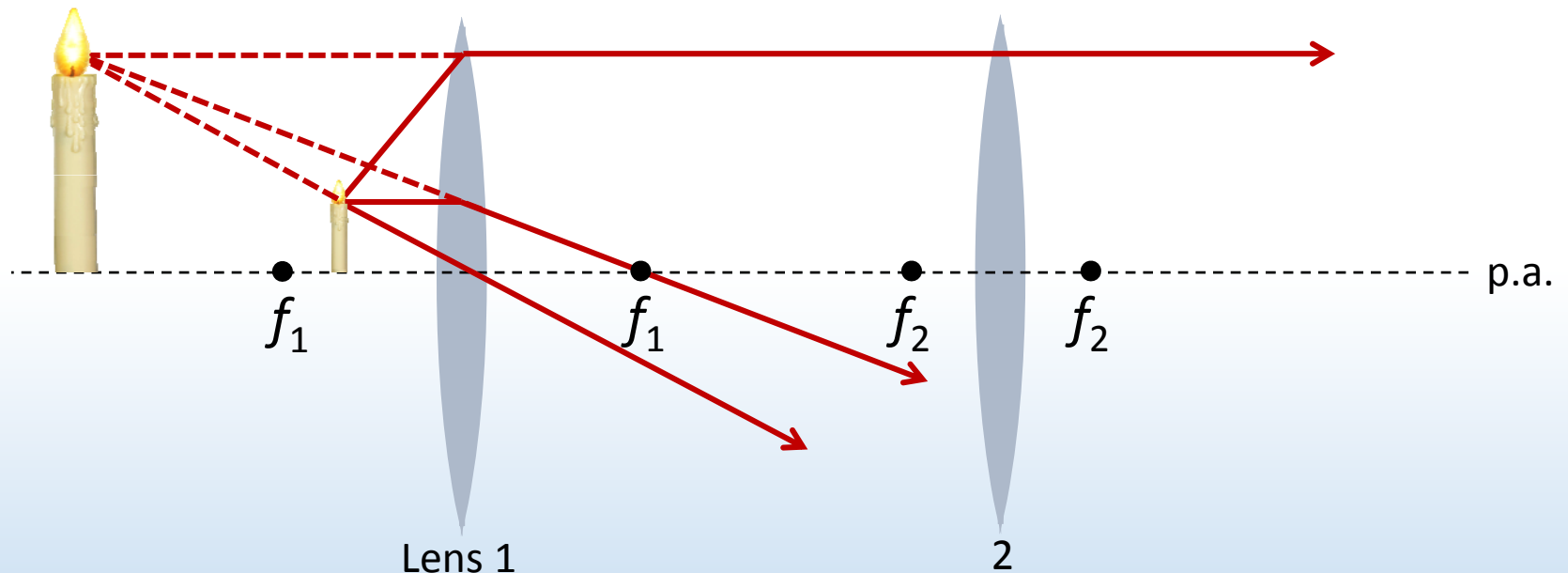
- A. Lens 2 has no object
- B. The object distance for lens 2  $> 0$
- C. The object distance for lens 2  $< 0$





# ***ACT: Multiple lenses image***

A converging lens creates a virtual upright image. A second converging lens is placed after the first lens.



The final image is

- A. Real and inverted
- B. Real and upright
- C. Virtual and upright

# ***Lens combination: summary***

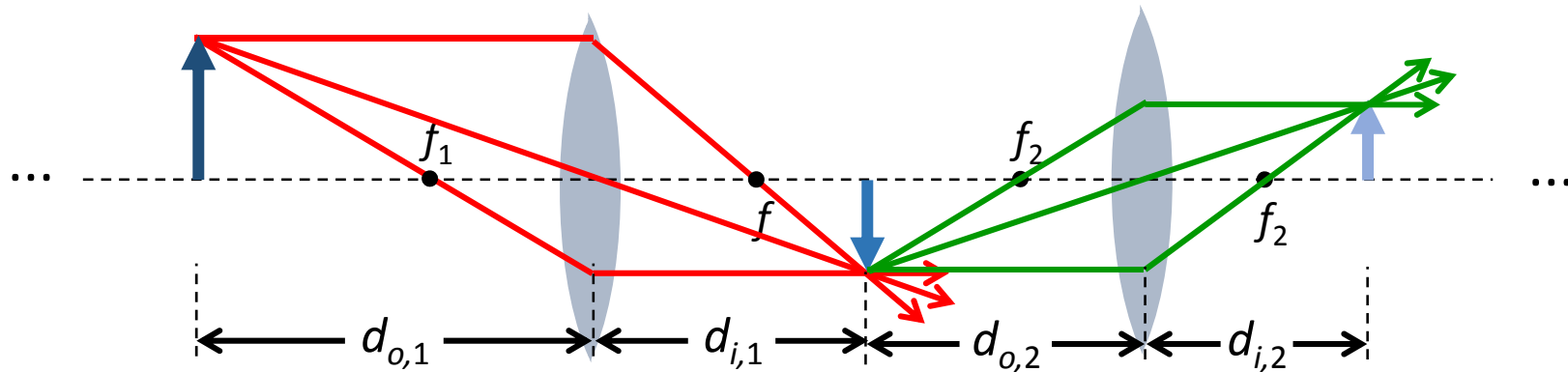


Image of first lens becomes object of second lens, ...

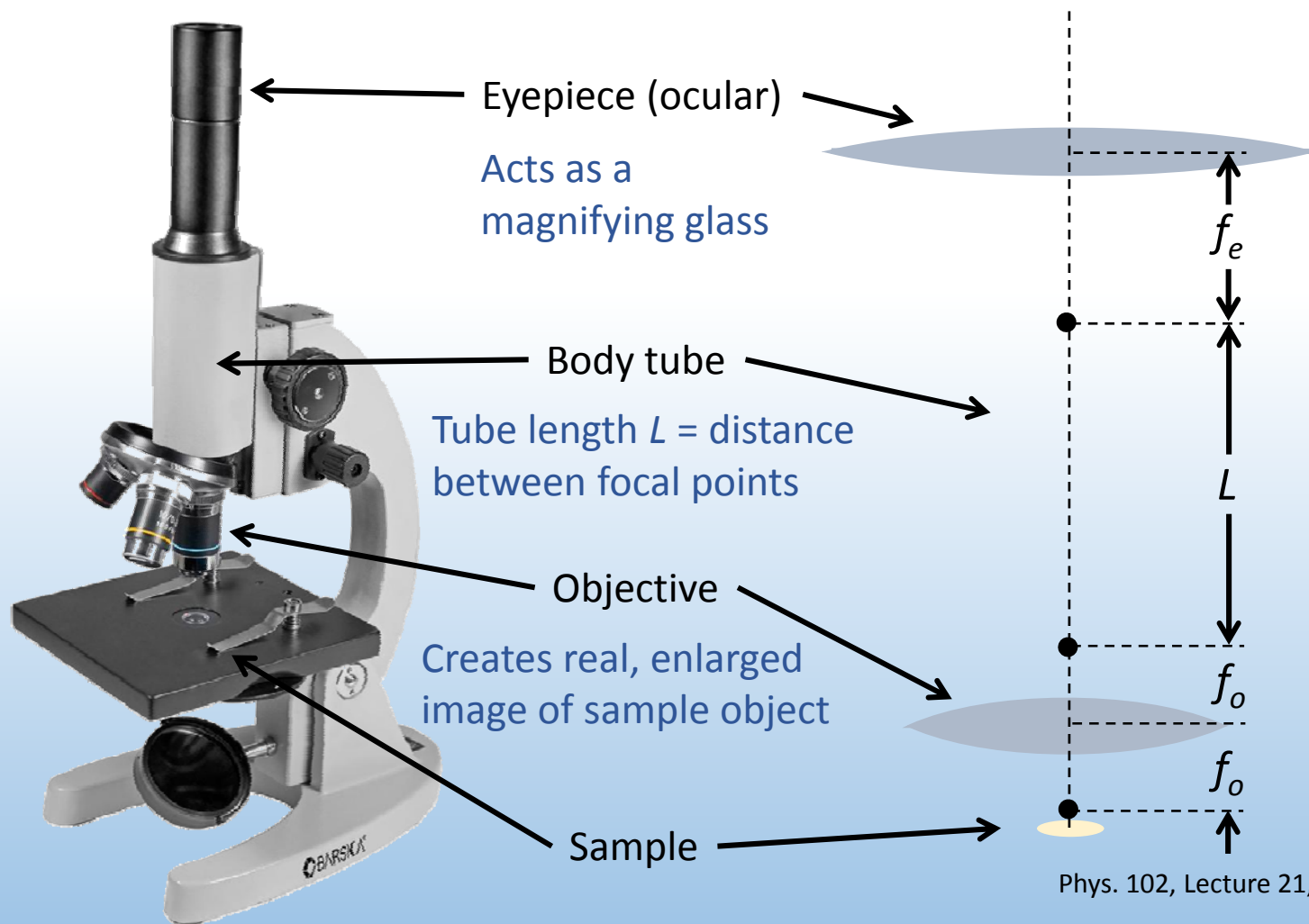
$$m_{tot} = m_1 m_2 m_3 \dots$$

- $d_o$  = distance object is from lens:
  - > 0: real object (before lens)
  - < 0: virtual object (after lens)
- $d_i$  = distance image is from lens:
  - > 0: real image (after lens)
  - < 0: virtual image (before lens)
- $f$  = focal length lens:
  - > 0: converging lens
  - < 0: diverging lens

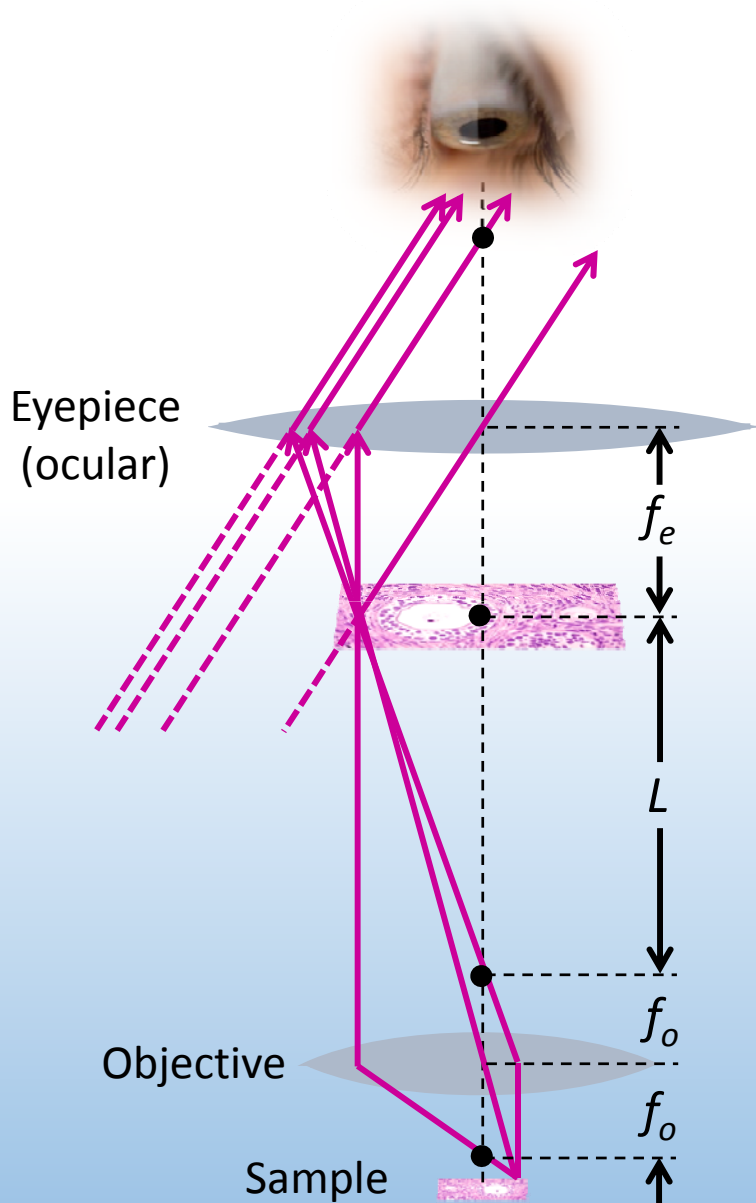
**Watch your signs!**

# Compound microscope

A compound microscope is made up of two converging lenses



# Microscope ray diagram



Total image magnification:

$$M_{tot} = M_e m_o = -\frac{d_{near}}{f_e} \frac{L}{f_o}$$

Eyepiece creates virtual, upright image at  $\infty$

$$M_e = \frac{d_{near}}{f_e} \quad \text{Recall Lect. 20}$$

Object just past objective focal pt. creates real, inverted image at eyepiece focal pt.

$$1 = \frac{d_i}{f_o} - \frac{d_o}{f_o} = \frac{L + f_o}{f_o} + m_o$$

$$m_o = -\frac{d_i}{d_o} = -\frac{L}{f_o}$$



# ***ACT: Microscope eyepiece***

The magnification written on a microscope eyepiece assumes the user has “normal” adult vision



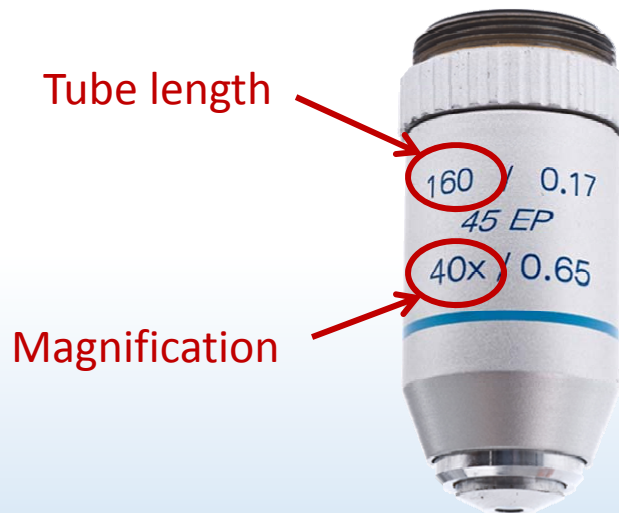
What is the focal length of a 10× eyepiece?

- A.  $f_e = 2.5 \text{ cm}$
- B.  $f_e = 10 \text{ cm}$
- C.  $f_e = 25 \text{ cm}$



# ***ACT: Microscope objective***

A standard biological microscope has a 160 mm tube length and is equipped with a 40× objective

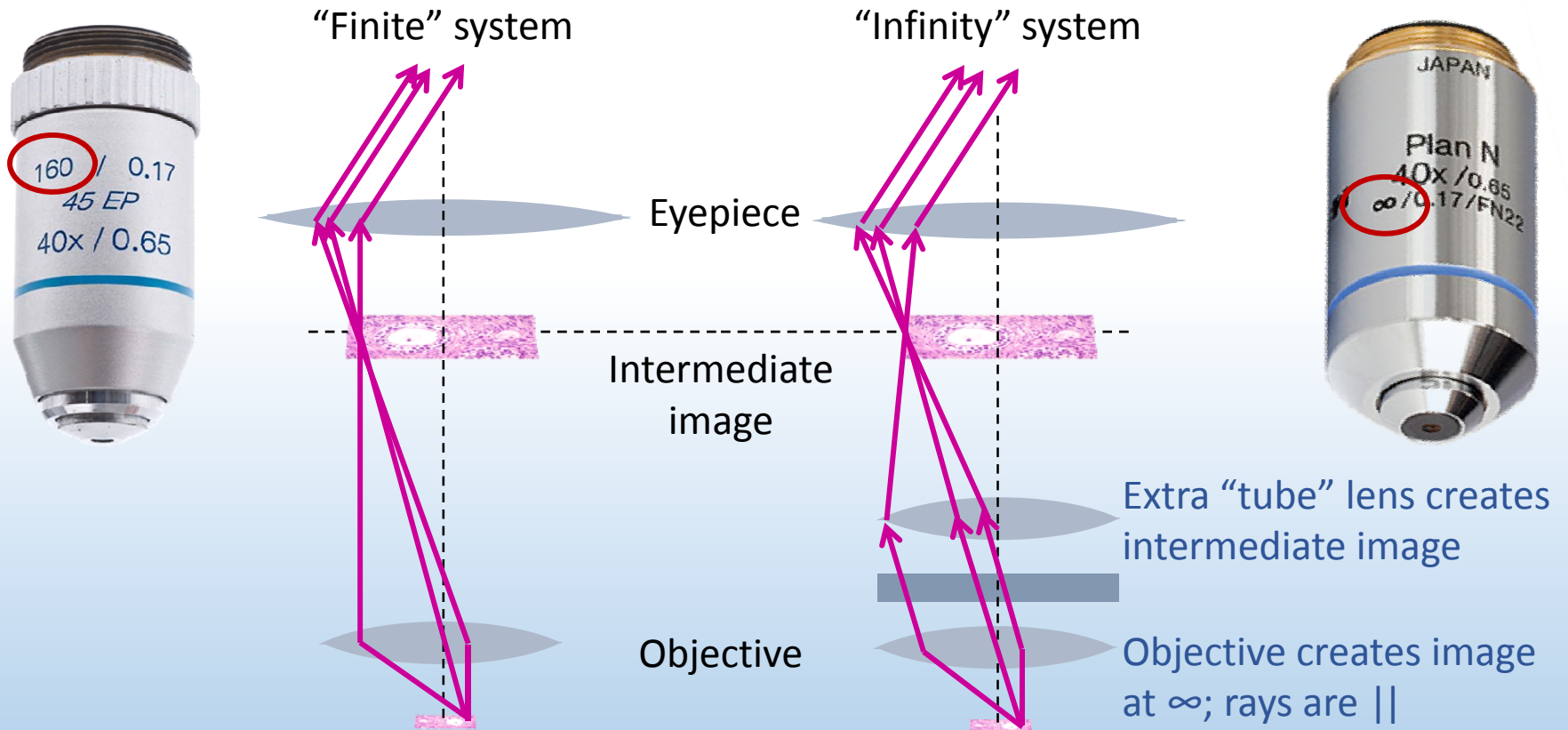


What is the focal length of the objective?

- A.  $f_o = 4 \text{ mm}$
- B.  $f_o = 8 \text{ mm}$
- C.  $f_o = 16 \text{ mm}$

# Modern microscope objectives

Most modern objectives are “infinity corrected”



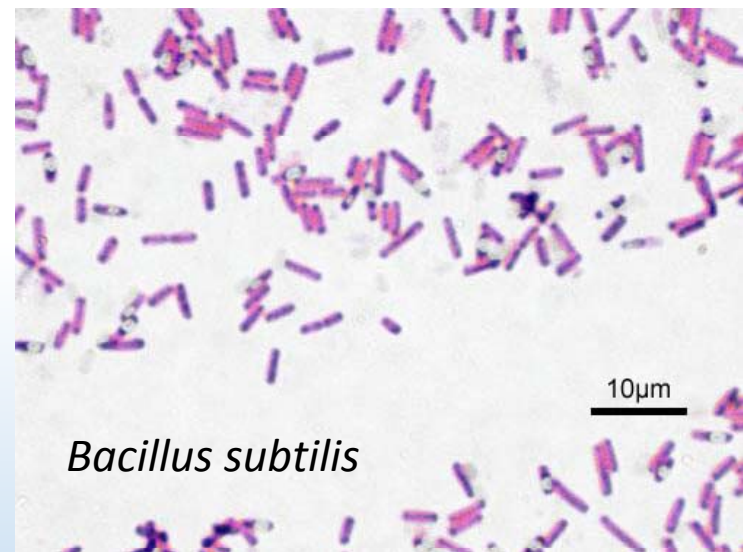
# Calculation: Angular size

A microscope has a 10× eyepiece and a 60× objective. How much larger does the microscope image appear to our eyes?

$$M_{tot} = M_e m_o$$

At a near pt. of 25 cm, a 2-μm bacterium has angular size to an unaided eye of:

In the microscope the angular size is:

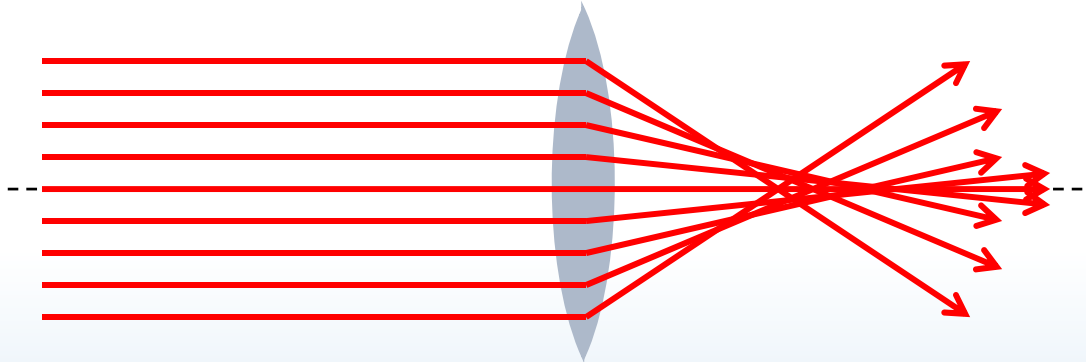




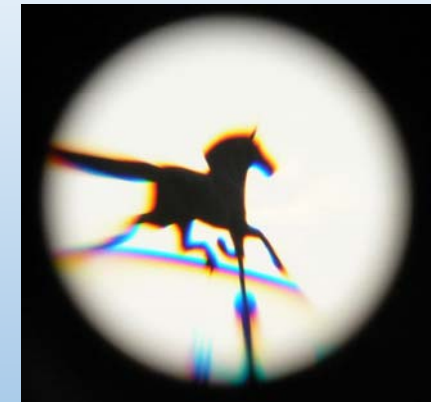
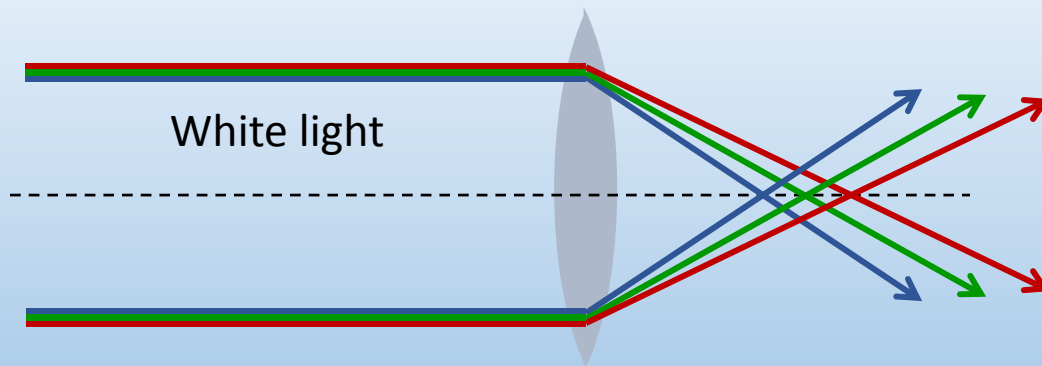
# ***Aberrations***

Aberrations are imperfections relative to ideal lens

Spherical: rays hitting lens at different points focus differently



Chromatic: rays of different color focus differently



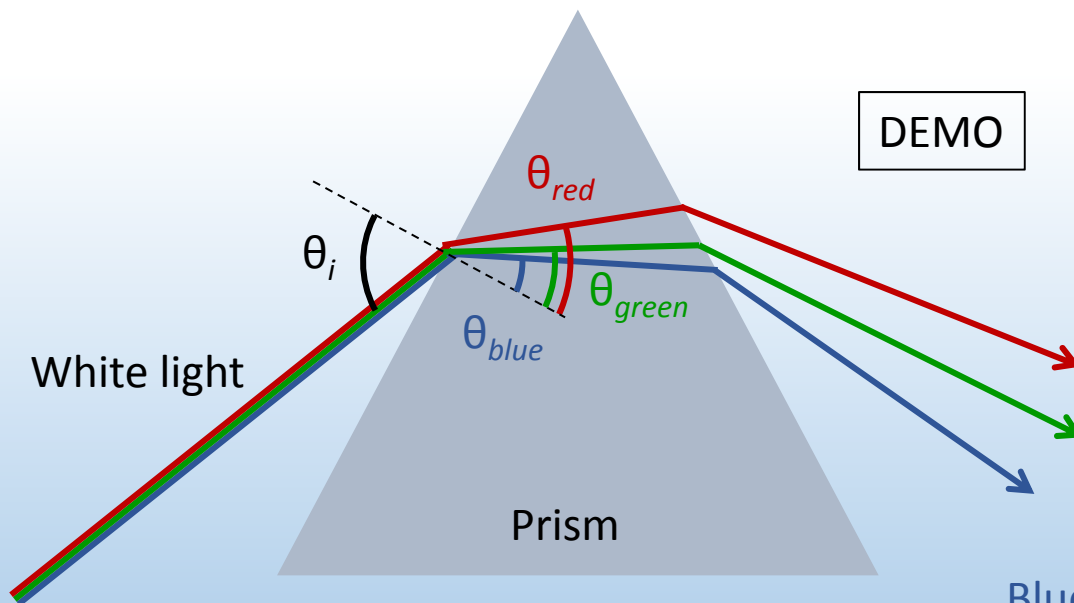
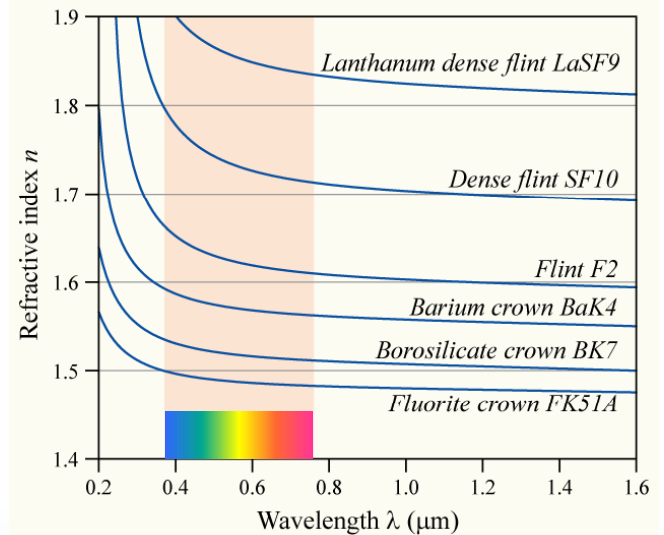
Where do chromatic aberrations come from?

# Dispersion

The index of refraction  $n$  depends on  $\lambda$

In glass,  $n_{\text{blue}} > n_{\text{green}} > n_{\text{red}}$

In prism,  $\theta_{\text{blue}} < \theta_{\text{green}} < \theta_{\text{red}}$

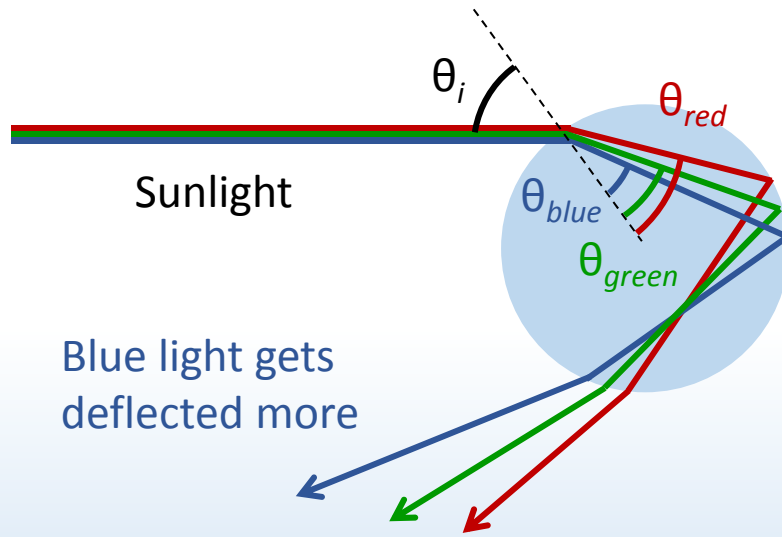


Blue light gets deflected more

$$n_i \sin \theta_i = n_{\text{blue}} \sin \theta_{\text{blue}} = n_{\text{green}} \sin \theta_{\text{green}} = n_{\text{red}} \sin \theta_{\text{red}}$$

# CheckPoint 2.1: Rainbows

Dispersion in water droplets create rainbows



In water,  $n_{blue} > n_{green} > n_{red}$

# *Double rainbow*

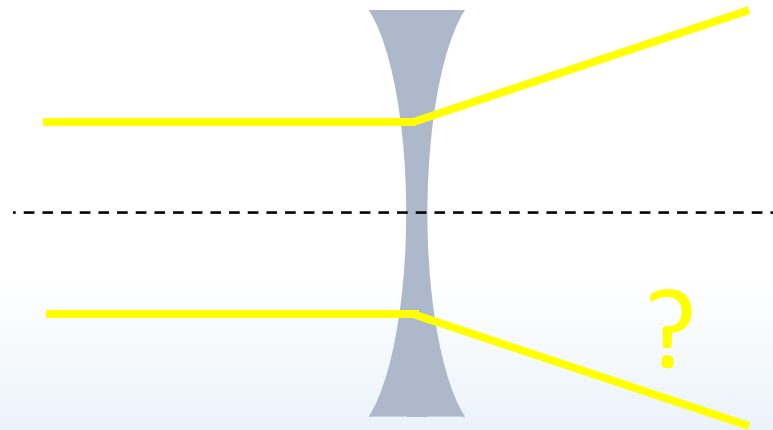


[Double rainbow](#)

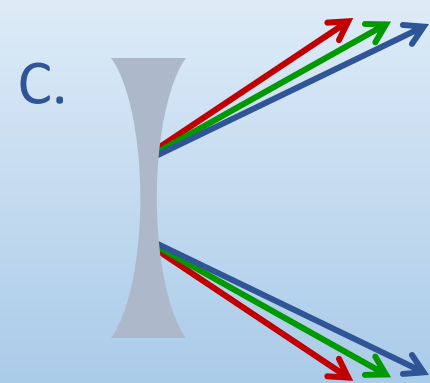
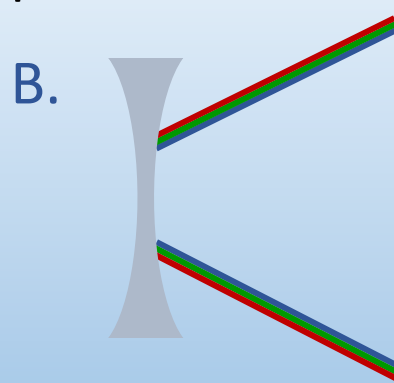
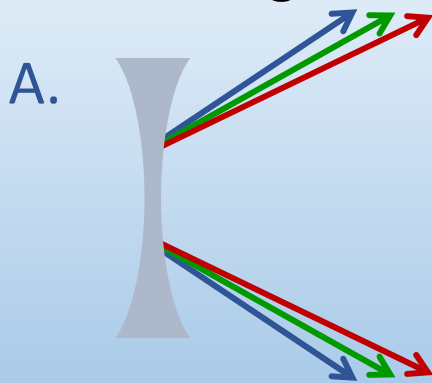


# ACT: Dispersion

A diverging lens made of flint glass has  $n_{red} = 1.57$ ,  $n_{blue} = 1.59$ . Parallel rays of white light are incident on the lens.



Which diagram best represents how light is transmitted?



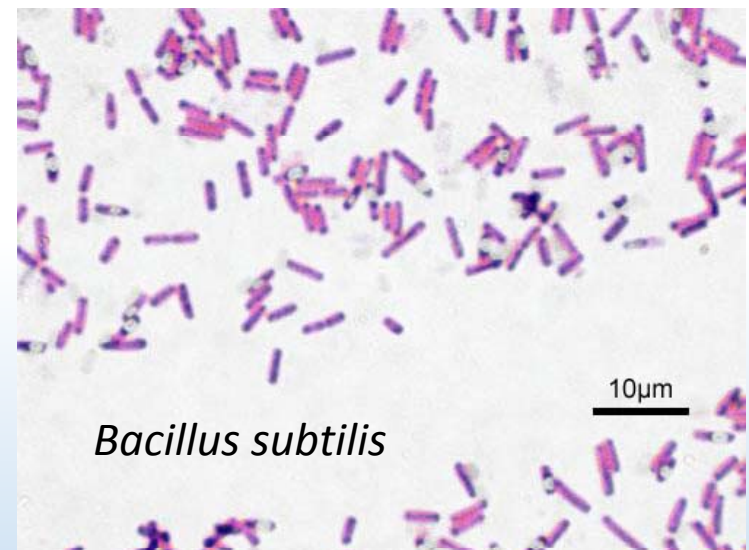
# *Ultimate limit of resolution*

One can play clever tricks with combinations of lenses to compensate for spherical and chromatic aberrations

Ultimately, even with *ideal* lenses resolution of light microscope is limited to  $\sim\lambda$  of light ( $\sim 500\text{ nm}$ )

We won't understand why using *ray picture* of light; we have to treat light as a *wave* again

Next two lectures!



Ray optics works for objects  $\gg \lambda$

# *Summary of today's lecture*

- Combinations of lenses:

Image of first lens is object of second lens... **Watch signs!**

- The compound microscope

Objective forms real image at focal pt. of eyepiece

Eyepiece forms virtual image at  $\infty$

- Limits to resolution

Spherical & chromatic aberrations

Dispersion

*Diffraction limit* – next week!