

# Physics 102: Lecture 09

## Currents and Magnetism

- Reminder: Exam 1 next Monday
- 5:15pm conflict: sign up in gradebook
- Be sure to bring your ID, a calculator, #2 pencil, and go to the correct room
- Extra office hours Friday this week
- Video solutions available in byteshelf as unit 8

# Summary of Today

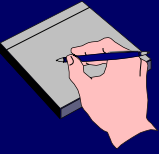
- Magnetic forces on currents and torques on current loops



- Magnetic fields created by currents
  - long straight wire
  - solenoid

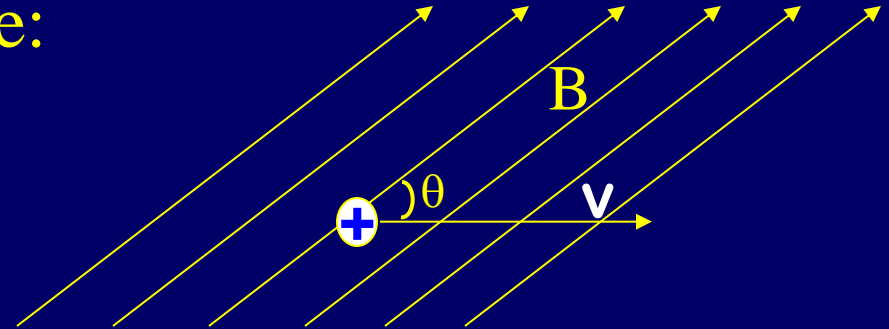


# Force of magnetic field on Current



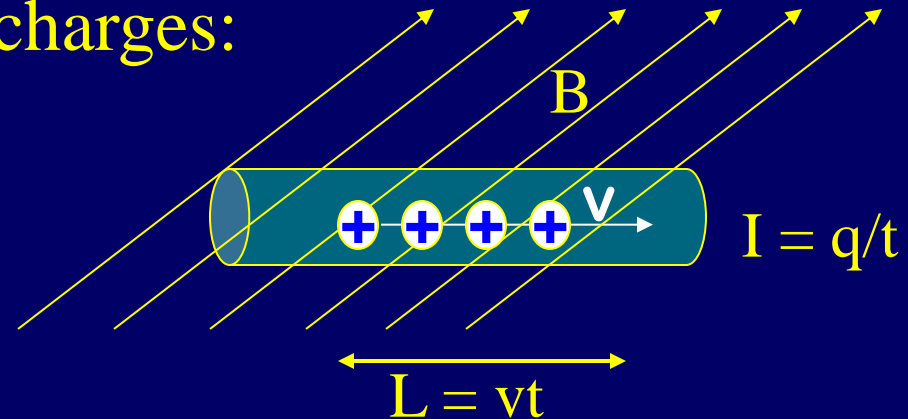
- Force on 1 moving charge:

- $F = q v B \sin(\theta)$
- Out of the page (RHR)



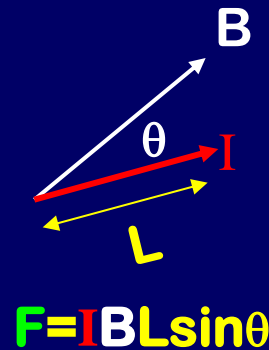
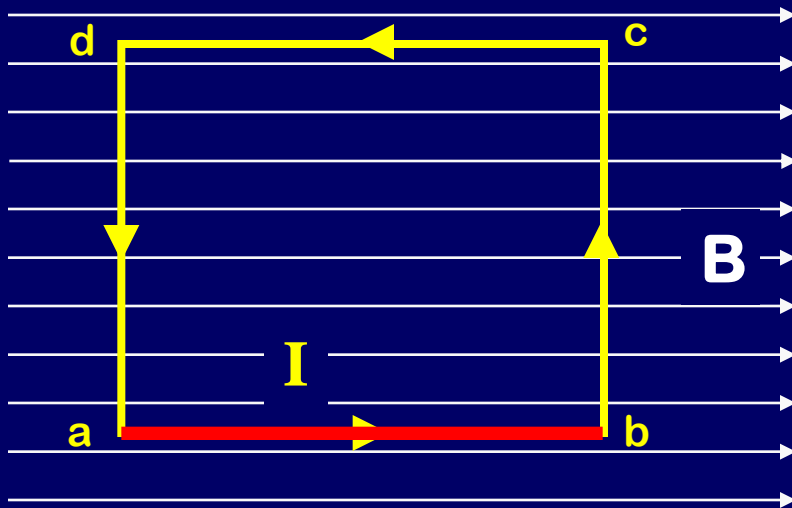
- Force on many moving charges:

- $F = q v B \sin(\theta)$   
 $= (q/t) (vt) B \sin(\theta)$   
 $= I L B \sin(\theta)$
- Out of the page!



# CheckPoint 1.1

A rectangular loop of wire is carrying current as shown. There is a uniform magnetic field parallel to the sides a-b and c-d.



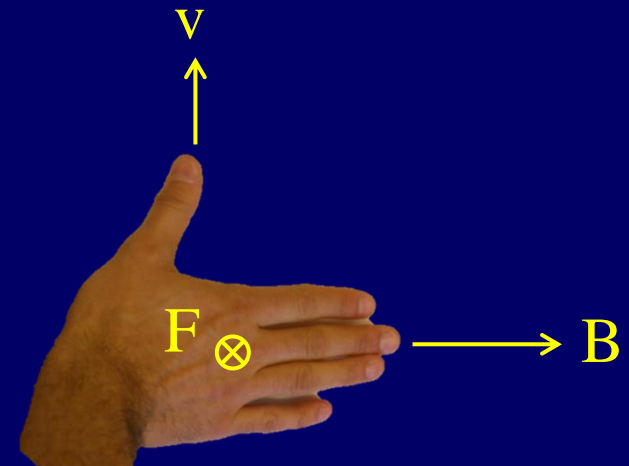
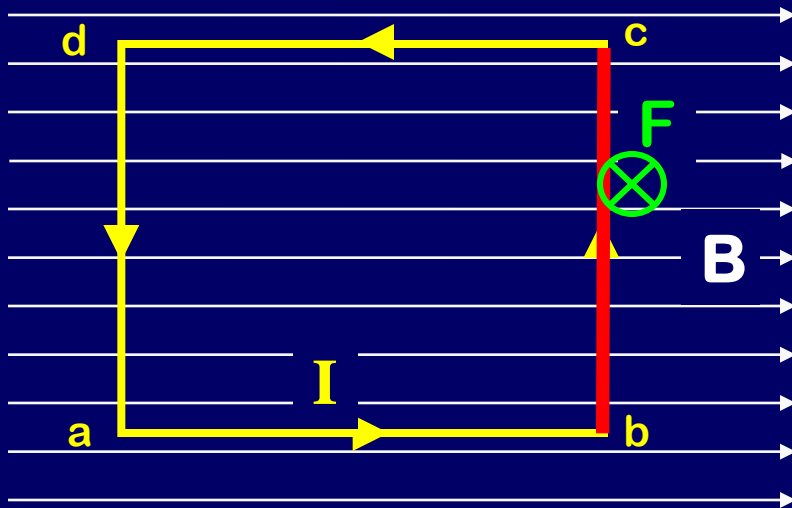
Here  $\theta = 0$

What is the direction of the force on section a-b of the wire?

- A) force is zero 62%
- B) out of the page 22%
- C) into the page 16%

# Checkpoint 1.2

A rectangular loop of wire is carrying current as shown. There is a uniform magnetic field parallel to the sides a-b and c-d.

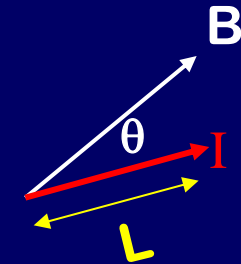
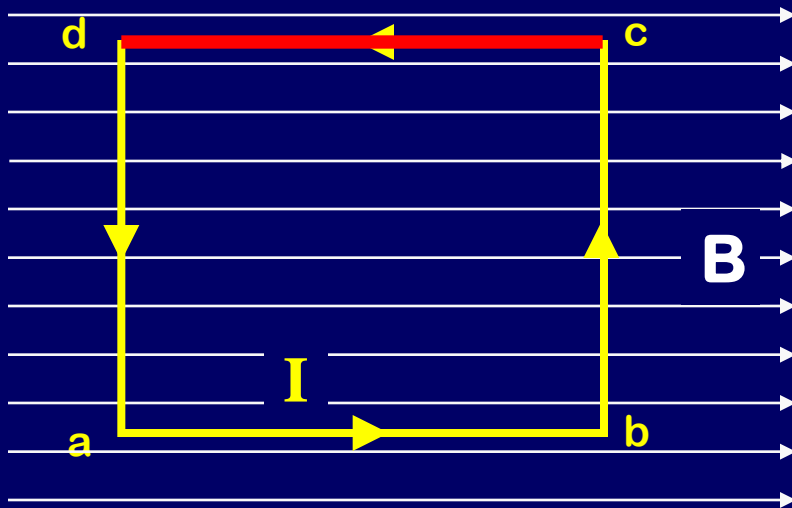


What is the direction of the force on section b-c of the wire?

- A) force is zero 14%
- B) out of the page 30%
- C) into the page 56%**

# Force on loop

A rectangular loop of wire is carrying current as shown. There is a uniform magnetic field parallel to the sides a-b and c-d.



$$F = IBL \sin \theta$$

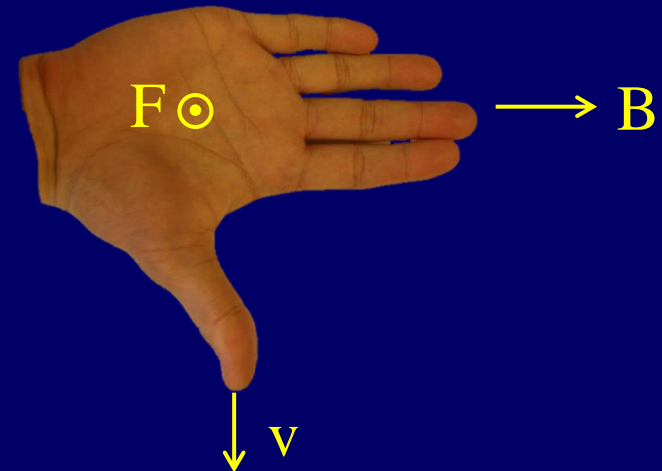
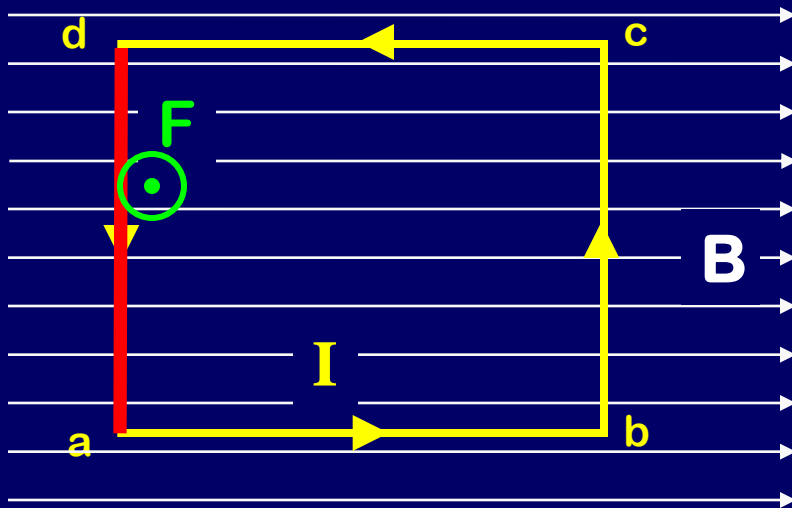
Here  $\theta = 180^\circ$

Force on section c-d is zero! Same as a-b



# ACT: Force on loop (cont'd)

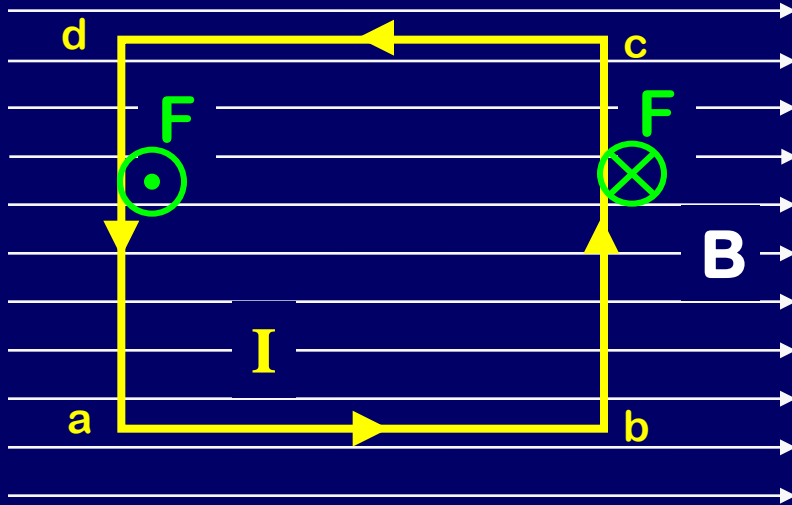
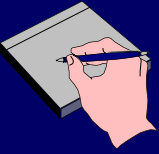
A rectangular loop of wire is carrying current as shown. There is a uniform magnetic field parallel to the sides a-b and c-d.



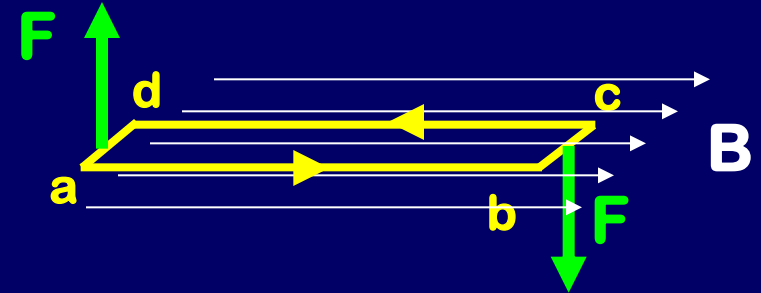
What is the direction of the force on section d-a of the wire?

- A) force is zero
- ☒ B) out of the page
- C) into the page

# Torque on Current Loop in magnetic field



Look from here



The loop will **spin in place!**

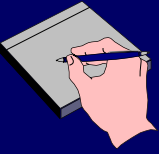
CheckPoints 1.3, 1.4:

Net force on loop is **zero**.

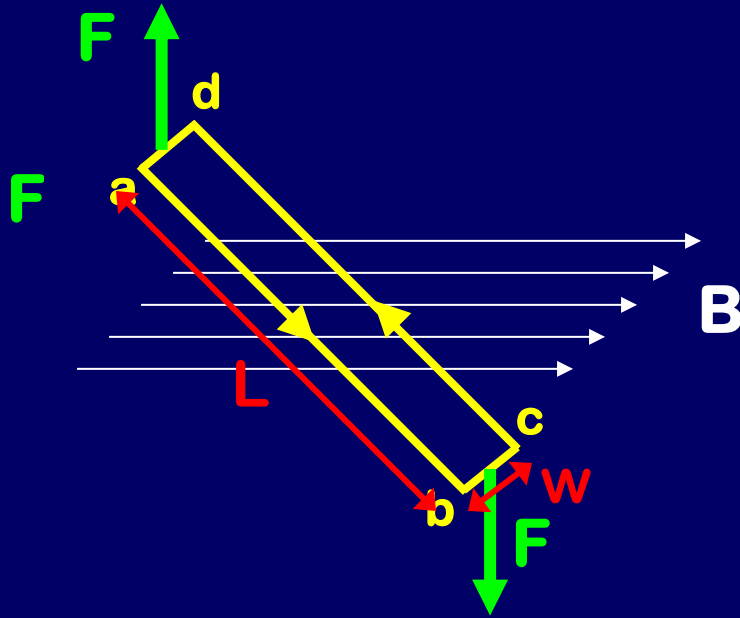
But the net torque is **not**!



# Torque on Current Loop

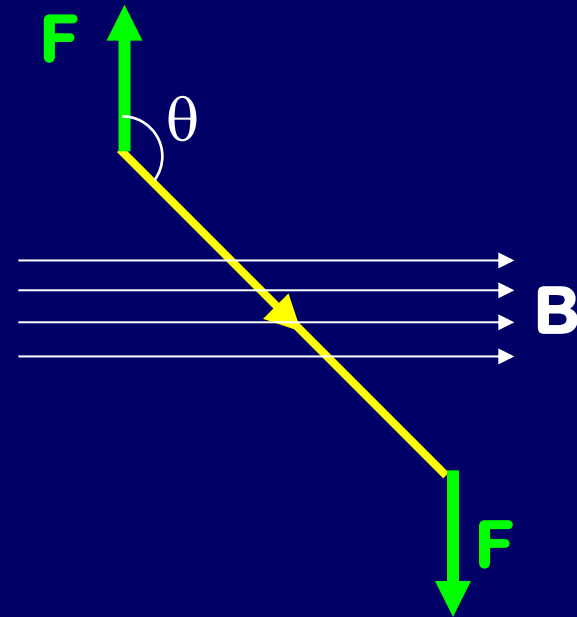


The loop will spin in place!



Recall from Phys 101:

$$\tau = F r \sin \theta$$



Force on sections b-c and a-d:  $F = IBw$

Torque on loop is  $\tau = 2 (L/2) F \sin(\theta) = I \underbrace{Lw}_{Lw = A!} B \sin(\theta)$

Torque is:  $\tau = IAB \sin \theta$



# ACT: Torque on Current Loop

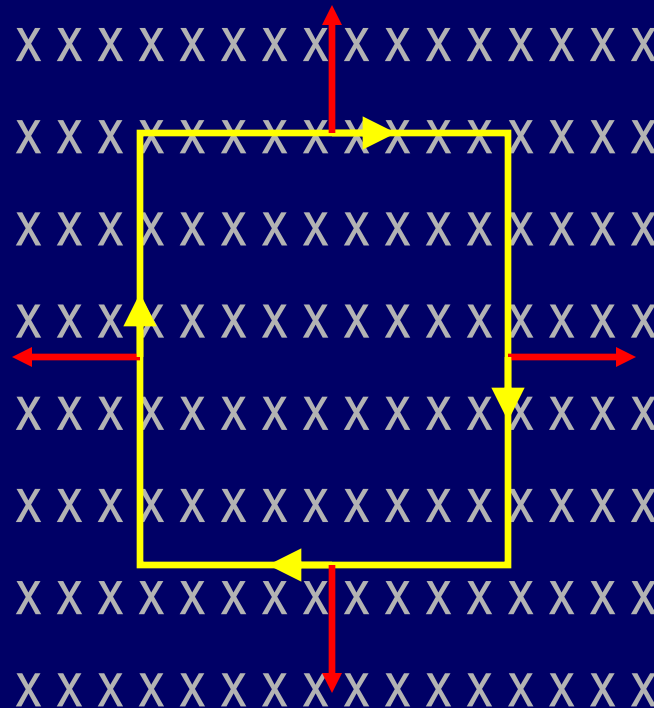
What is the torque on the loop below?

A.  $\tau < IAB$

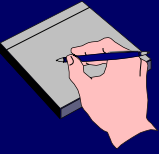
B.  $\tau = IAB$

C.  $\tau > IAB$

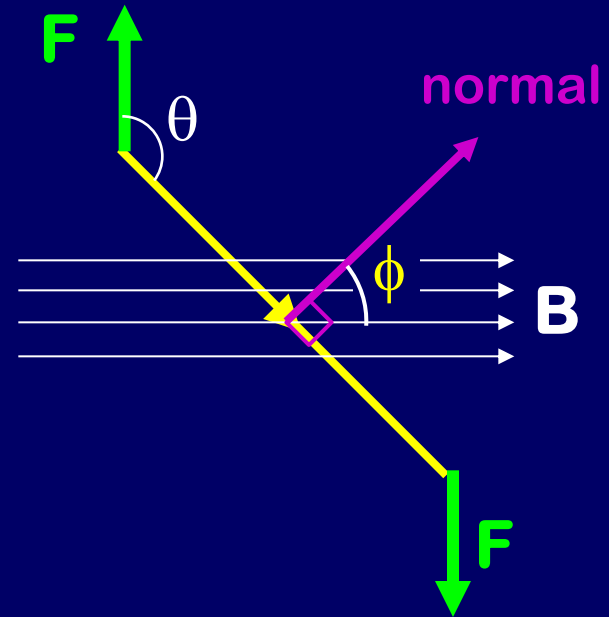
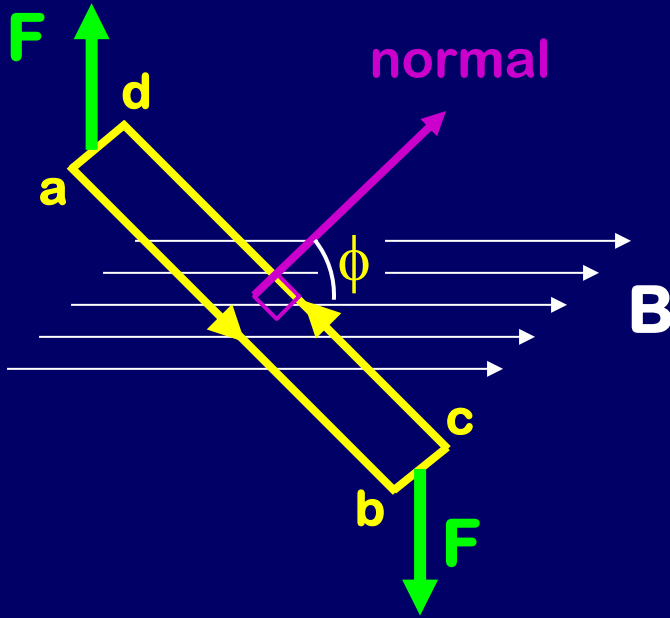
$$\tau = 0$$



# Torque on Current Loop



It is useful to define normal vector  $\perp$  to loop



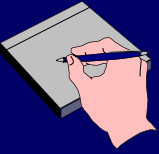
$$\phi = 180 - \theta$$

Torque is:  $\tau = IAB \sin \theta = IAB \sin \varphi$

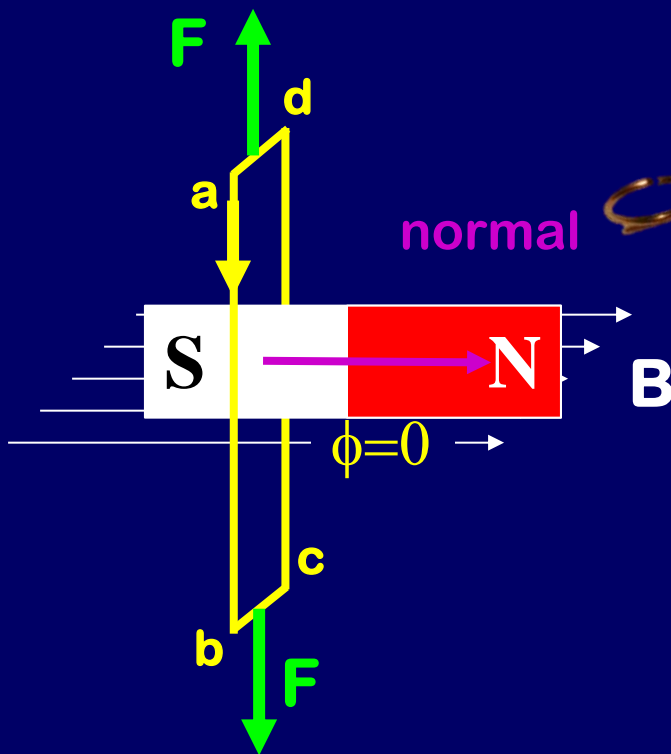
If there are N loops:  $\tau = NIAB \sin \varphi$

Even if loop is not rectangular, as long as it is flat

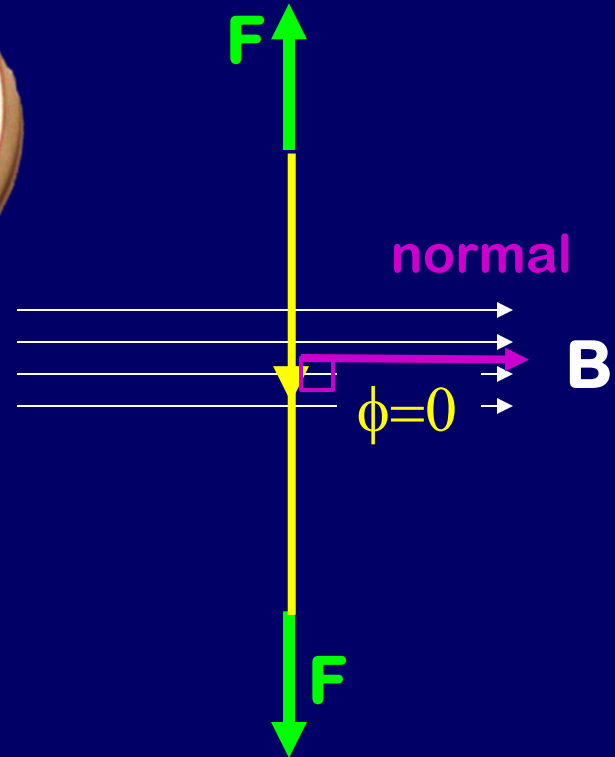
# Torque on Current Loop



It is useful to define normal vector  $\perp$  to loop



$$\phi = 180 - \theta$$



Torque is:  $\tau = IAB \sin \theta = IAB \sin \varphi$

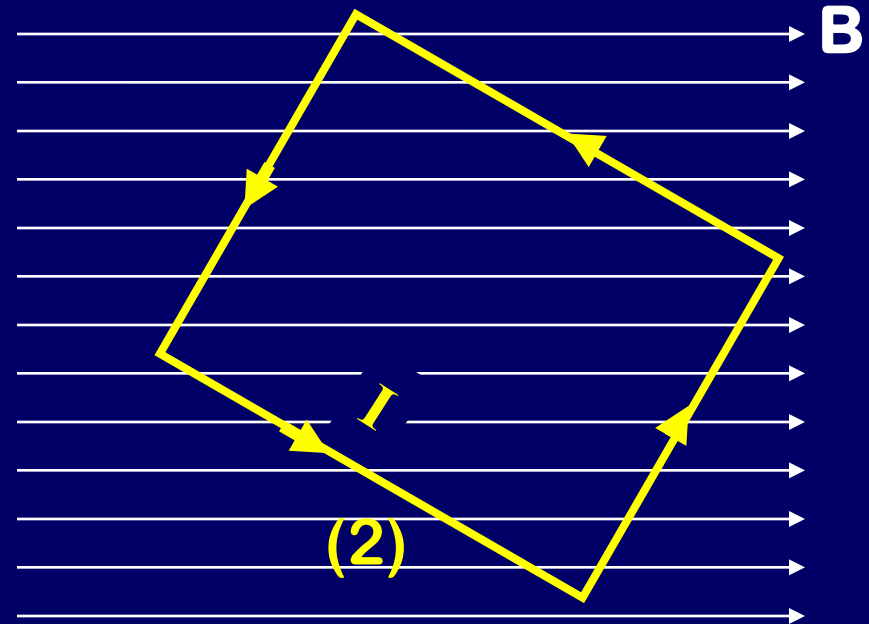
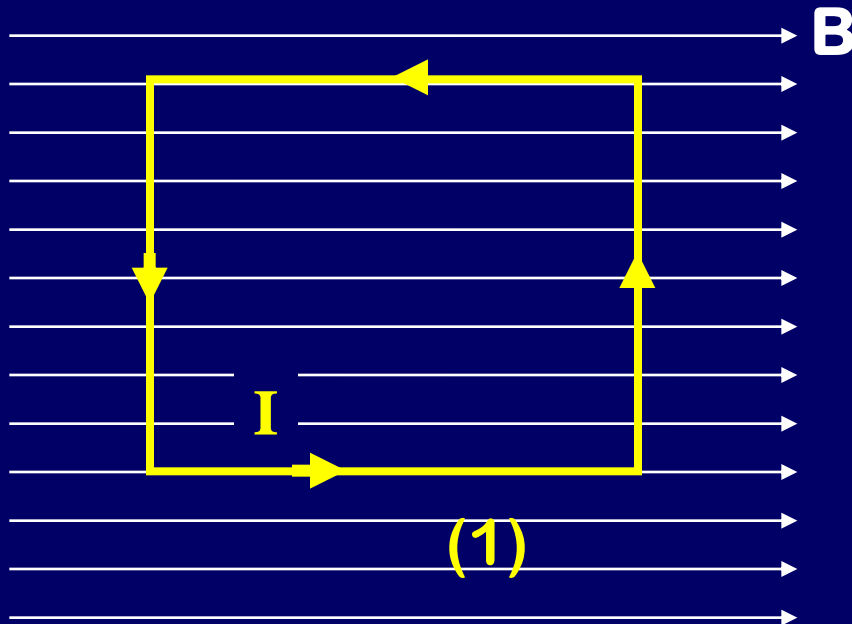
If there are N loops:  $\tau = NIAB \sin \varphi$

Even if loop is not rectangular, as long as it is flat

Note torque will align  
normal parallel to B  
like a magnetic dipole!



# ACT: Torque



Compare the torque on loop 1 and 2 which have identical area, and current.

A)  $\tau_1 > \tau_2$     **B)  $\tau_1 = \tau_2$**     C)  $\tau_1 < \tau_2$

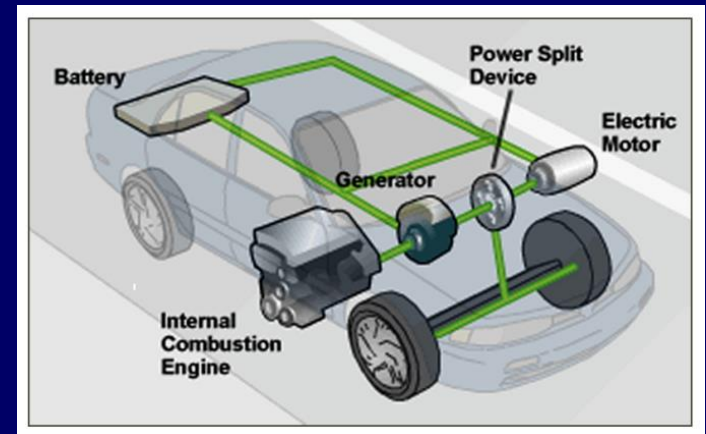
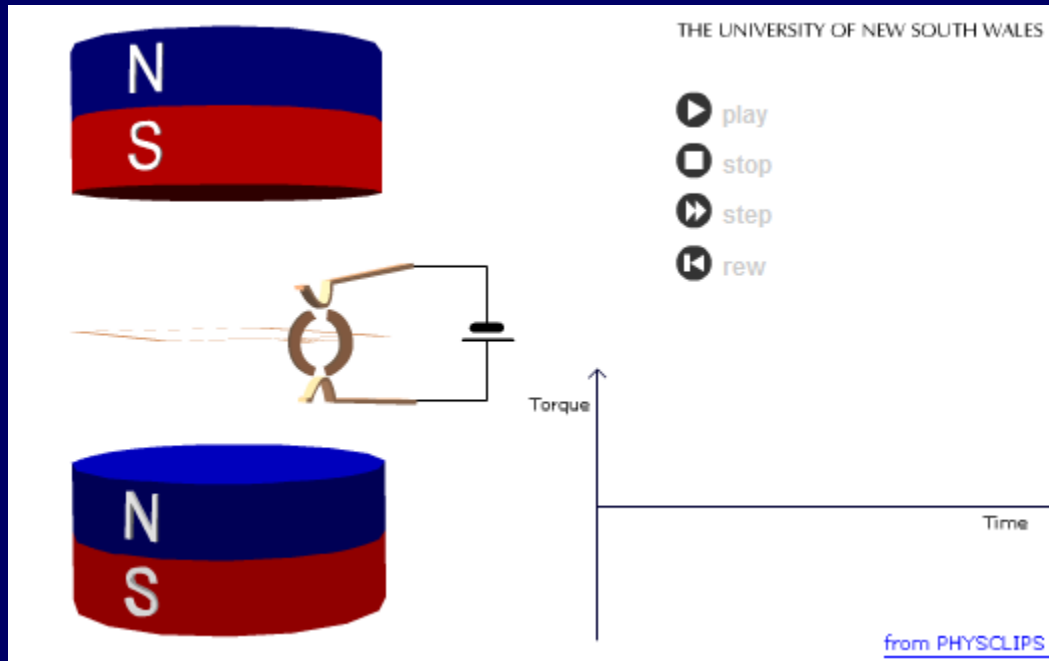
$$\tau = I A B \sin(\phi)$$

Normal vector points out of page for both!

$$\phi = 90$$

# Motors

DC motors use a clever arrangement of current carrying coils and permanent magnets to turn a shaft:



# Currents *create* magnetic fields

- Straight wire carrying current  $I$  generates a field  $B$  at a distance  $r$ :

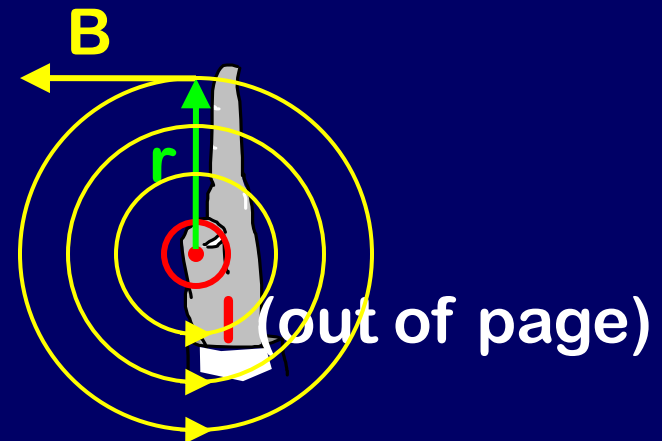
$$B = \frac{\mu_0 I}{2\pi r}$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ Tm/A}$$

“Permeability of free space”  
(similar to  $\epsilon_0$  for electricity)

- “Right-hand rule 2”:

- Thumb of right hand along  $I$
- Fingers of right hand along  $r$
- Out-of-palm points along  $B$



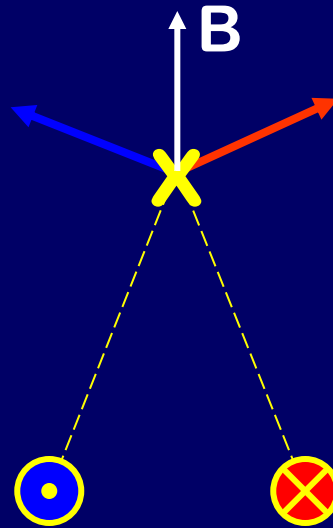
**B field circles wire**

**Note: there are different versions of RHR**



# ACT: Adding Magnetic Fields

Two long wires carry opposite current (same magnitude)



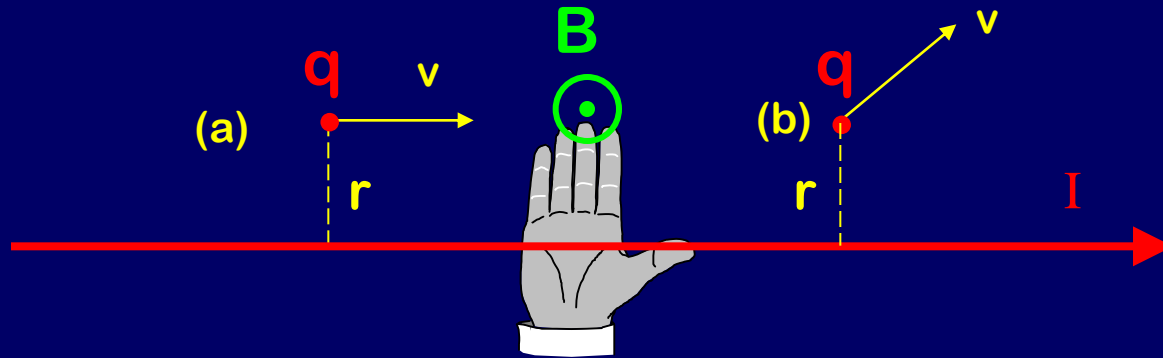
What is the direction of the magnetic field above, and midway between the two wires carrying current – at the point marked “X”?

- 1) Left   2) Right   3) Up   4) Down   5) Zero



# ACT/Checkpoint 2.1-a

A long straight wire is carrying current from left to right. Near the wire is a charge  $q$  with velocity  $v$

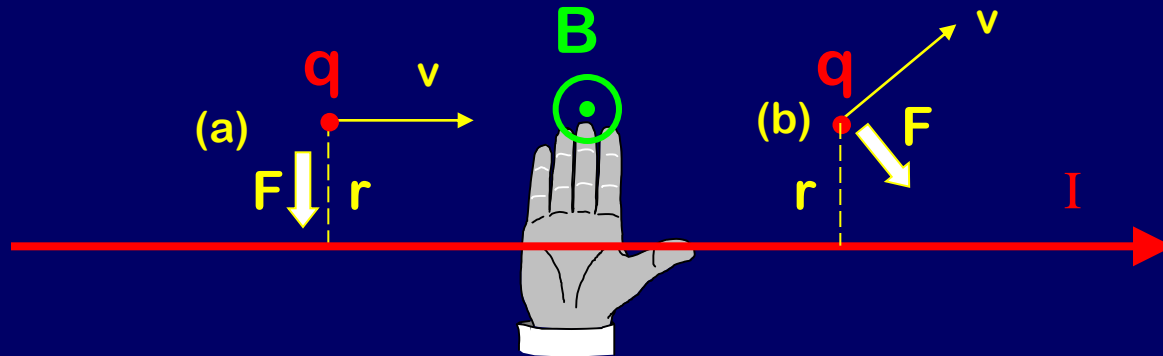


What is direction of magnetic field above wire

- a) Up
- b) Down
- c) Right
- d) Left
- e) Out of page

# ACT/Checkpoint 2.1

A long straight wire is carrying current from left to right. Near the wire is a charge  $q$  with velocity  $v$



Compare magnitude of magnetic force on  $q$  at (a) vs. (b)

a) has the larger force 29%

b) has the larger force 49%

c) force is the same for (a) and (b) 21%

$$\text{Same } B = \frac{\mu_0 I}{2\pi r}$$

$$\text{Same } F = qvB \sin \theta$$
$$\theta = 90 \text{ for (a) and (b)!}$$

Same magnitude  
Different directions

# Solenoids

Magnitude

- A solenoid consists of  $N$  loops of wire

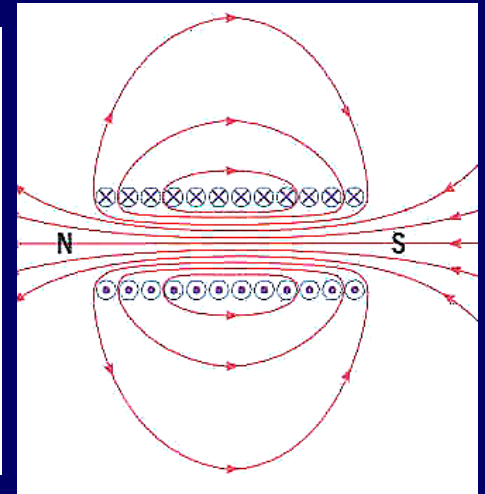
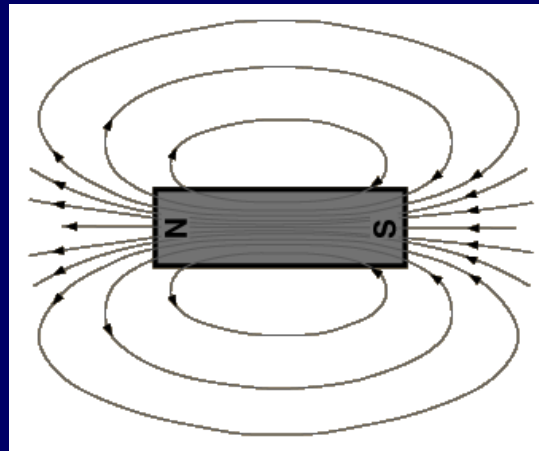
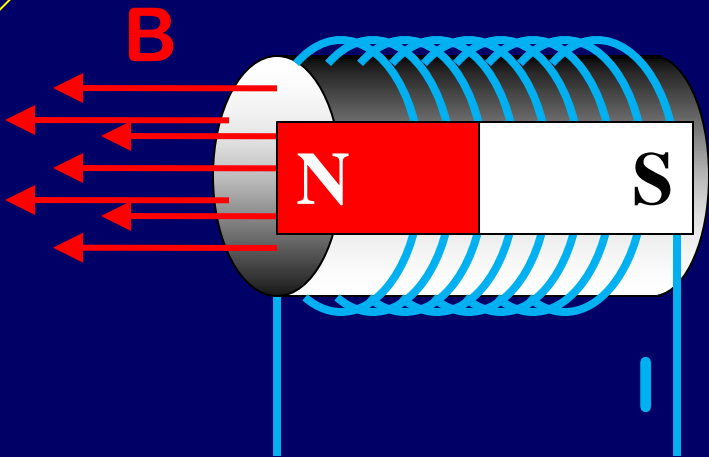
$B$  is uniform everywhere inside of solenoid:

$$B = \mu_0 n I \quad \mu_0 = 4\pi \times 10^{-7} \text{ Tm/A}$$

$n$  is the number of turns of wire/meter ( $n = N/L$ )

Direction

- Use “Right-hand rule 2”

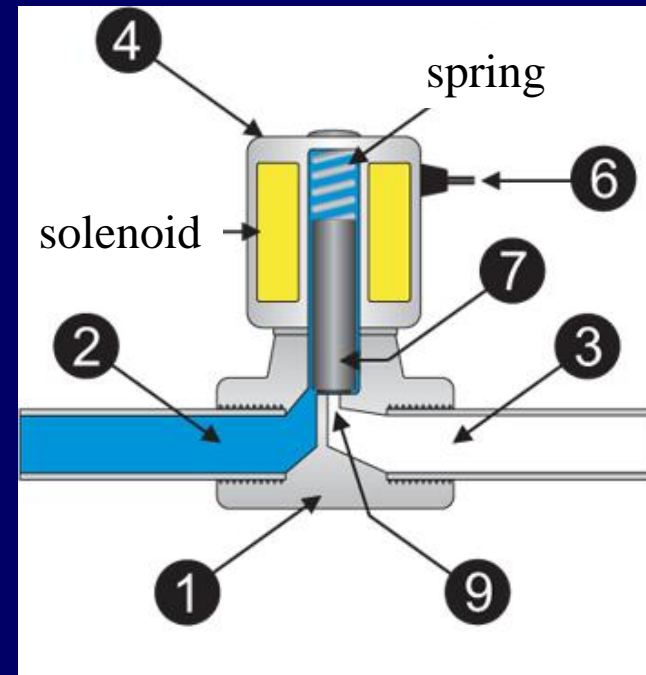


$B$  field lines look like bar magnet!

Solenoid has N and S poles! (Checkpoint 3.1)

# Electromagnets

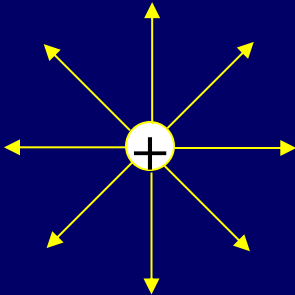
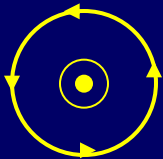
Solenoids are a way to make powerful magnets that can be turned on and off!



Solenoid valve

# Comparison:

## *Electric Field vs. Magnetic Field*

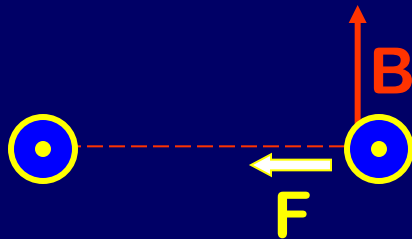
	Electric	Magnetic
Source	Charges	Moving Charges
Acts on	Charges	Moving Charges
Force	$F = Eq$	$F = q \ v \ B \ \sin(\theta)$
Direction	Parallel E	Perpendicular to v,B
Field Lines		
Opposites	Charges Attract	

# Example



## Force between current-carrying wires

Currents in same direction

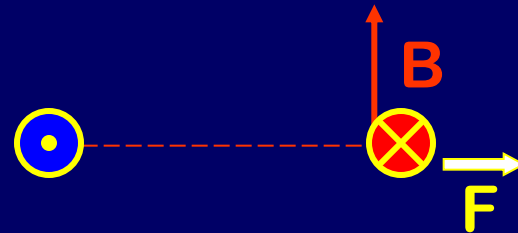


I towards us

Another I towards us

Currents in same  
direction attract!

Currents opposite direction



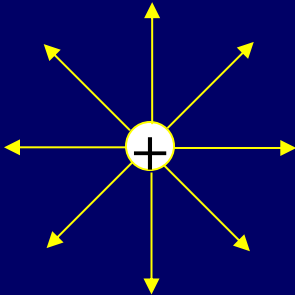
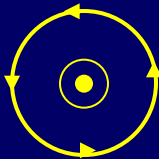
I towards us

Another I away from us

Currents in opposite  
direction repel!

# Comparison:

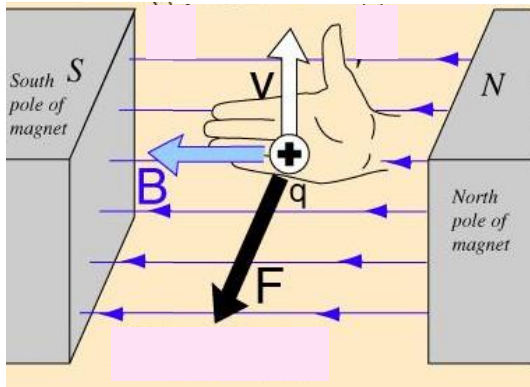
## *Electric Field vs. Magnetic Field*

	Electric	Magnetic
Source	Charges	Moving Charges
Acts on	Charges	Moving Charges
Force	$F = Eq$	$F = q \ v \ B \ \sin(\theta)$
Direction	Parallel E	Perpendicular to v,B
Field Lines	 <p>A central white circle with a black '+' sign has eight yellow arrows pointing outwards in all directions, representing the radial nature of an electric field from a positive charge.</p>	 <p>A yellow circular loop with arrows indicating a counter-clockwise direction. In the center of the loop is a small yellow dot, representing a current coming out of the page. This illustrates the circular nature of a magnetic field around a current.</p>
Opposites	Charges Attract	Currents Repel

# Summary of Right-Hand Rules

## RHR 1

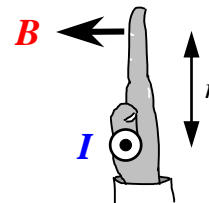
Force on moving  $q$



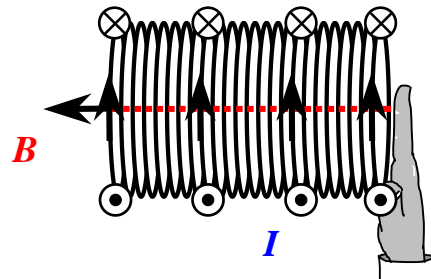
## RHR 2

B field from current  $I$

Straight wire



Solenoid



## Alternate

