

# Exam III on Monday Nov. 18!

- What will exam cover?
  - Lect. 16 – first  $\frac{1}{2}$  of Lect. 22 (Reflection – Resolving power)
- How do you study?
  - Start studying now! (cramming DOES NOT work)
  - Emphasize understanding concepts & problem solving,
  - Understand formula sheet & know what each symbol means
- Lecture next Wednesday, Nov. 13
  - I will be out of town, Alfredo Sanchez will teach
- Review, Sunday, Nov. 17, 2 PM, 141 Loomis
  - I will go over a past midterm

# Physics 102: Lecture 21

## Thin Films & Diffraction Gratings



Fraunhofer's solar spectrum (1814)

*A a B C D E b F G H*



Name	Wavelength	Origin	Name	Wavelength	Origin
<i>A</i>	7594	$O_2$	<i>T</i>	5270	$Fe\ 1$
<i>a</i>	7165	$H_2O$	<i>b</i>	5170, 5180	$Mg\ 1$
<i>B</i>	6867	$O_2$	<i>F</i>	4861	$H_{\beta}$
<i>C</i>	6563	$H_{\alpha}$	<i>G</i>	4300	$CH$
<i>D</i>	5890, 5896	$Na\ 1$	<i>H</i>	3968	$Ca\ 2$

# Recall

Same for  $\lambda$

- **Interference** (at least 2 coherent waves)

- Constructive (full wavelength difference)
- Destructive (half wavelength difference)

- **Light** (1 source, but different paths)

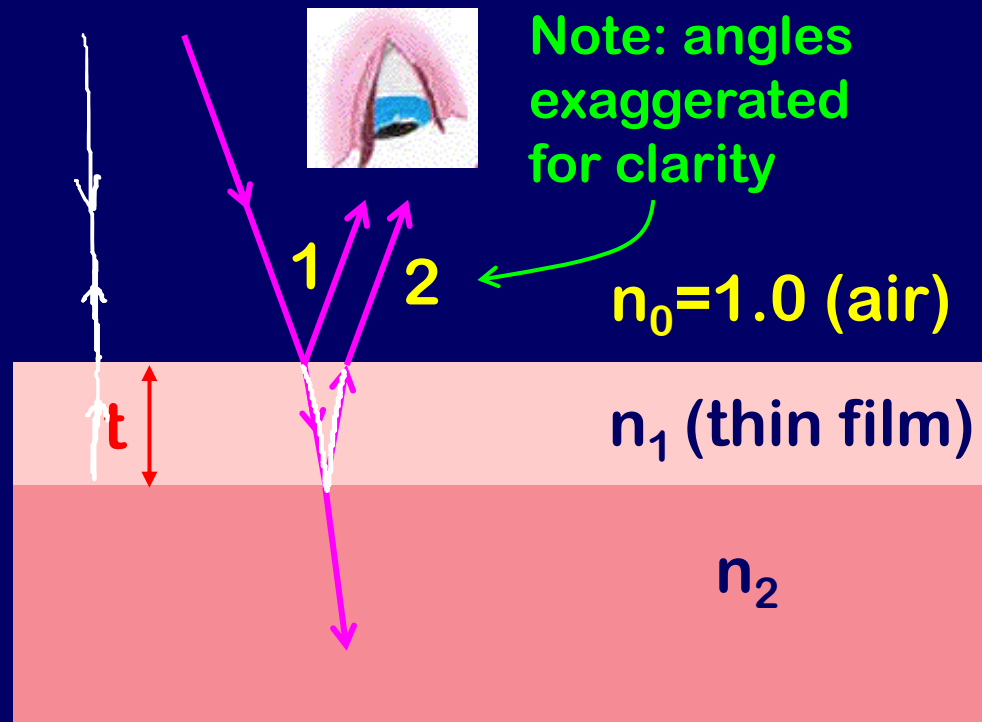
- Young's double slit
- Thin films
- Multiple slit
- X-ray diffraction from crystal
- Diffraction/single slit

Last lecture

Today's lecture

# Thin Film Interference

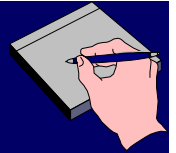
Light is incident normal to a thin film



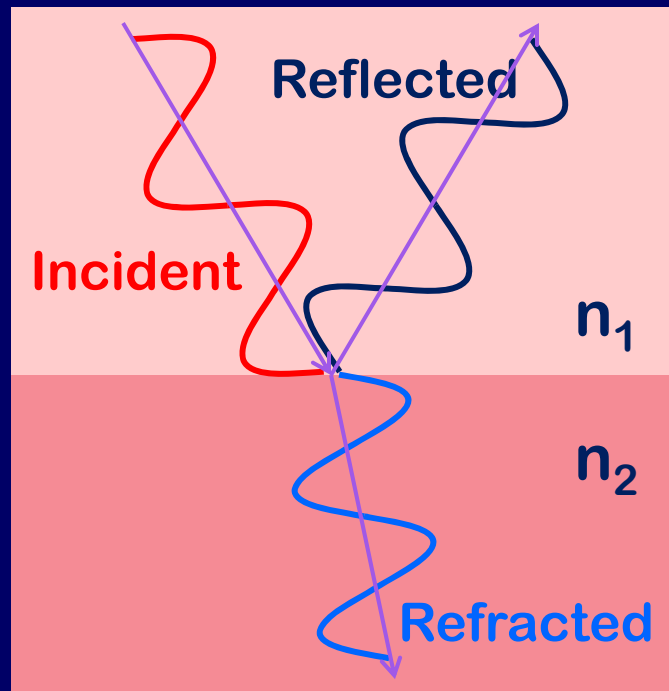
Get two waves by reflection off two different interfaces: interference!

Ray 2 travels approximately  $2t$  further than ray 1.

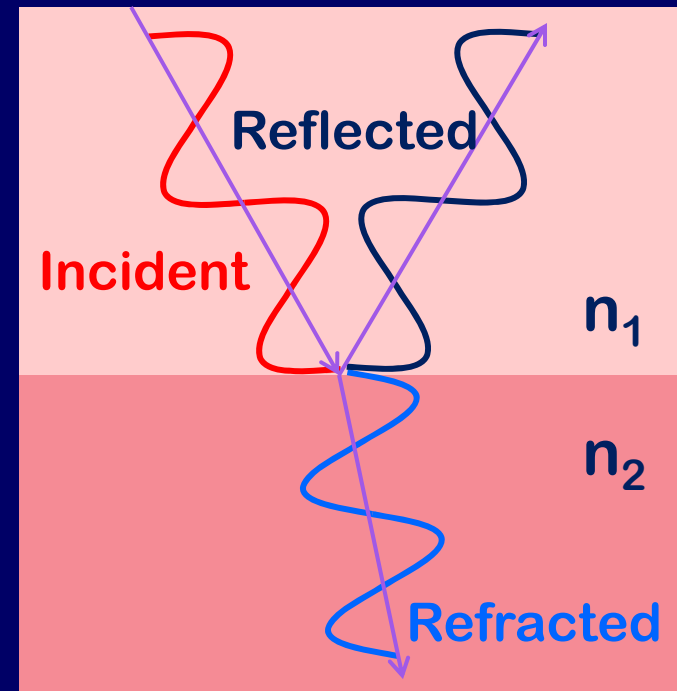
# Reflection & Phase Shifts



Upon reflection from a boundary between two transparent materials, the phase of the reflected light may change.



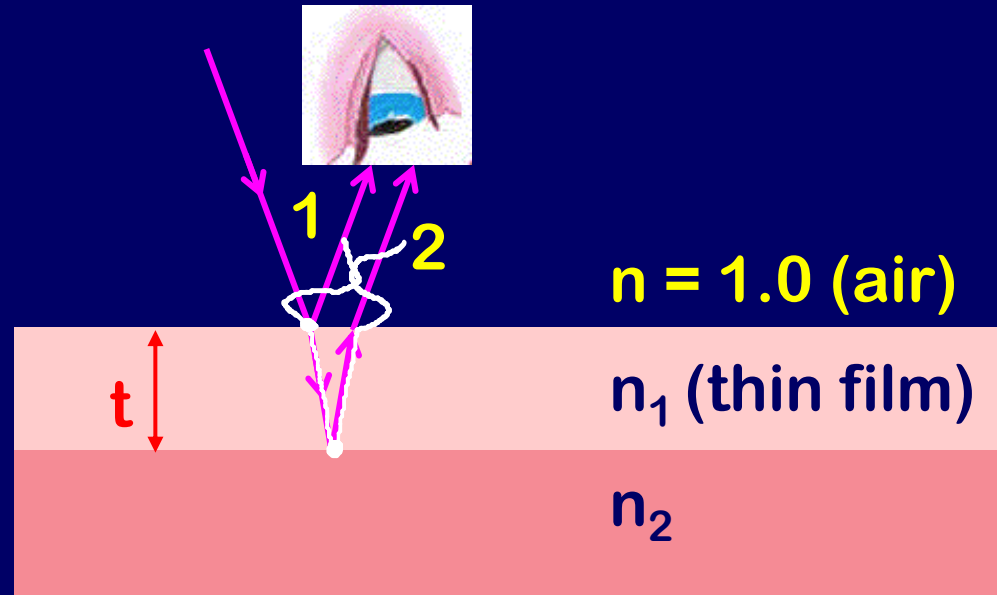
- If  $n_1 > n_2$  – no phase change upon reflection



- If  $n_1 < n_2$  –  $180^\circ$  phase change upon reflection
- This is like the wave went an extra  $\lambda/2$ ;  $\delta = 1/2$

# Thin Film Summary

Determine  $\delta$ , number of extra wavelengths for each ray.



This is important!

Ray 1:  $\delta_1 = \underbrace{0 \text{ or } \frac{1}{2}}_{\text{Reflection}} + \underbrace{0}_{\text{Distance}}$

Ray 2:  $\delta_2 = 0 \text{ or } \frac{1}{2} + 2t \underbrace{\lambda_{\text{film}}}_{\text{Distance}}$

**Note: this is wavelength in film!** ( $\lambda_{\text{film}} = \lambda_o / n_1$ )

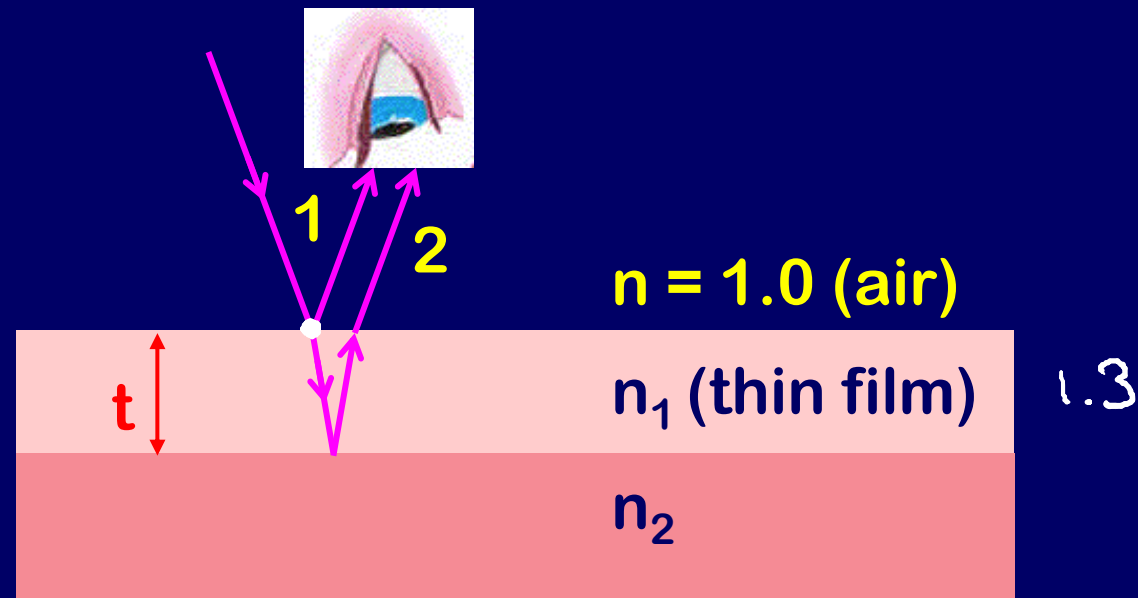
If  $|\delta_2 - \delta_1| = 0, 1, 2, 3 \dots$  (m) **constructive**

If  $|\delta_2 - \delta_1| = \frac{1}{2}, 1 \frac{1}{2}, 2 \frac{1}{2} \dots$  ( $m + \frac{1}{2}$ ) **destructive**



# ACT: Thin Film Practice

Blue light ( $\lambda_0 = 500 \text{ nm}$ ) incident on a glass ( $n_1 = 1.5$ ) cover slip ( $t = 167 \text{ nm}$ ) floating on top of water ( $n_2 = 1.3$ ).



What is  $\delta_1$ , the total phase shift for ray 1

A)  $\delta_1 = 0$

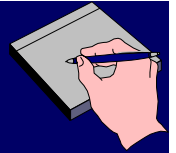
B)  $\delta_1 = \frac{1}{2}$

C)  $\delta_1 = 1$

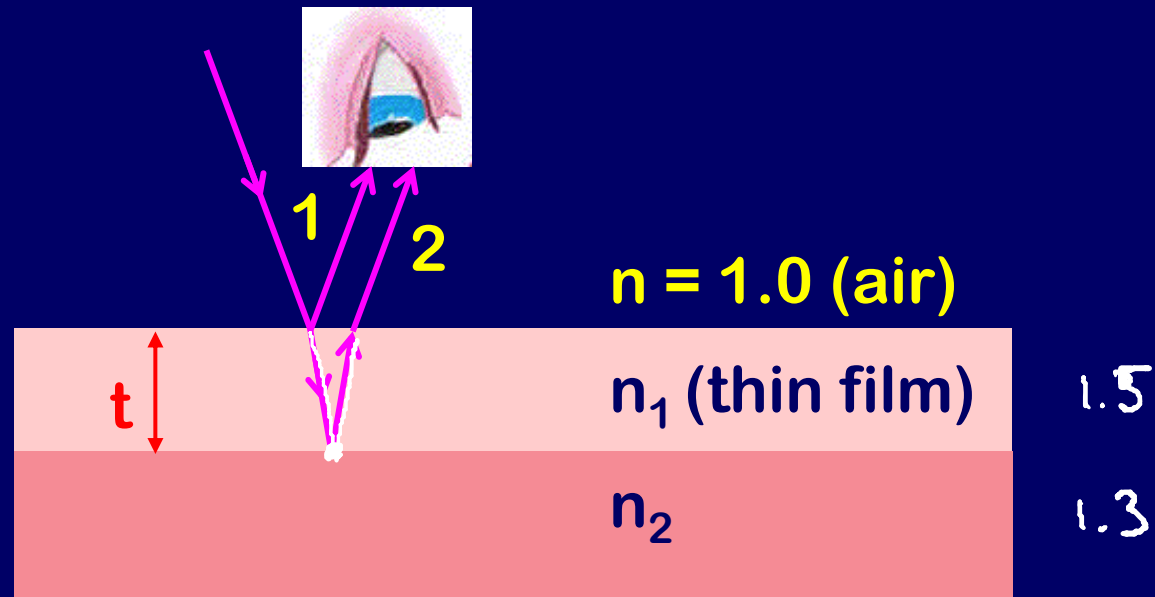
# Example

## Thin Film Practice

### Checkpoint 1.2



Blue light ( $\lambda_0 = 500 \text{ nm}$ ) incident on a glass ( $n_1 = 1.5$ ) cover slip ( $t = 167 \text{ nm}$ ) floating on top of water ( $n_2 = 1.3$ ).



Is the interference **constructive** or **destructive** or neither?

$$\delta_1 = \frac{1}{2}$$

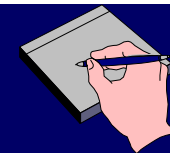
$$\delta_2 = 0 + 2t / \lambda_{\text{glass}} = 2t n_{\text{glass}} / \lambda_0 = (2)(167)(1.5) / 500 = 1$$

$$\text{Phase shift} = |\delta_2 - \delta_1| = \frac{1}{2} \text{ wavelength}$$



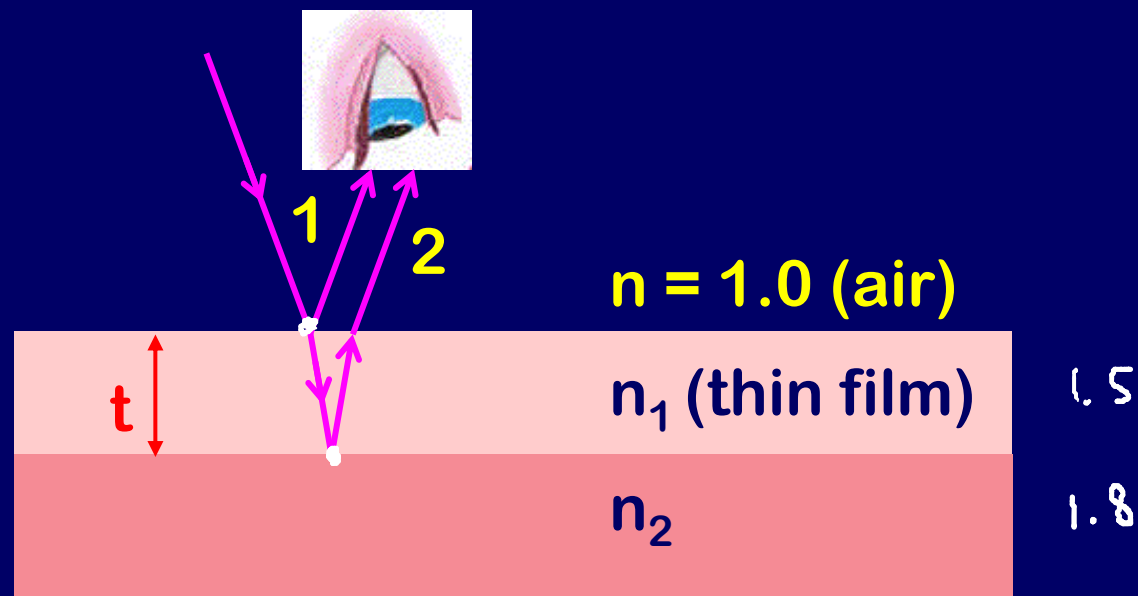
# Example

## ACT: Thin Film Practice II



### Checkpoint 1.1

Blue light ( $\lambda_0 = 500 \text{ nm}$ ) incident on a glass ( $n_1 = 1.5$ ) cover slip ( $t = 167 \text{ nm}$ ) floating on top of plastic ( $n_2 = 1.8$ ).



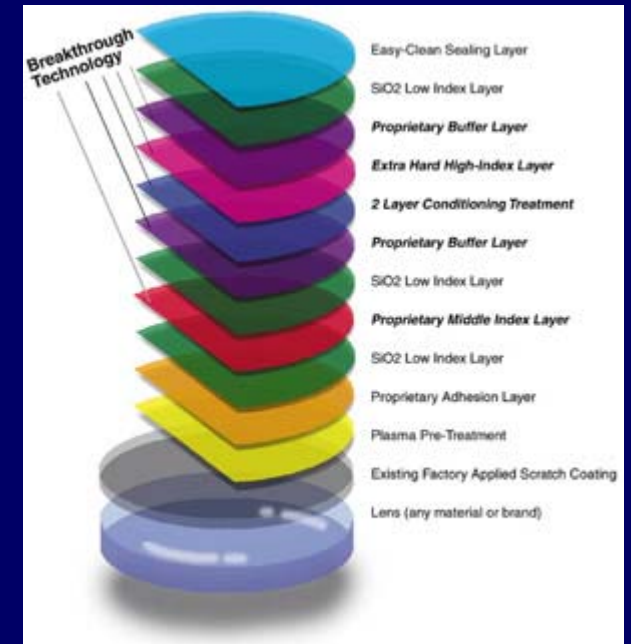
Is the interference : **A) constructive** B) destructive C) neither?

$$\delta_1 = \frac{1}{2}$$

$$\delta_2 = \frac{1}{2} + 2t / \lambda_{\text{glass}} = \frac{1}{2} + 2t n_{\text{glass}} / \lambda_0 = (2)(167)(1.5)/500 = 3/2$$

$$\text{Phase shift} = |\delta_2 - \delta_1| = 1 \text{ wavelength}$$

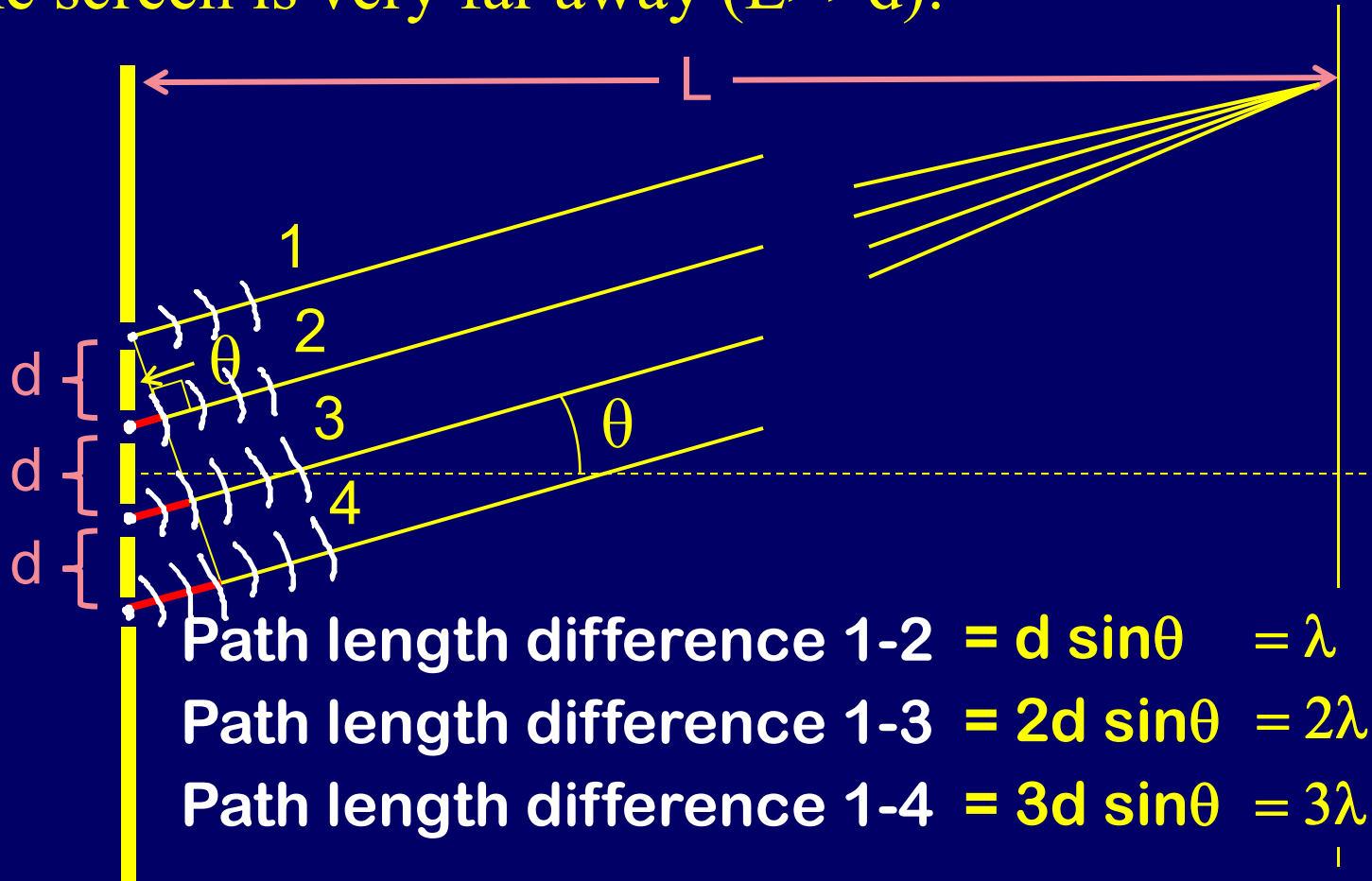
# Thin film application: Anti-reflection coatings



# Diffraction Gratings: multiple slits

(N slits with spacing d)

Assume screen is very far away ( $L \gg d$ ):



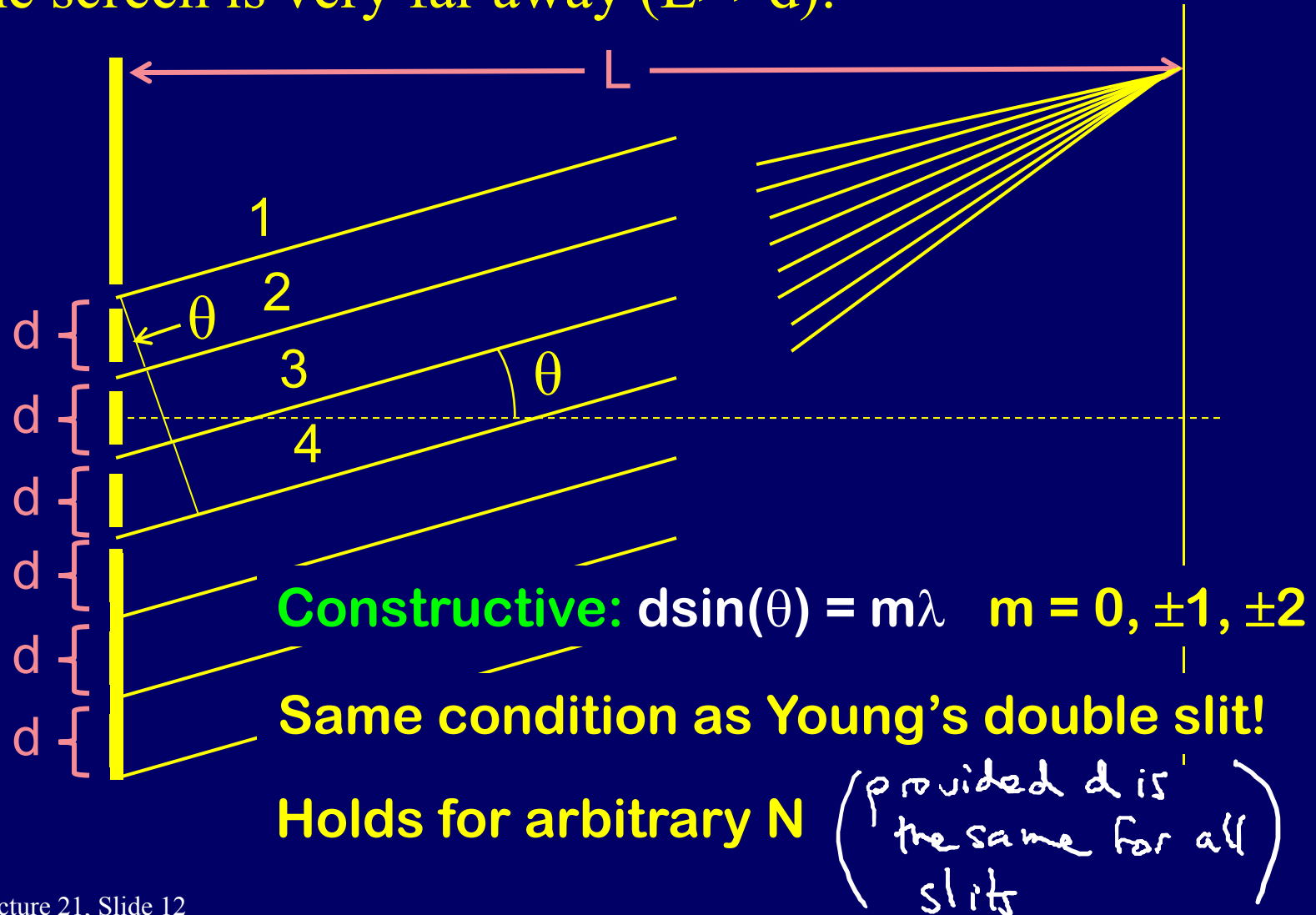
Constructive interference for all paths when

$$d \sin(\theta) = m\lambda \quad m = 0, \pm 1, \pm 2$$

# Multiple Slits:

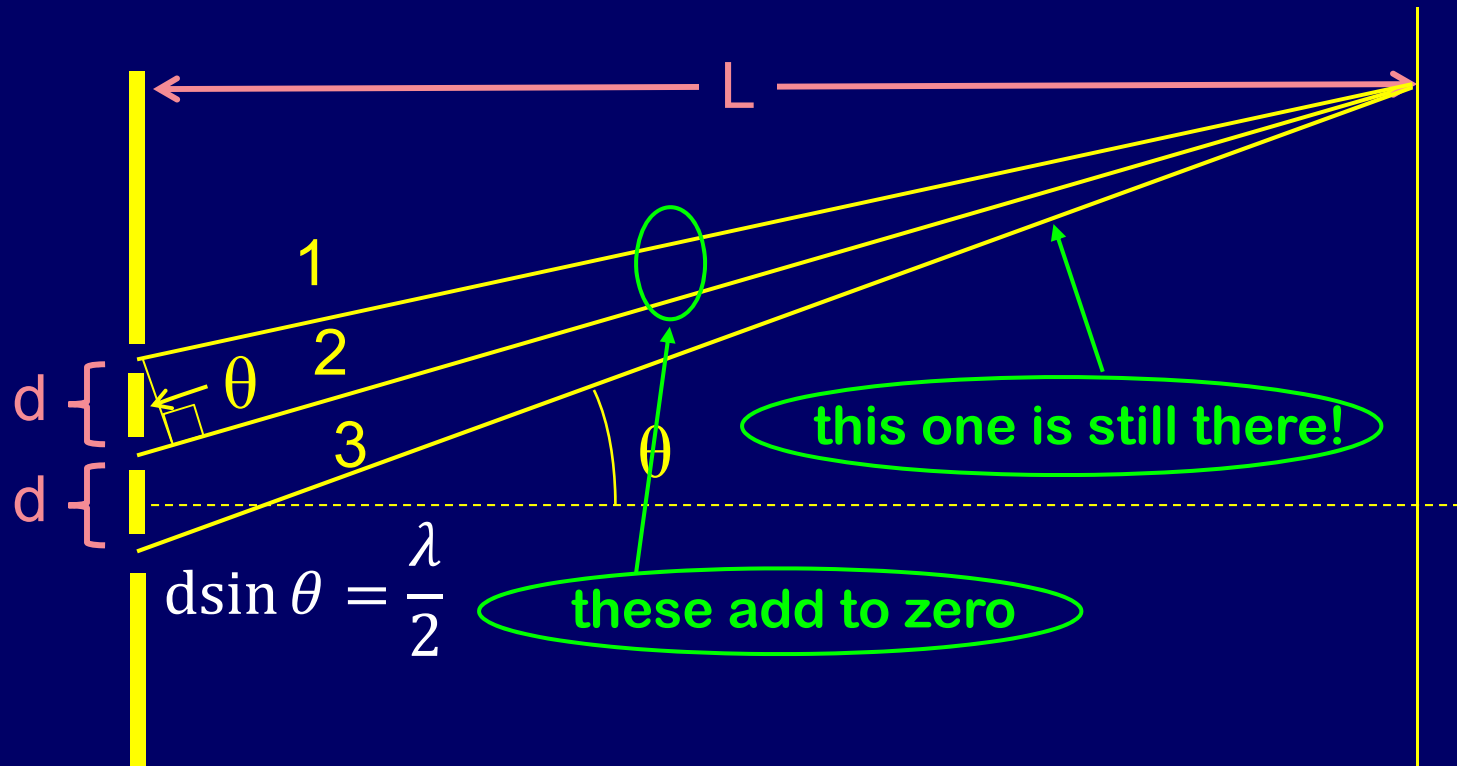
(Diffraction Grating – N slits with spacing d)

Assume screen is very far away ( $L \gg d$ ):





# ACT/Checkpoint 2

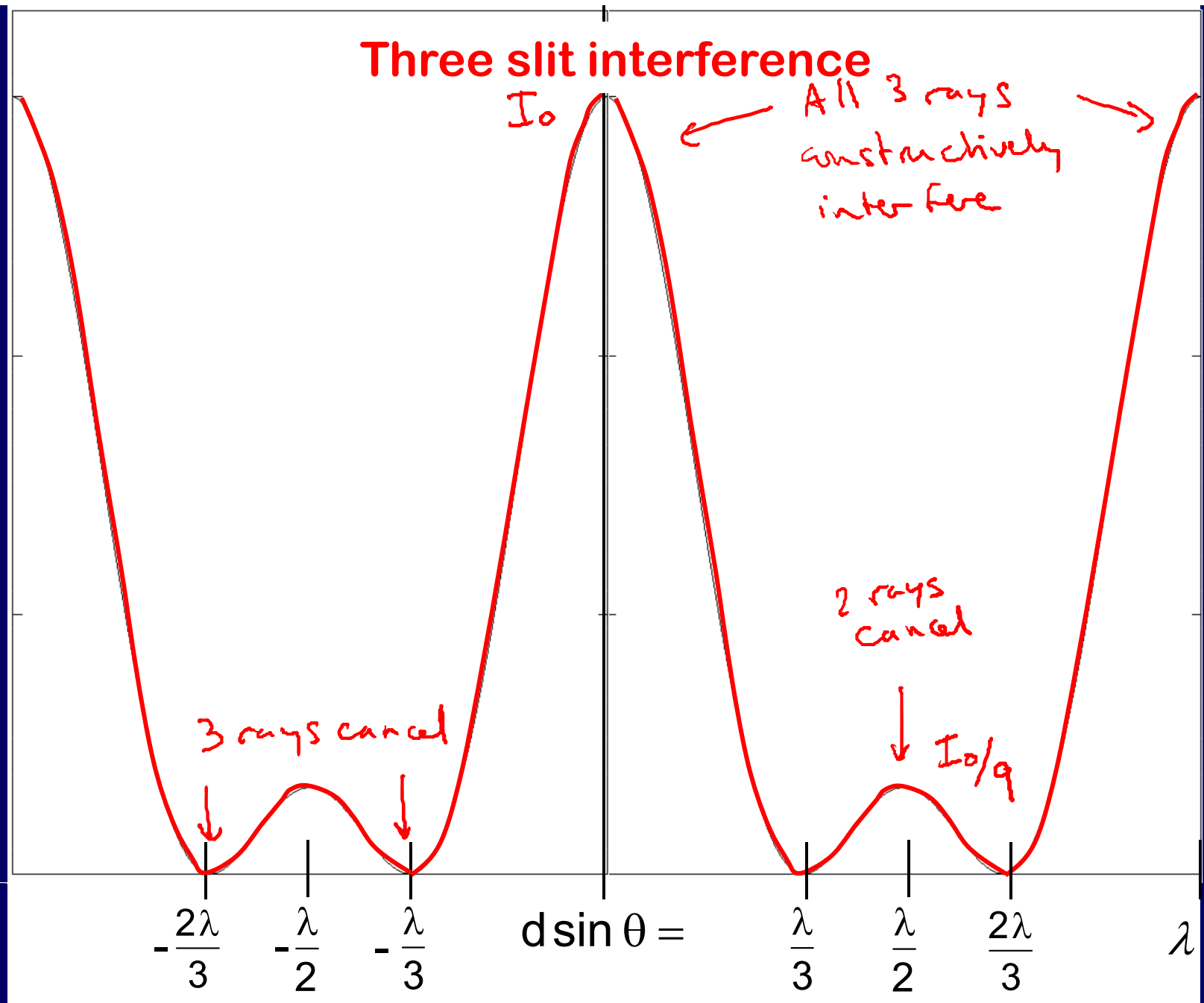


When rays 1 and 2 are interfering destructively, is the intensity from the three rays a minimum? A) Yes B) No

46%

54%

Rays 1 and 2 completely cancel, but ray 3 is still there.



# Multiple Slit Interference

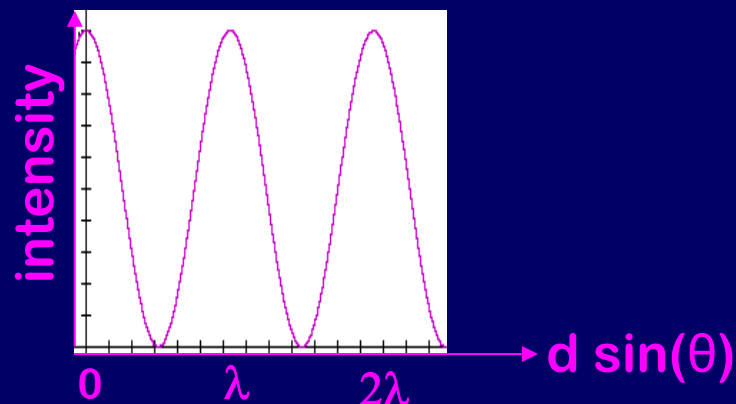
## (Diffraction Grating)

For many slits, maxima are still at  $\sin \theta = m \frac{\lambda}{d}$

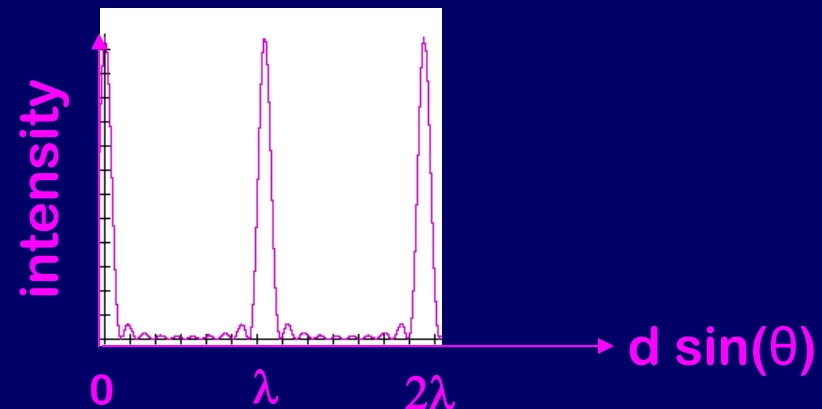
Peak location  
depends on  
wavelength!

Region between maxima gets suppressed more and more as no. of slits increases – bright fringes become narrower and brighter.

2 slits (N=2)



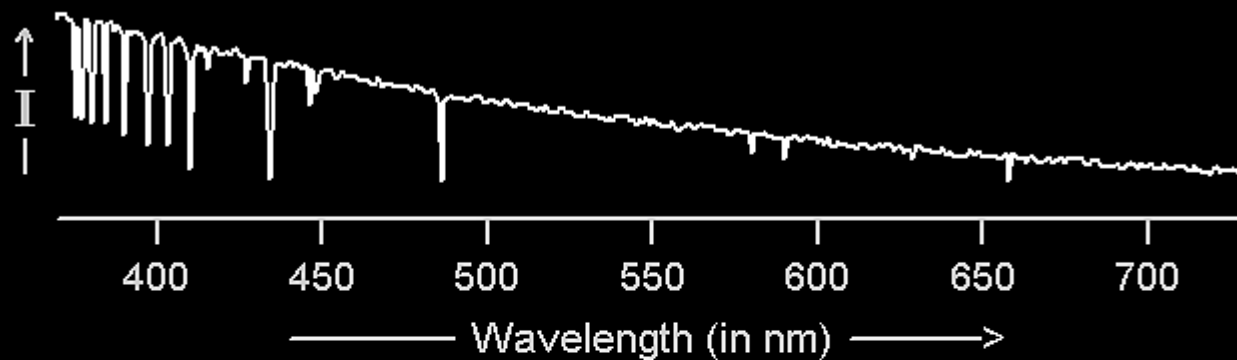
10 slits (N=10)



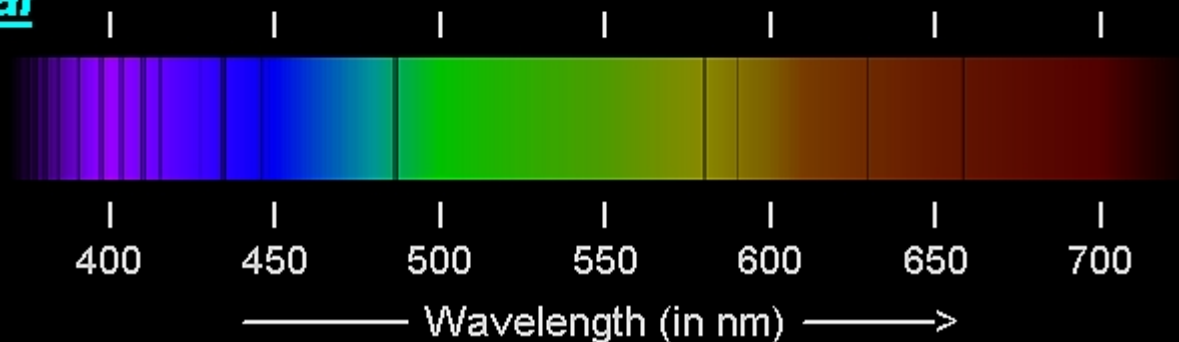
Diffraction grating:  
spreads out different wavelengths, determine spectrum

# Solar spectrum!

## Graphical



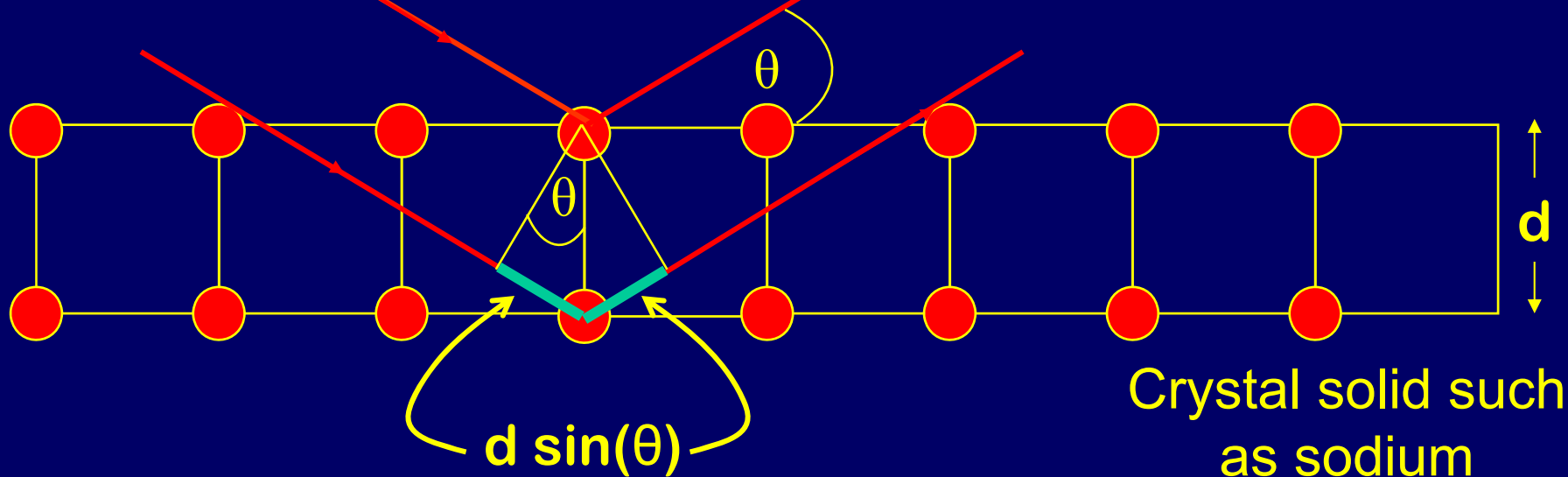
## Visual





# X-Ray Diffraction:

A technique to study crystal structure



Constructive interference:  $2d \sin(\theta) = m\lambda$

$d \approx 0.5\text{nm}$  in NaCl

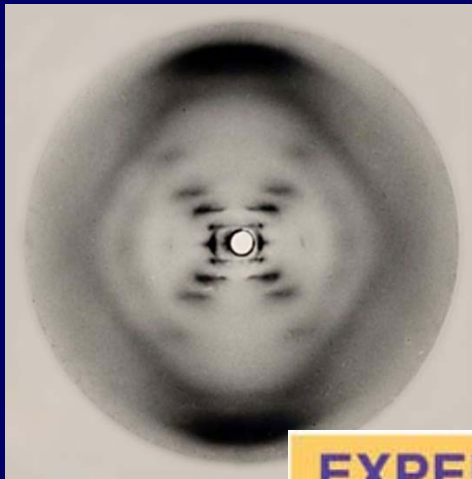
For  $\lambda = 0.017\text{nm}$   
X-ray

$m = 1$   
1<sup>st</sup> maximum will be at  $10^0$

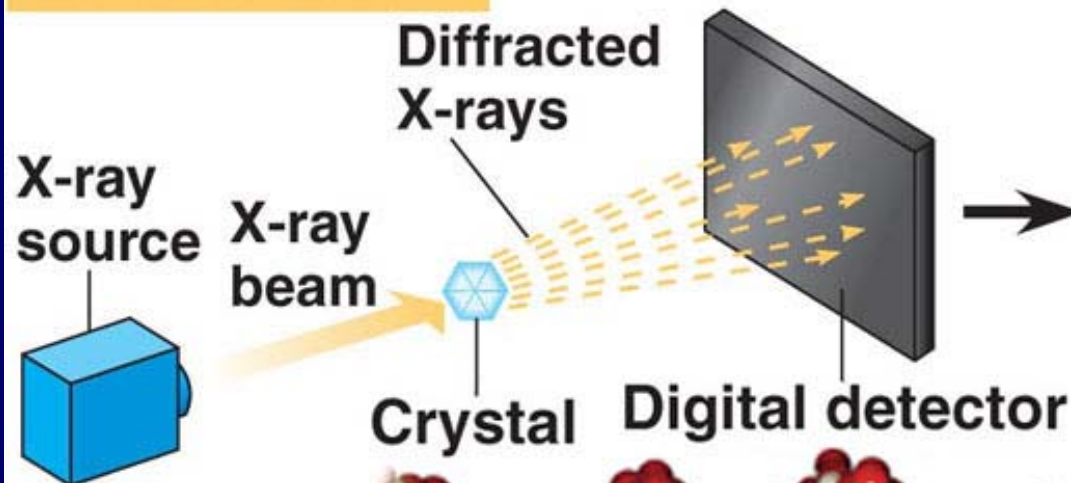
$$\sin \theta = \frac{\lambda}{2d}$$

$$\lambda < 2d$$

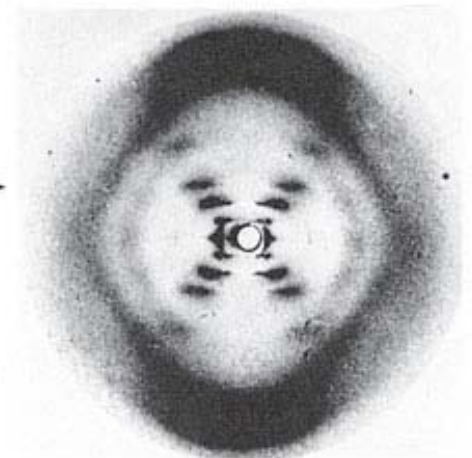
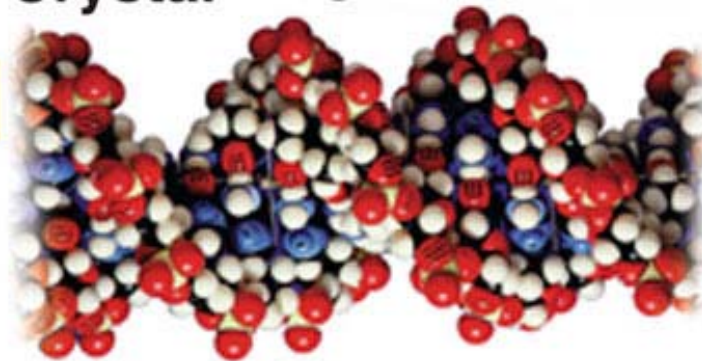
Measure  $\theta$ , determine  $d$



## EXPERIMENT



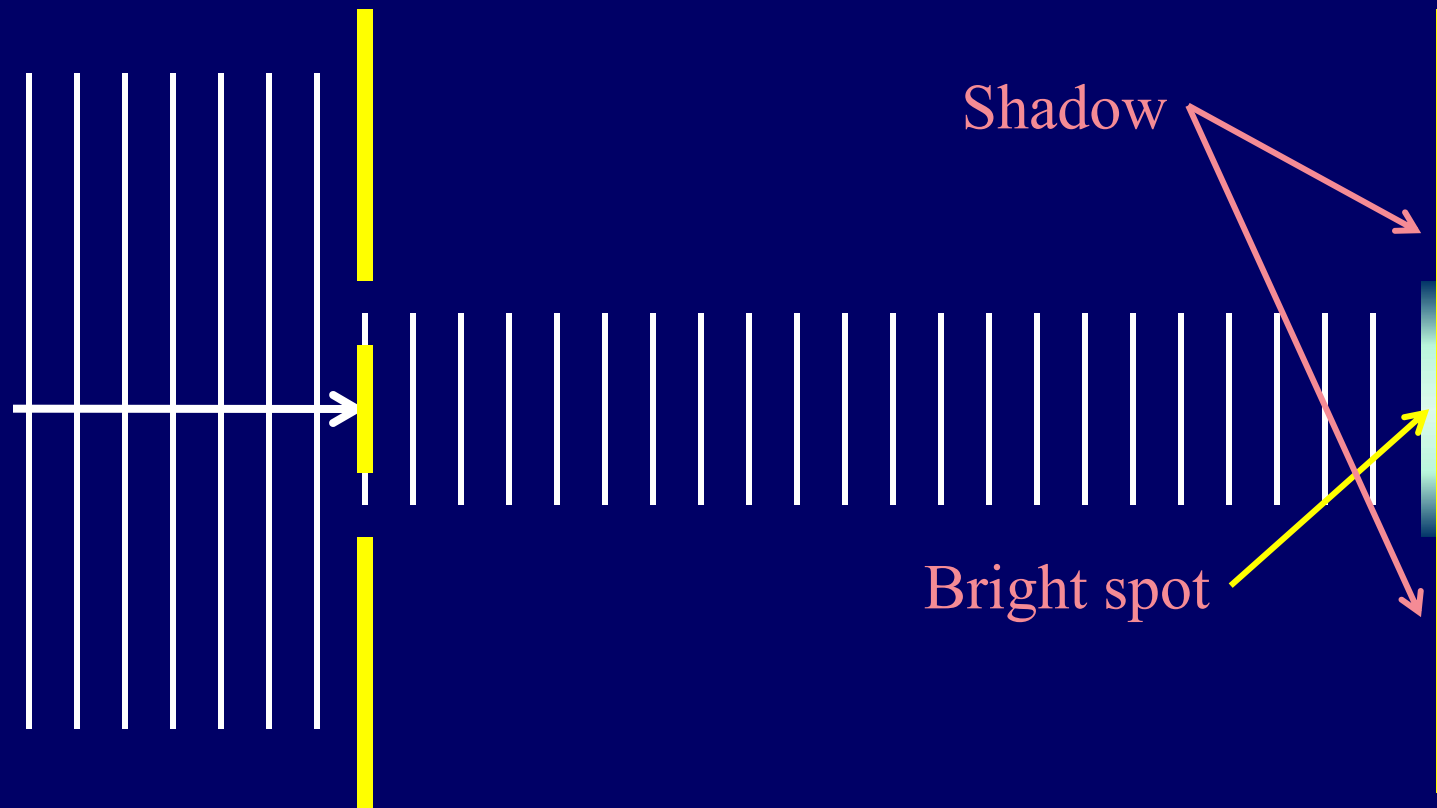
## RESULTS



Franklin's X-ray diffraction photograph of DNA

# Single slit interference?

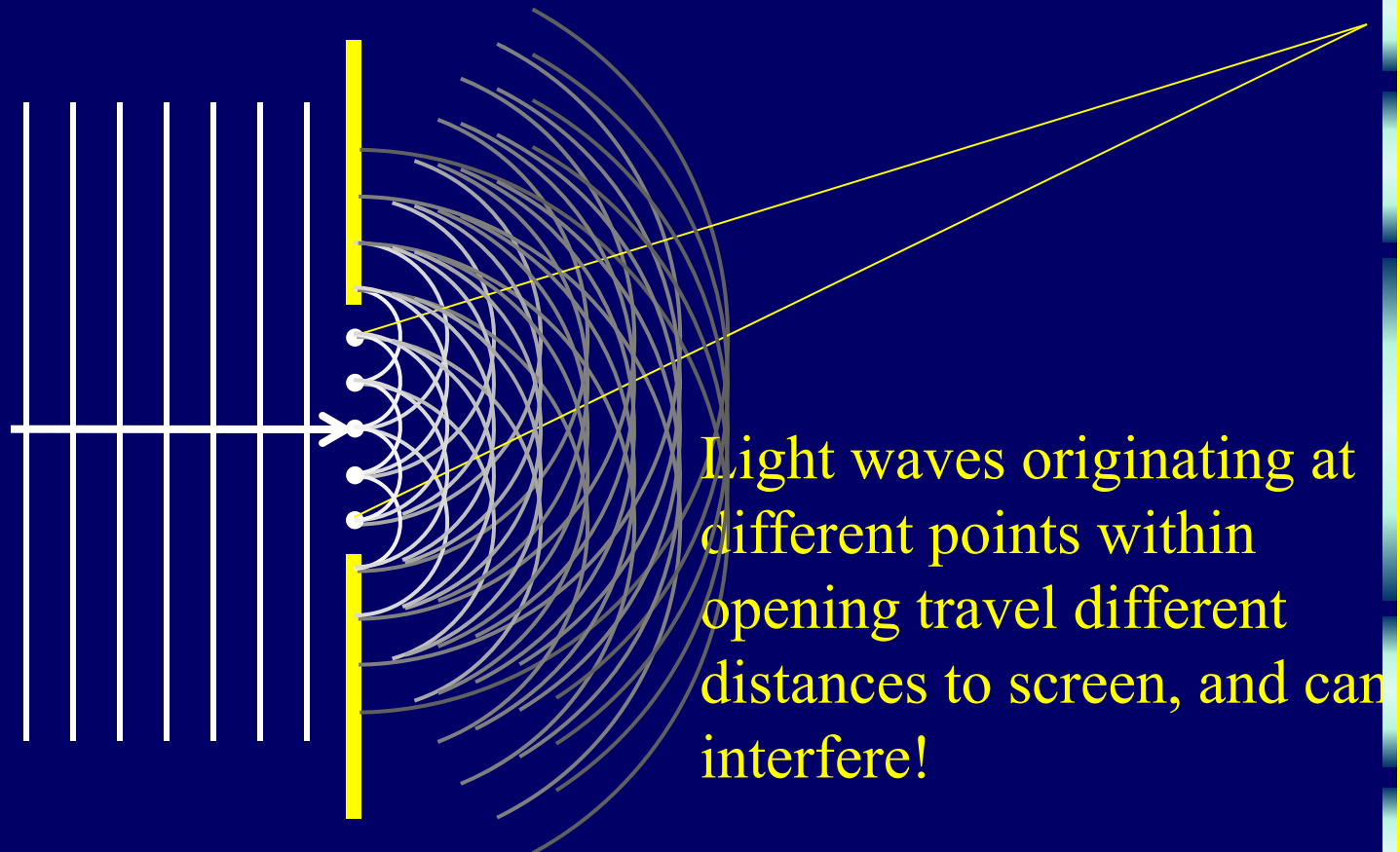
Monochromatic light travels through a screen with opening



**This is not what is actually seen!**

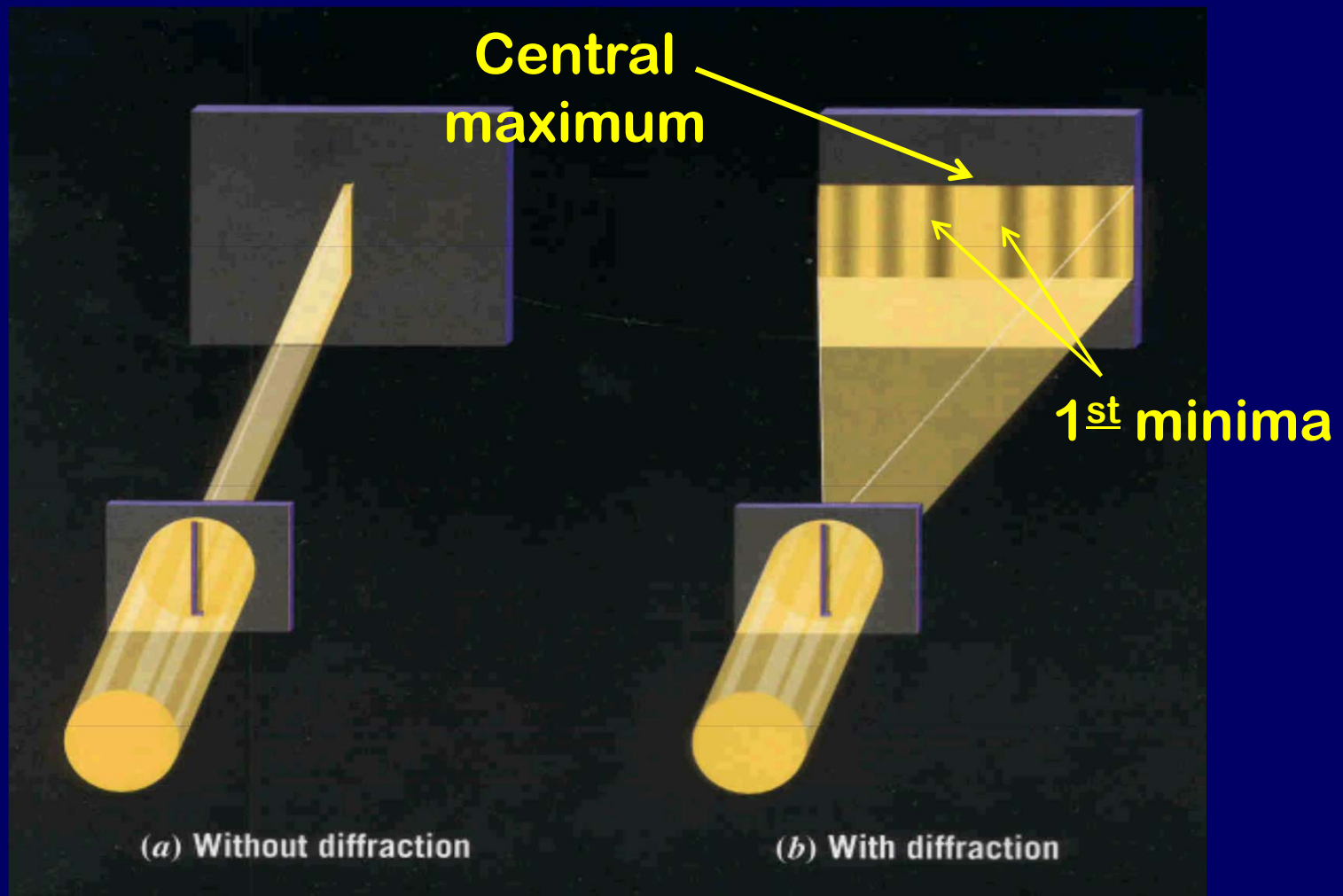
# Diffraction/Huygens' principle

Huygens: Every point on a wave front acts as a source of tiny wavelets that move forward.



Light waves originating at different points within opening travel different distances to screen, and can interfere!

We will see maxima and minima on the wall!



Next lecture: quantitative single-slit diffraction

# Recap

- **Interference: Coherent waves**
  - Full wavelength difference = Constructive
  - $\frac{1}{2}$  wavelength difference = Destructive
- **Multiple Slits**
  - Constructive  $d \sin(\theta) = m \lambda$  ( $m=1,2,3\dots$ )
  - Destructive  $d \sin(\theta) = (m + 1/2) \lambda$  **2 slit only**
  - More slits = brighter max, darker mins
- **Single Slit Interference**