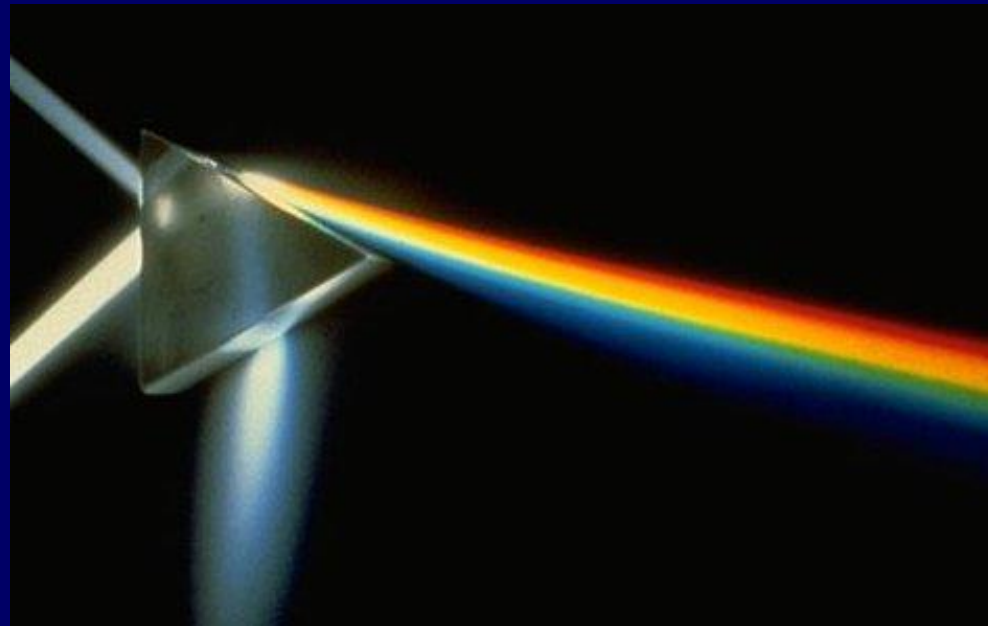


# Physics 102: Lecture 18

## Refraction!

Snell's Law, Total Internal Reflection, Dispersion, Lenses



# Exam II is Tuesday!

- What will exam cover?
  - Lectures 8 – 15 (Magnetic fields – Polarization)
- What do you need to bring?
  - All you need is a #2 pencil, calculator, and your ID
  - Go to correct room (sign-up for conflict)
- Office hours
  - Extra office hours available
- Video of Fall 13 Solutions Available

# Plane Wave Equations (useful for Hour exam 2)

$$\vec{E}(x, t) = E_{\max} \sin(kx - \omega t) \hat{z}$$

$E_{\max}$  is peak value of Electric field

$k = 2\pi / \lambda$  wave number

$x$  = traveling in + or – x direction

+ direction if relative – sign between terms

- direction if  $kx$  and  $\omega t$  have same sign

$\omega = f / 2 \pi$

$z$  = electric field points in +/- z direction

# Plane Wave Equations (useful for Hour exam 2)

$$\vec{E}(y, t) = E_{\max} \sin(-ky - \omega t) \hat{x}$$

What direction is this wave travelling?

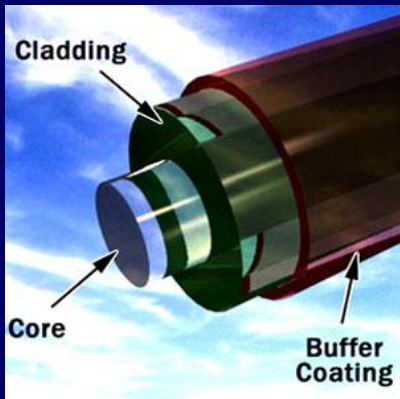
a) +x   b) -x   c) +y   d) -y

What direction does the magnetic field point?

a) x   b) y   c) z

# Summary of today's lecture

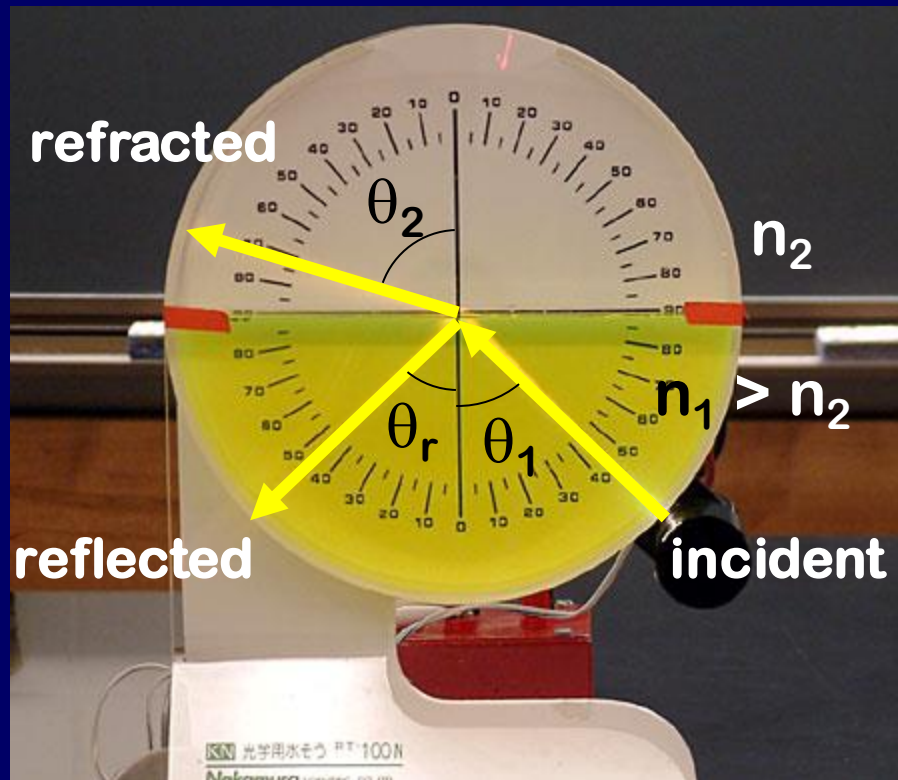
- Examples of refraction
  - 1) Total internal reflection
  - 2) Dispersion (rainbows)
  - 3) Lenses



# Refraction: Snell's Law

When light travels from one medium to another the speed (and wavelength) changes  $v=c/n$ , but the frequency is constant. So the light bends:

$$n_1 \sin(\theta_1) = n_2 \sin(\theta_2)$$





**Apparent depth:**

$$d' = d \frac{n_2}{n_1}$$

$n_2$

$n_1$

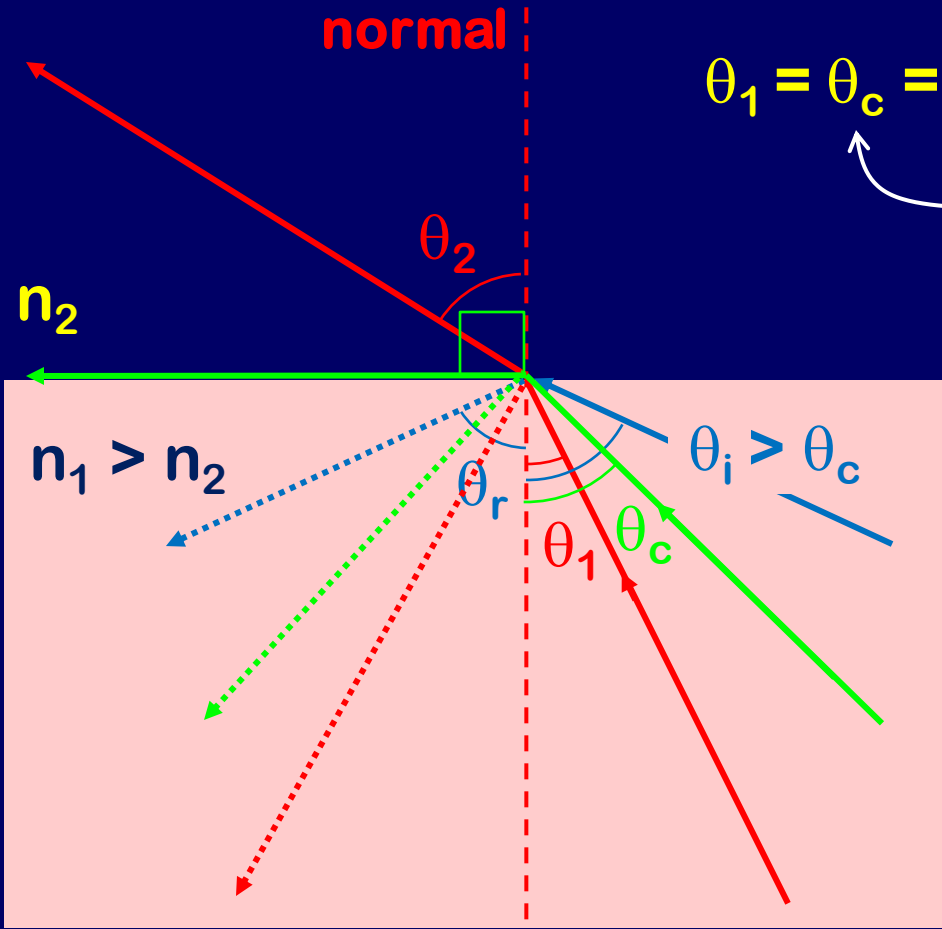
**apparent fish**

**actual fish**

# 1) Total Internal Reflection

# Snell's Law: $n_1 \sin(\theta_1) = n_2 \sin(\theta_2)$

$$(n_1 > n_2 \Rightarrow \theta_2 > \theta_1)$$



$$\theta_1 = \theta_c = \sin^{-1}(n_2/n_1) \quad \text{then} \quad \theta_2 = 90^\circ$$

- “critical angle”

Light incident at a larger angle will only have reflection ( $\theta_i = \theta_r$ )

## For water/air:

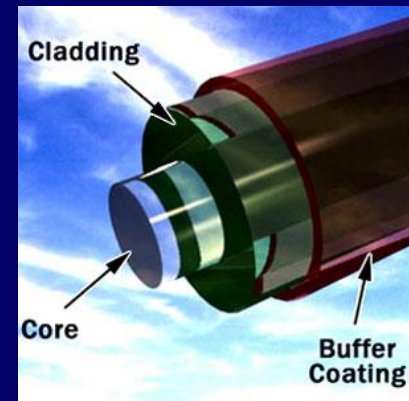
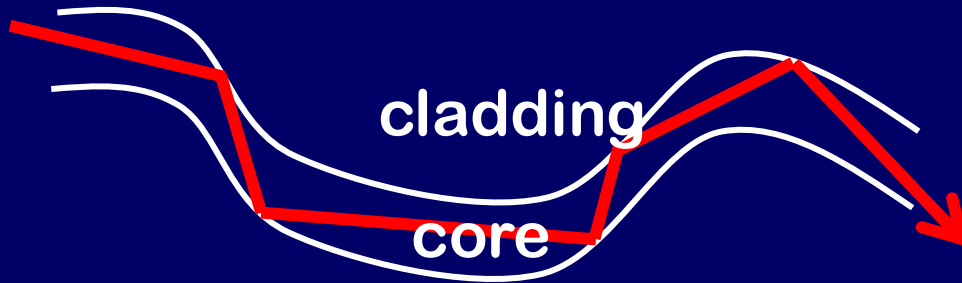
$$n_1 = 1.33, n_2 = 1$$

$$\theta_c = \sin^{-1}(n_2/n_1) = 48.8^\circ$$



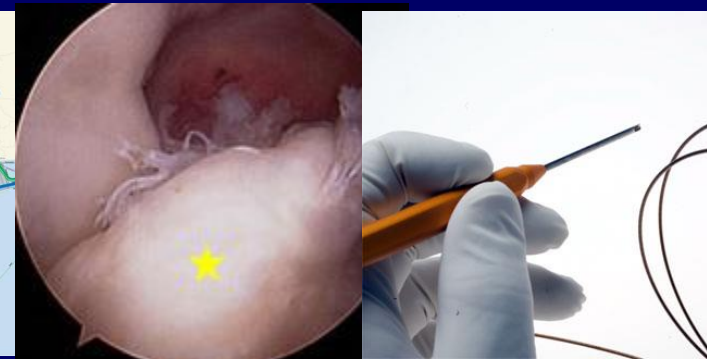
# Fiber Optics

At each contact w/ the glass air interface, if the light hits at greater than the critical angle, it undergoes total internal reflection and stays in the fiber.



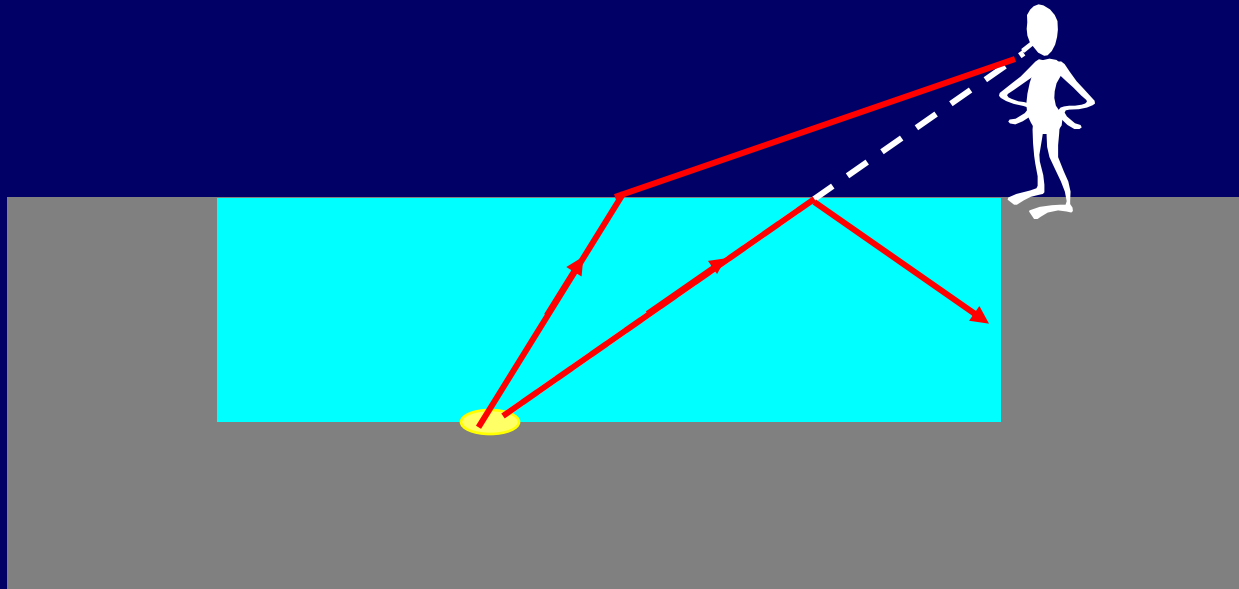
Total Internal Reflection only works if  $n_{\text{cladding}} < n_{\text{core}}$

- Telecommunications
- Arthroscopy
- Laser surgery





# ACT: Checkpoint 1.1



Can the person standing on the edge of the pool be prevented from seeing the light by total internal reflection?

1) Yes

42%

2) No

58%

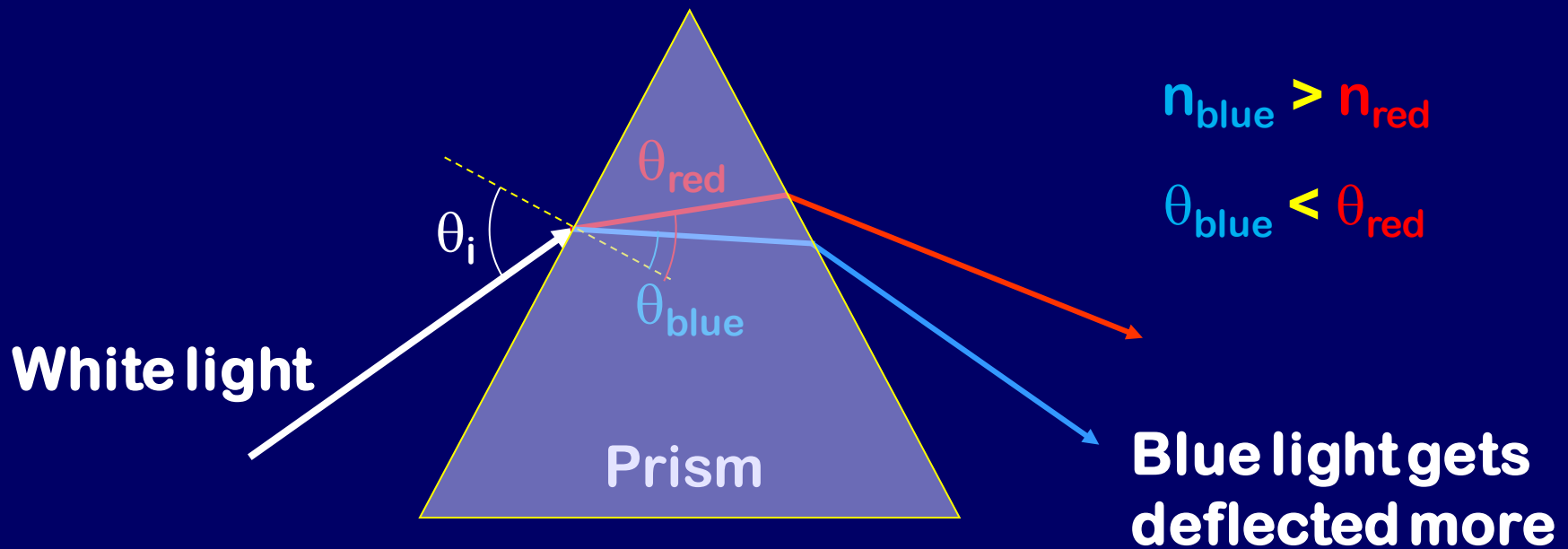
"Light is made of many light rays. Most of the rays will not be totally reflected back into the water."

## 2) Dispersion



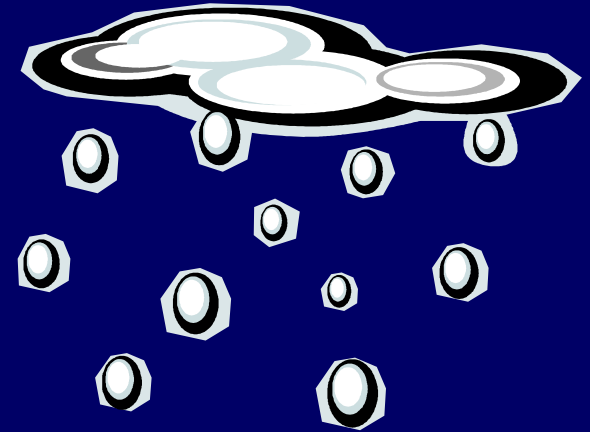
The index of refraction  $n$  depends on color!

In glass:  $n_{\text{blue}} = 1.53$       $n_{\text{red}} = 1.52$



# Rainbow:

## Checkpoint 2.1

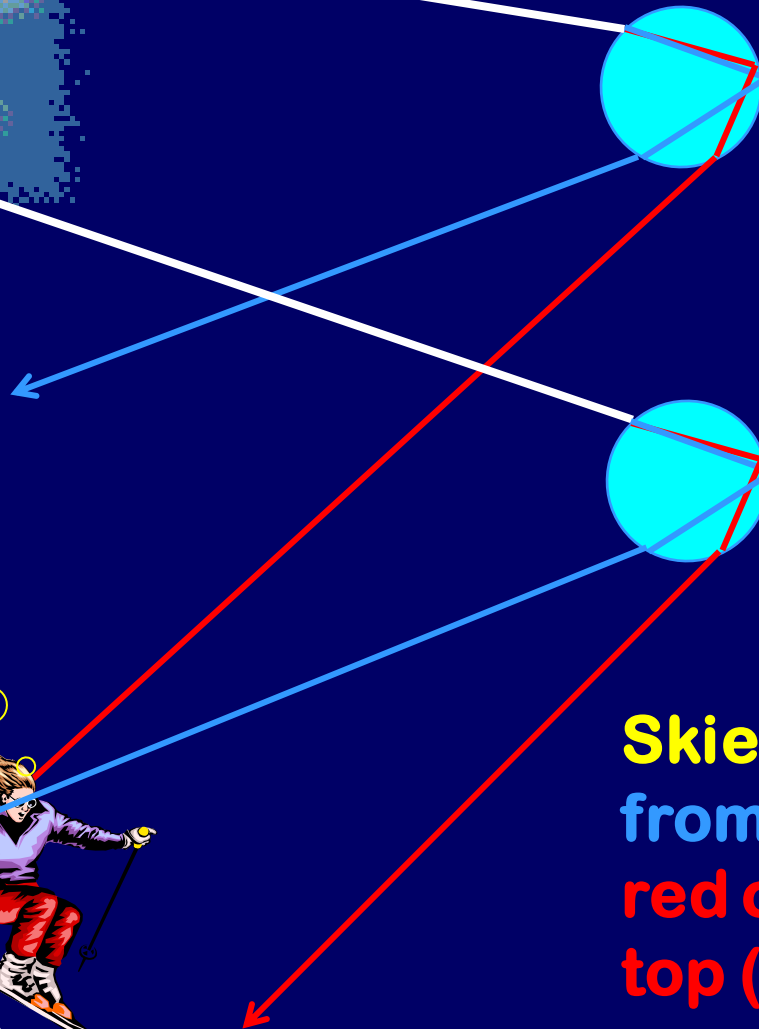
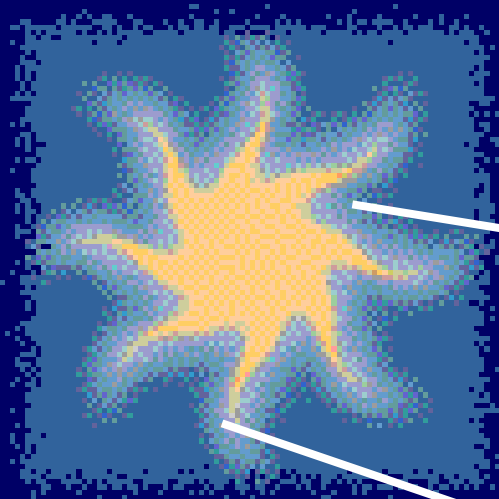


Which is red?

Which is blue?

Skier sees blue coming up from the bottom (1), and red coming down from the top (2) of the rainbow.

Blue light is deflected more!



**LIKE SO!**



**In second rainbow  
pattern is reversed**

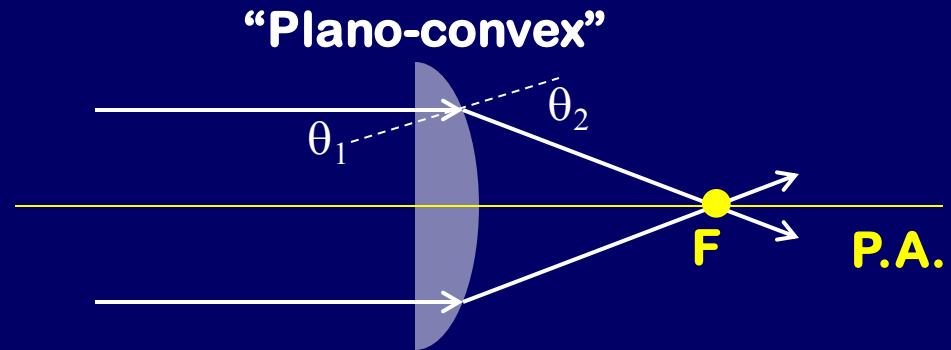


**Double rainbow**

# Lenses

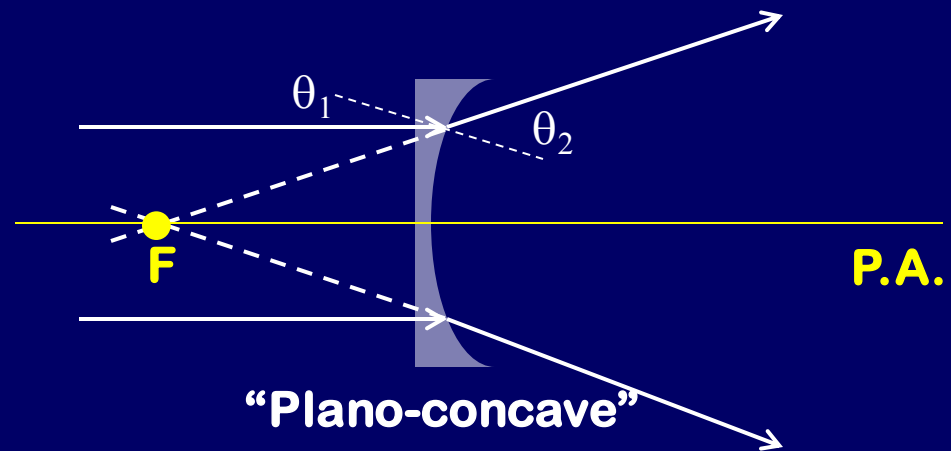
## Converging lens:

- Rays parallel to P.A. converge on focal point



## Diverging lens:

- Rays parallel to P.A. diverge as if emerging from focal point behind lens



Focal point determined by geometry and Snell's Law:  $n_1 \sin(\theta_1) = n_2 \sin(\theta_2)$

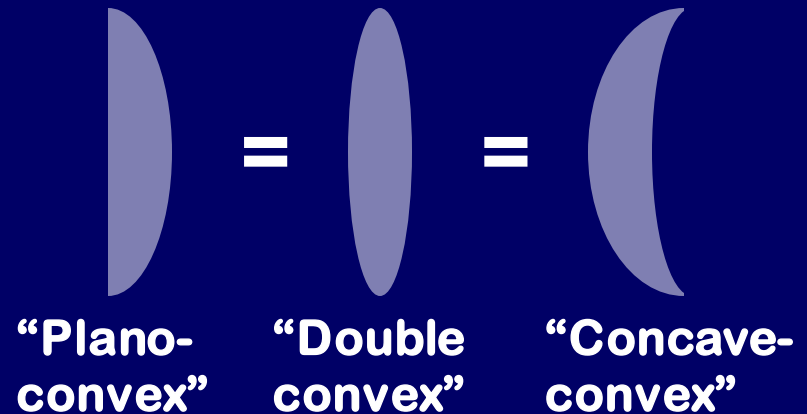
Larger  $n_2/n_1$  = more bending, shorter focal length.  
Smaller  $n_2/n_1$  = less bending, longer focal length.

# Converging & Diverging Lenses

## Converging lens:

- Rays parallel to P.A. converge on focal point

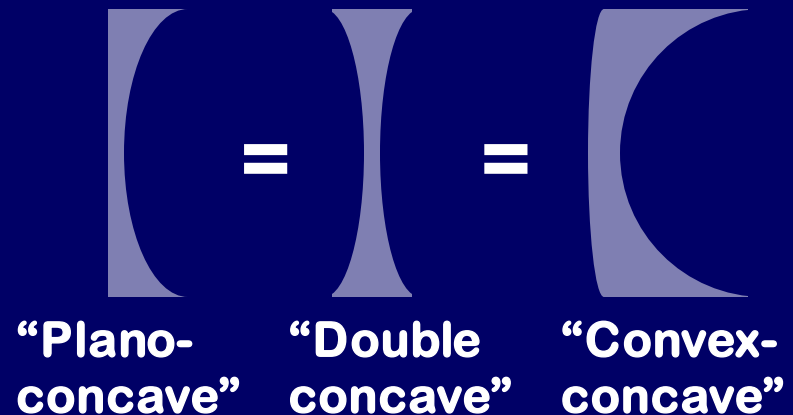
**Converging = fat in the middle**



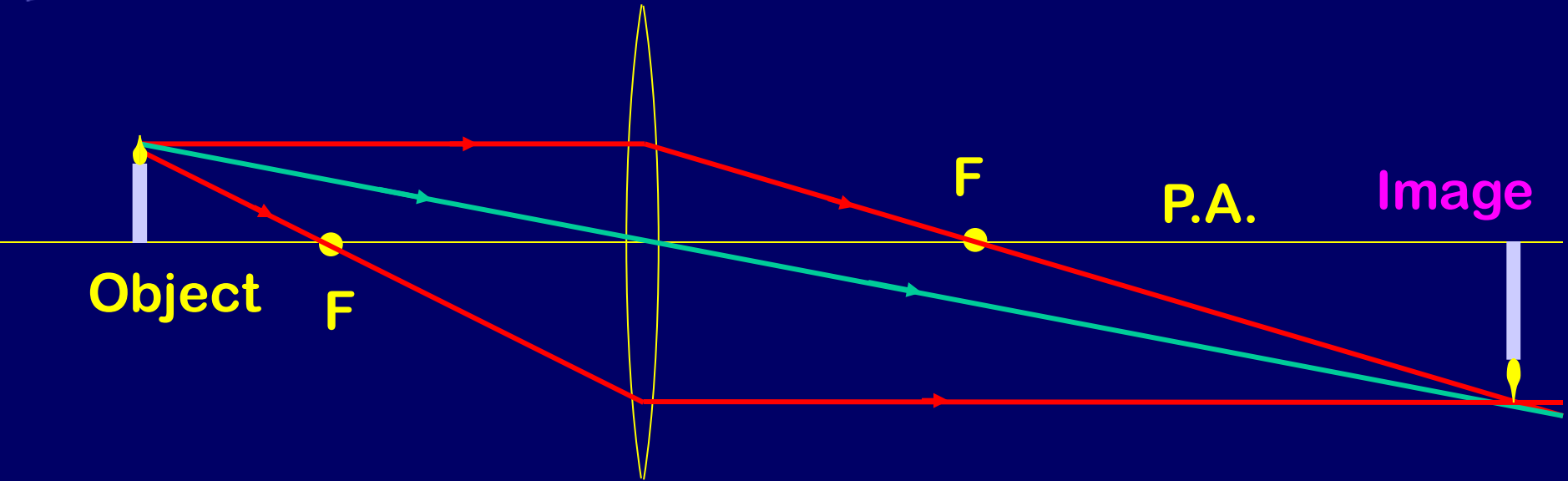
## Diverging lens:

- Rays parallel to P.A. diverge as if emerging from focal point behind lens

**Diverging = thin in the middle**



# Example Converging Lens Principal Rays



- 1) Rays **parallel** to principal axis pass through focal point.
- 2) Rays through **center** of lens are not refracted.
- 3) Rays **through F** emerge parallel to principal axis.

Image is: **real, inverted and enlarged** (in this case).

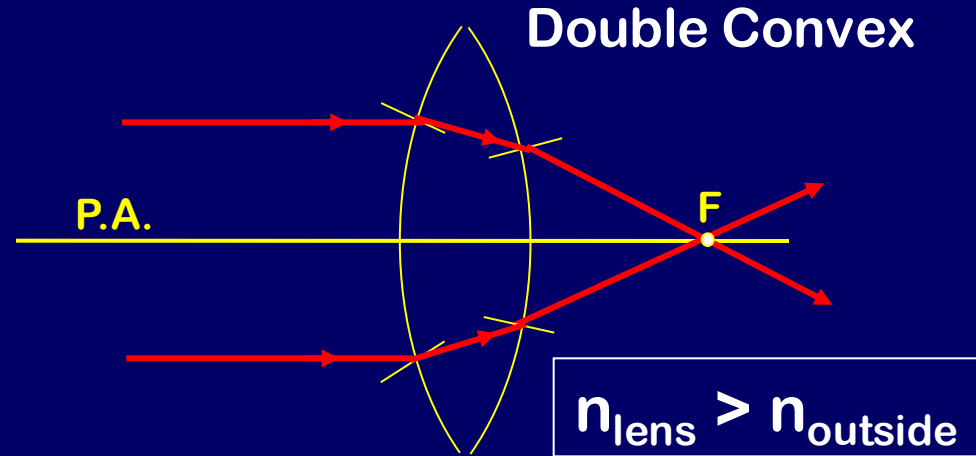
Key assumptions:

- monochromatic light incident on a **thin** lens.
- rays are all “near” the principal axis.



# Converging Lens

All rays parallel to principal axis pass through focal point F.



## Checkpoint 3.1

A beacon in a lighthouse produces a parallel beam of light. The beacon consists of a bulb and a converging lens. Where should the bulb be placed?

71%

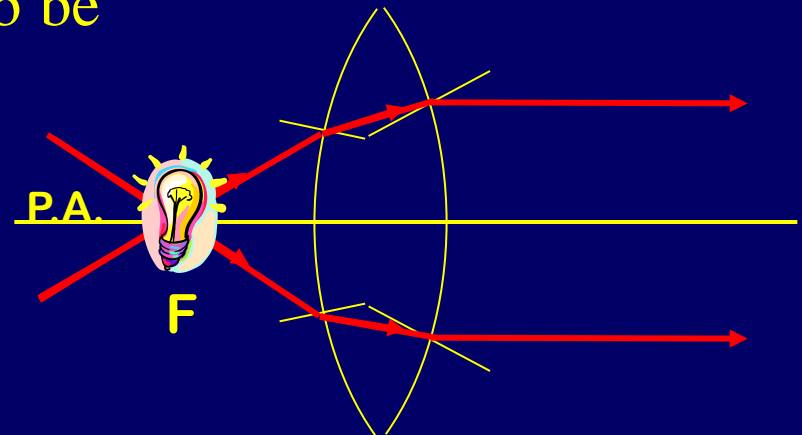
A. At F

17%

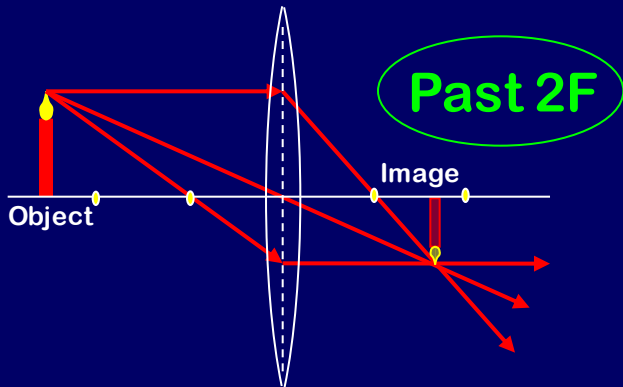
B. Inside F

12%

C. Outside F

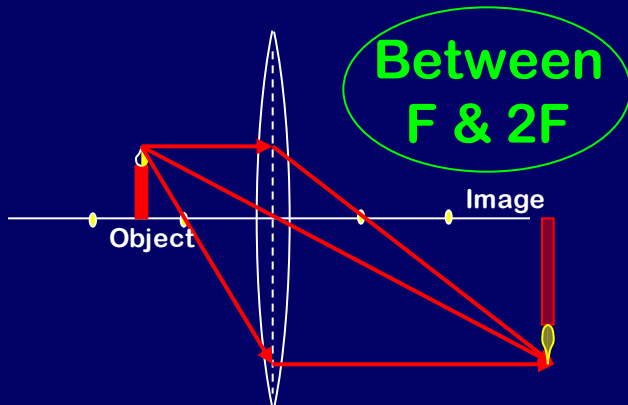


# 3 Cases for Converging Lenses



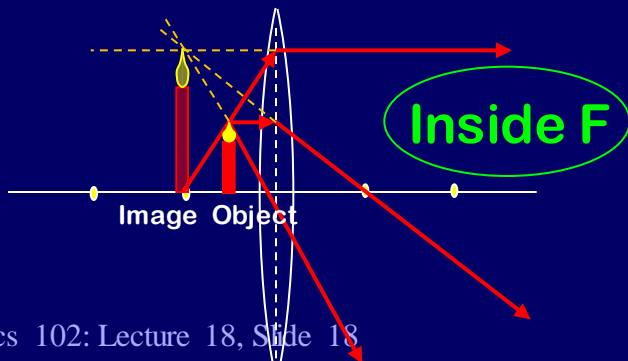
**Inverted  
Reduced  
Real**

This could be used in a camera.



**Inverted  
Enlarged  
Real**

This could be used as a projector.



**Upright  
Enlarged  
Virtual**

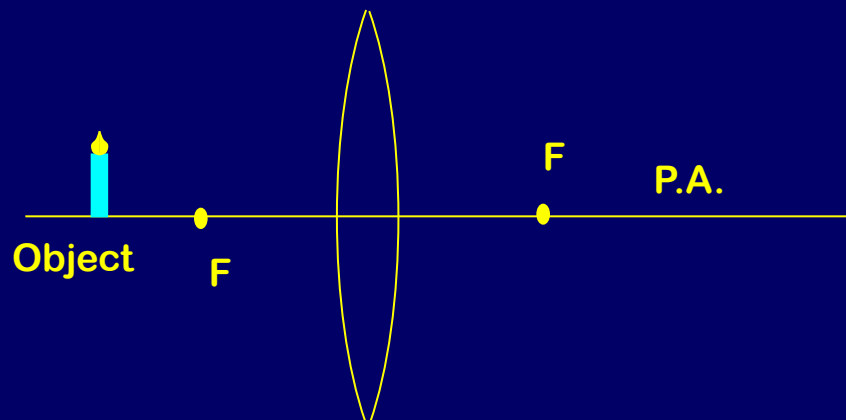
This is a magnifying glass.





# ACT: Converging Lens

Which way should you move object so image is real and diminished?



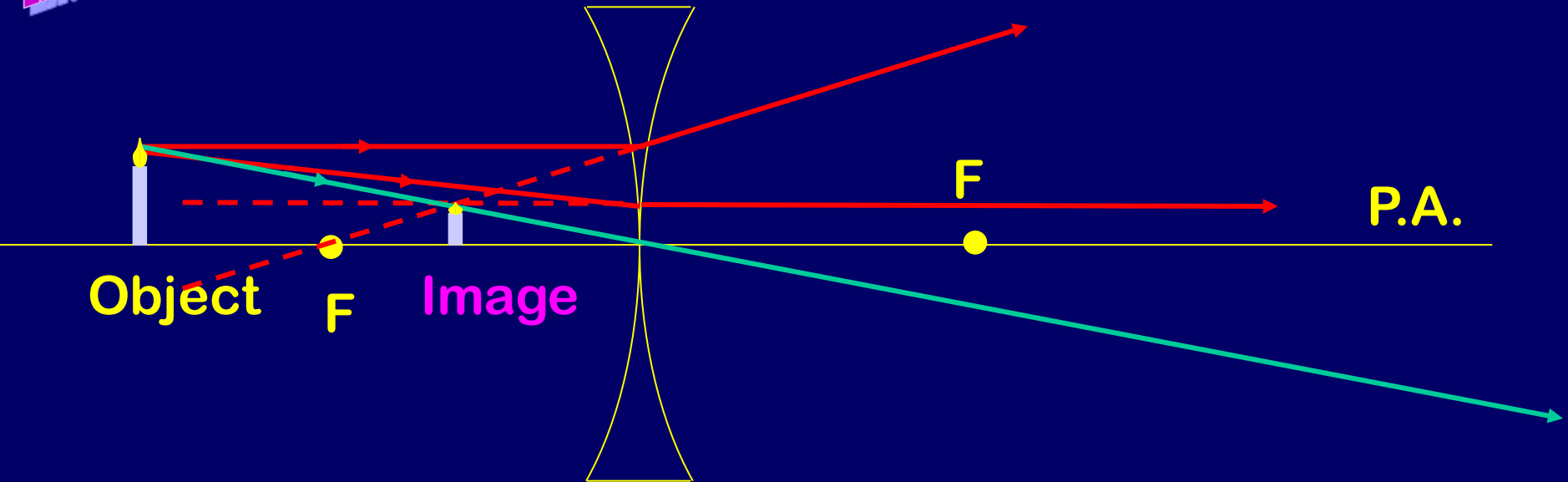
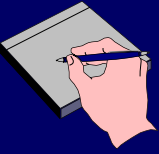
(A) Closer to lens

(B) Further from lens

(C) Converging lens can't create real diminished image.

## Example

# Diverging Lens Principal Rays



- 1) Rays **parallel** to principal axis pass through focal point.
- 2) Rays through **center** of lens are not refracted.
- 3) Rays **toward F** emerge parallel to principal axis.

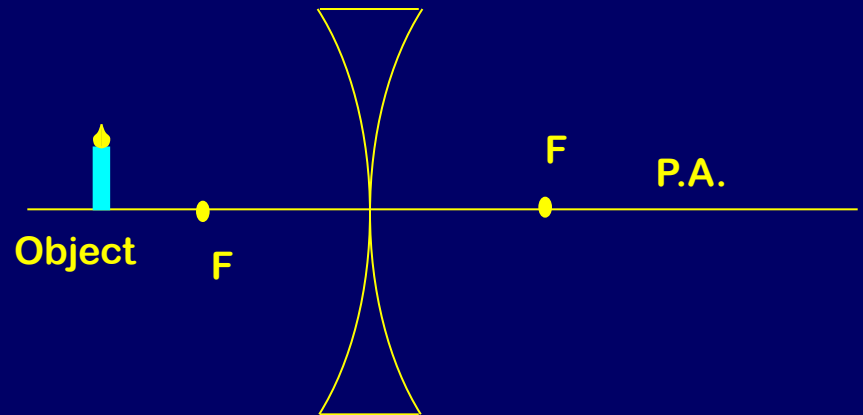
Only 1 case for diverging lens:

Image is always **virtual, upright, and reduced.**



# ACT: Diverging Lenses

Which way should you move object so image is real?



- 1) Closer to lens
- 2) Further from lens
- 3) Diverging lens can't create real image.