

# ***Your questions/comments***

**IMPORTANT ANNOUNCEMENT:** Exam 2 coming up on Oct. 23, 2014!  
Will cover Lect. 6 (circuit elements) – Lect. 12 (currents & magnetism)  
Review session Oct. 21, 2014 from 6-8pm (room TBD)

“Can you put together some type of review sheet that displays the right hand rule for... everything? Thanks! Hope the lecture clears up the topic. Very cool stuff nonetheless.” *I will do*

“Dude.....What the flux?”

“SO CONFUSED WITH THE SLIDING BAR AND MAGNETIC FLUX!!”

“These concepts are very hard. I am not getting a lot of concepts. Please review these checkpoints.”

“Please go over Lenz's law! This is my first time hearing about Lenz's law and magnetic flux. Thanks!”



# Phys 102 – Lecture 13

Motional EMF & Lenz' law

# ***Physics 102 recently***

## Basic principles of magnetism

- Lecture 10 – magnetic fields & forces
- Lecture 11 – magnetic dipoles & current loops
- Lecture 12 – currents & magnetic fields

## Connection between electricity & magnetism

- Lecture 13 – motional EMF & Lenz' law
- Lecture 14 – Faraday's law of induction
- Lecture 15 – electromagnetic waves

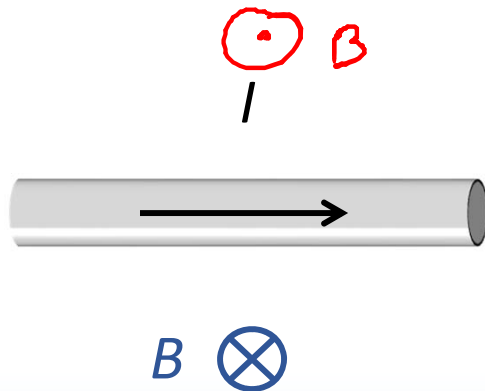
# *Today we will...*

- Learn how electric fields are created from...
  - Motion in magnetic fields (“motional EMF”)
  - Changing magnetic fields
- Learn Lenz’ law: principle unifying electricity and magnetism
- Apply these concepts:
  - Magnetoreception
  - Electrical generators & hybrid cars



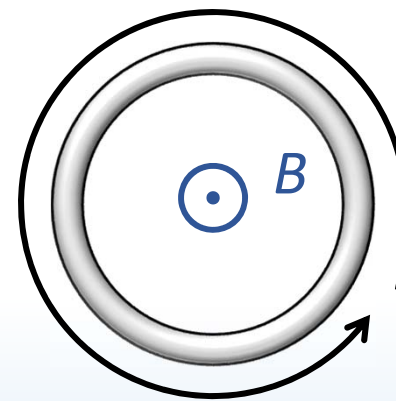
# ACT: Quick review!

In which direction does the  $B$  field point?



Below the wire:

- A. Into the page
- B. Out of the page
- C. Up
- D. Down

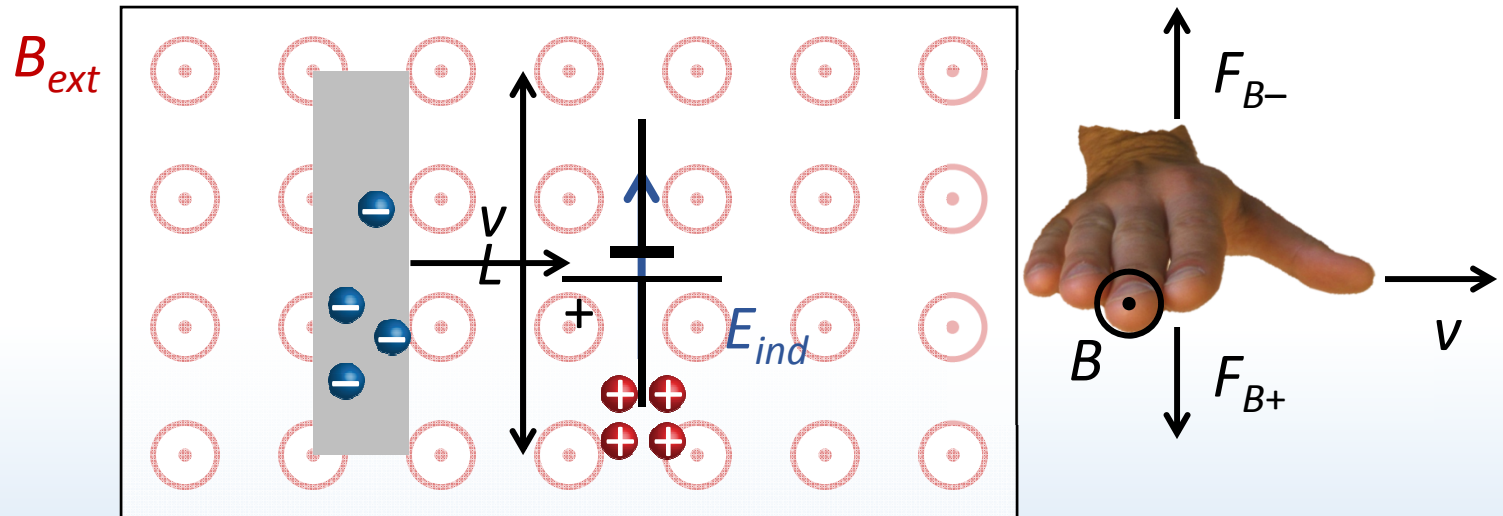


Inside the loop:

- A. Into the page
- B. Out of the page
- C. Up
- D. Down

# CheckPoint 1: Moving bar

A conducting bar moves in a uniform external  $B$  field at speed  $v$



47%

Magnetic force pushes – electrons to top, leaves + charge at bottom of bar

Separated + and – charge induces  $E$  field &  $\Delta V$

At equilibrium, forces must sum to zero

$$F_B = qvB_{ext} = F_E = qE_{ind}$$

**Moving bar acts like a battery!**  
**Motional EMF**

# ***Magnetoreception in sharks***

Sharks can sense changes in magnetic fields

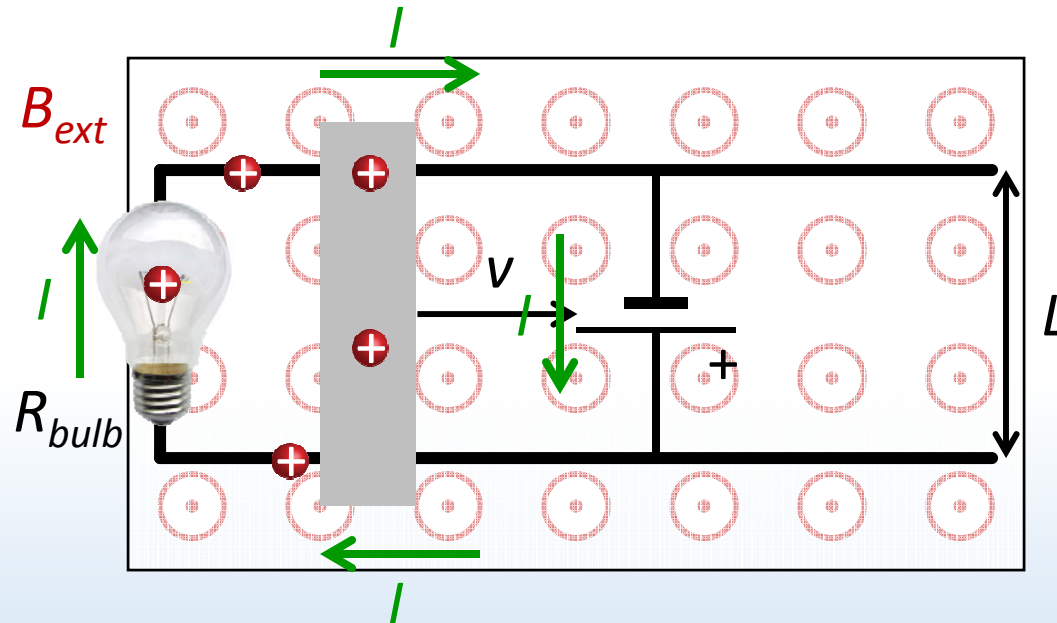


Sharks do not have magnetic organelles like magnetotactic bacteria, but they do have “ampullae of Lorenzini”, which sense  $E$  field

Model of magnetoreception in sharks: motional EMF from moving in  $B$  field generates  $E$  field detected by ampullae

# Motional EMF

Bar slides with speed  $v$  on a conducting track in a uniform  $B$  field



Can moving bar drive current around the circuit?

+ charges in moving bar experience force down  
Electrical current induced clockwise!

$$\varepsilon = vB_{ext}L \quad I = \frac{vB_{ext}L}{R_{bulb}}$$

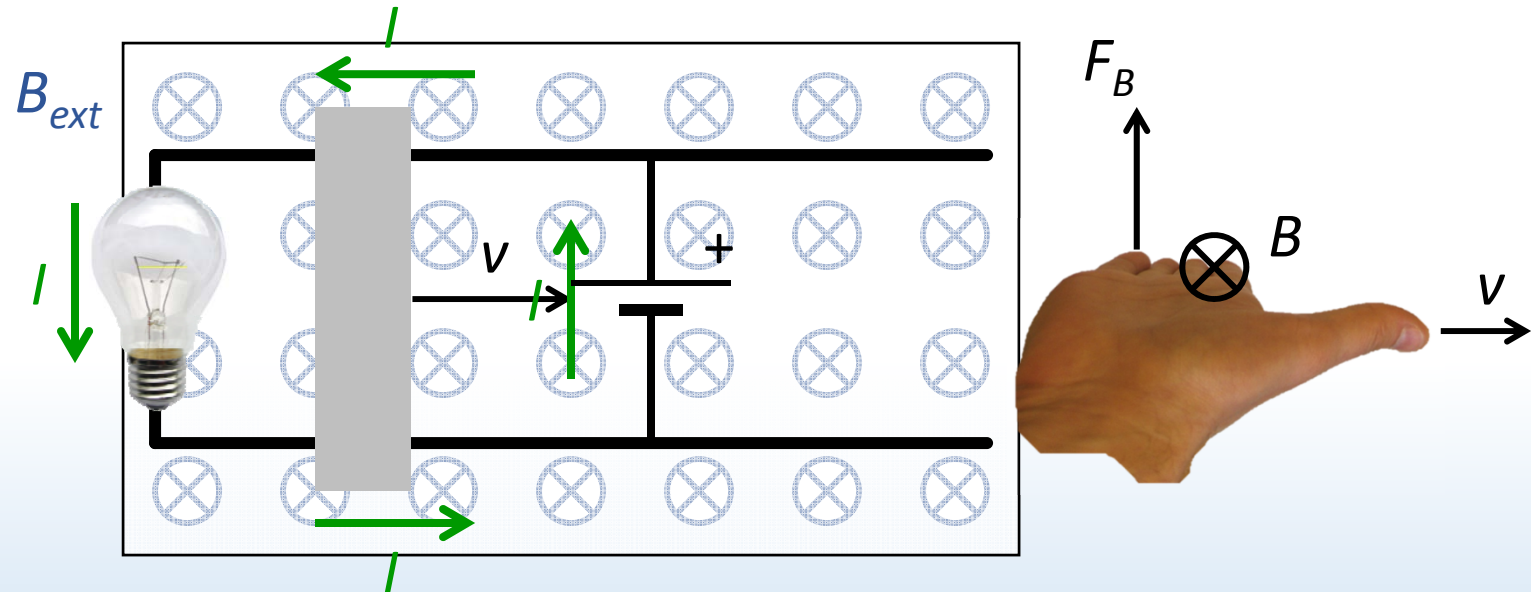
(Recall that  $e^-$  actually move, opposite current)





## ACT: CheckPoint 2.1

The conducting bar moves to the right in the opposite  $B$  field



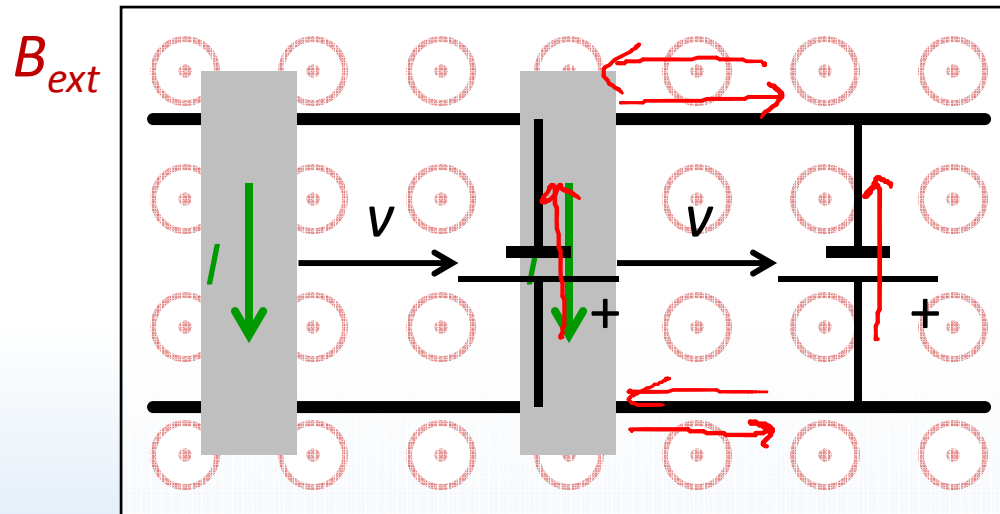
Which way does the current flow?

- A. Clockwise 43%
- B. Counterclockwise 52%**
- C. The current is zero 5%



## ***ACT: Two metal bars***

Circuit now has two metal bars moving right at the same speed  $v$



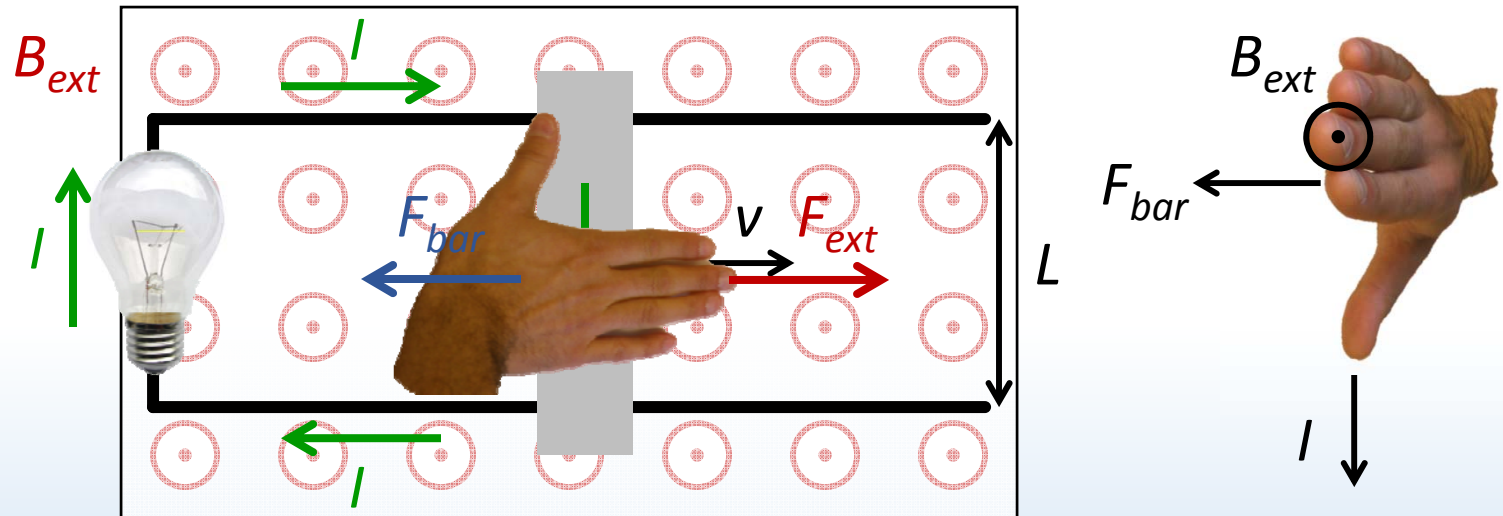
Which way does the current flow?

- A. Clockwise
- B. Counterclockwise
- C. The current is zero

Both bars generate equal current  $I$  down  
& opposite EMFs. Net current is zero

# Motional EMF and force

Where does the energy come from to generate electricity?



Moving bar carries current, so  $B$  field exerts a force  $F_{bar}$

$$F_{bar} = ILB_{ext} \sin \theta$$

$F_{bar}$  opposes  $v$ , so bar decelerates

To maintain constant  $v$ , you must provide external force  $F_{ext}$  opposing  $F_{bar}$

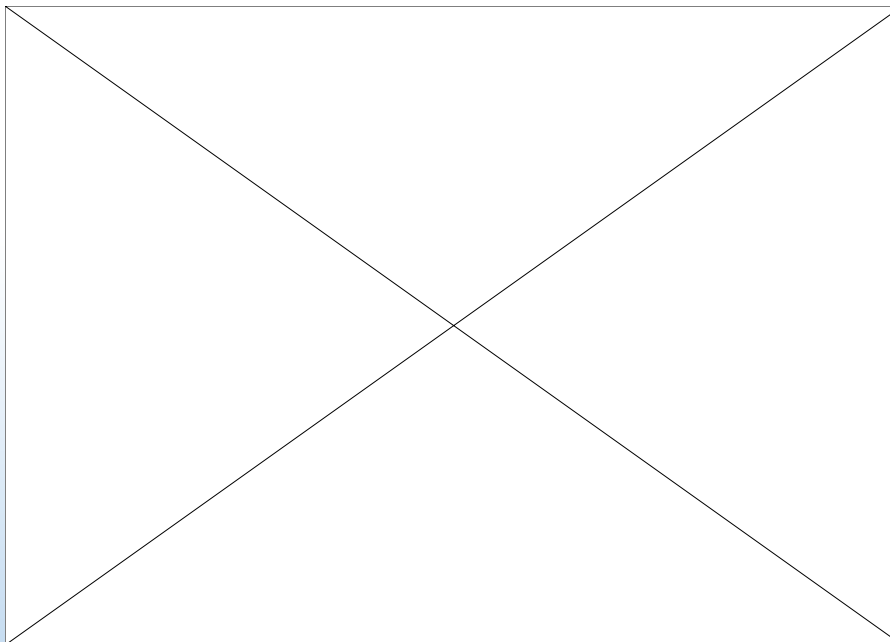
$F_{ext}$  does the work to generate electrical energy

Note:  $F_{bar}$  is NOT  $F_B$  which drives current around loop

# ***Electrical generators***

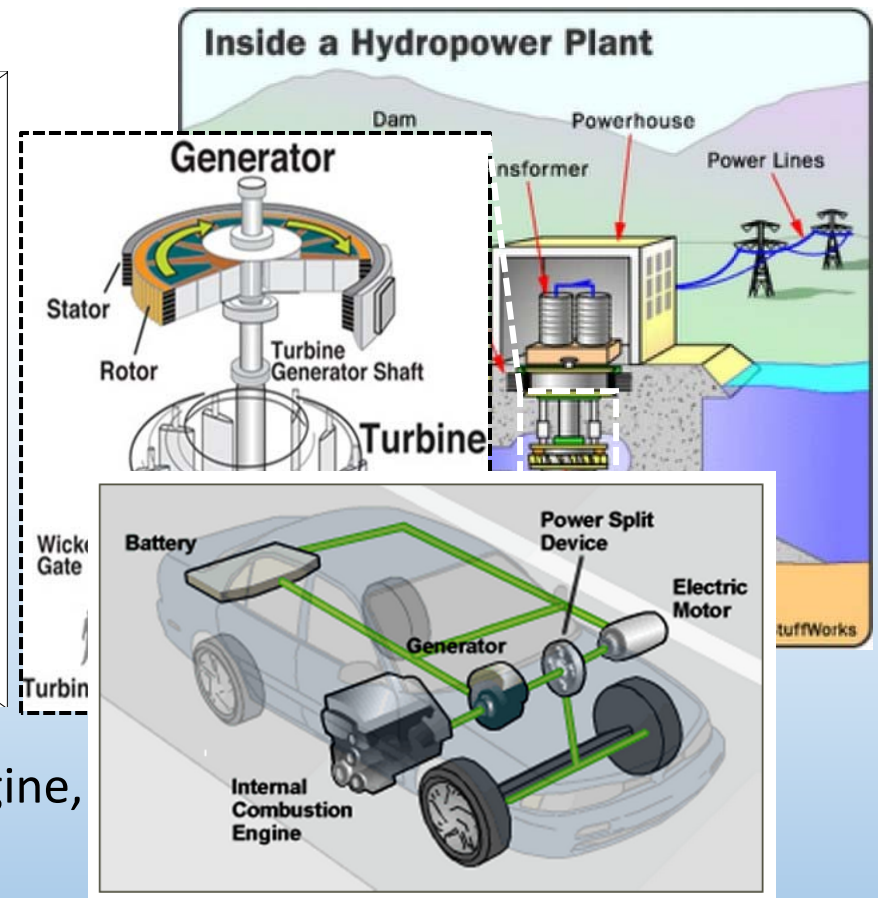
Motional EMF is the basis for modern electrical generation

Instead of sliding bar, use spinning loop in  $B$  field



External torque (from turbine, gas engine,

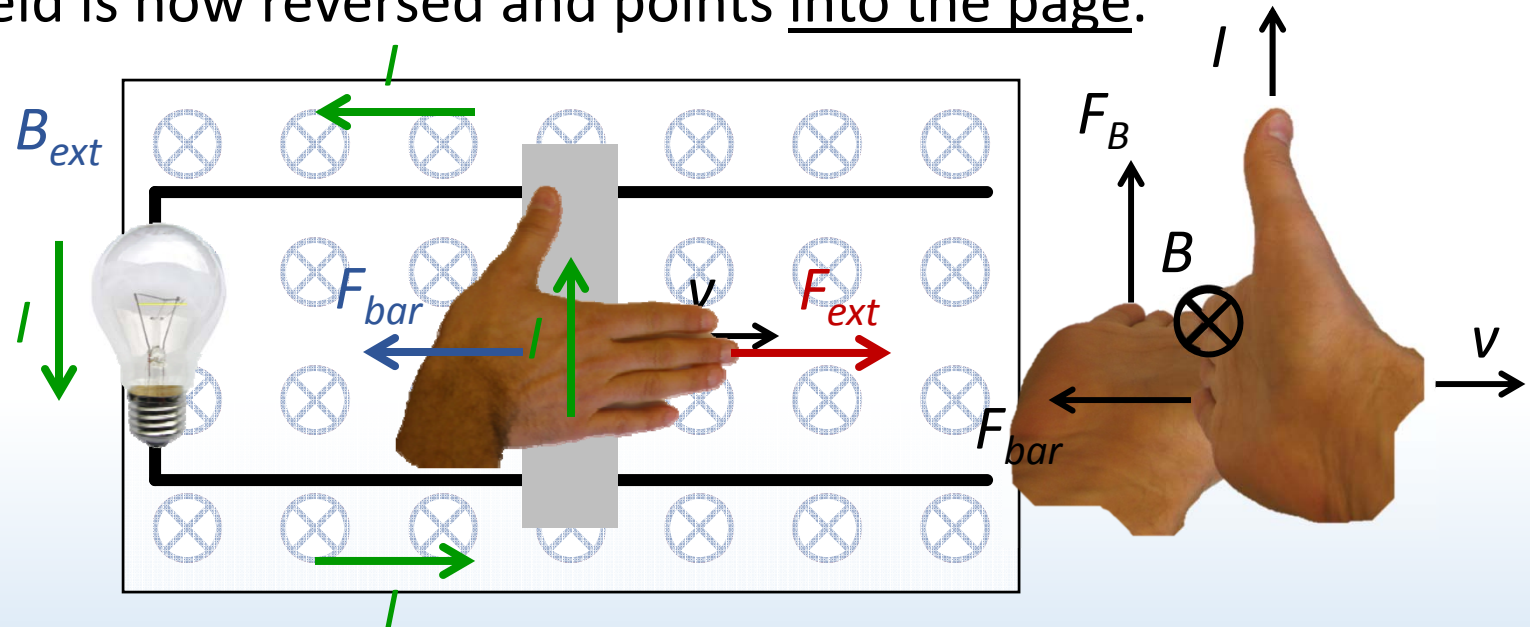
DEMO





## ACT: CheckPoint 2.2

The  $B$  field is now reversed and points into the page.



To keep the bar moving at the same speed, the hand must supply:

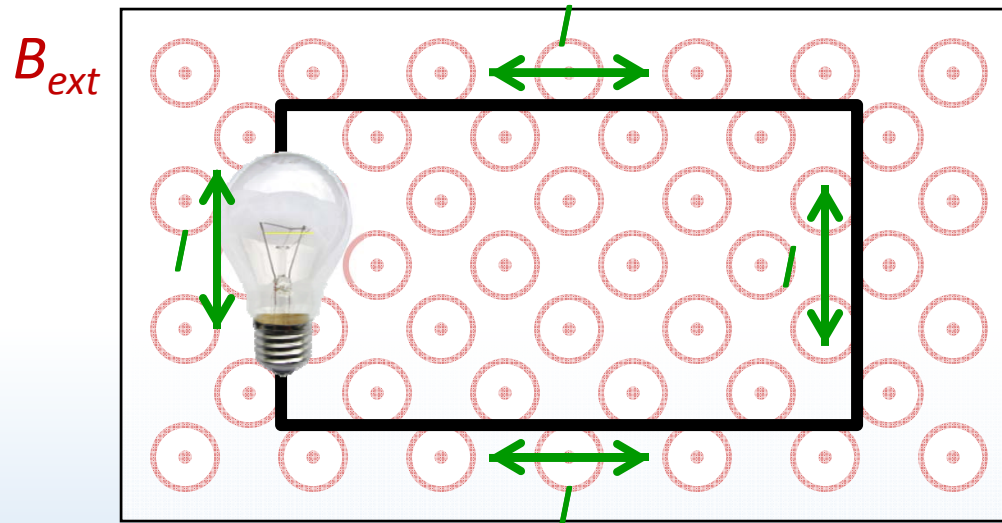
- 58% A. A force to the right
- 34% B. A force to the left
- 8% C. No force, the bar slides by inertia

Current flows counterclockwise  
(see previous ACT)

$F_{bar}$  still opposes  $v$ !  $F_{bar} = ILB_{ext}$

# Changing $B$ field

Now loop is fixed, but  $B$  field changes



If  $B_{ext}$  increases, current  $I$  flows clockwise

If  $B_{ext}$  decreases, current  $I$  flows counterclockwise

If  $B_{ext}$  is constant, no current flows

} Lenz's law

What is changing here and in previous cases? Magnetic flux  $\Phi$ !

# Magnetic flux

Flux “counts” number of  $B$  field lines passing through a loop

$$\Phi \equiv BA \cos \varphi$$

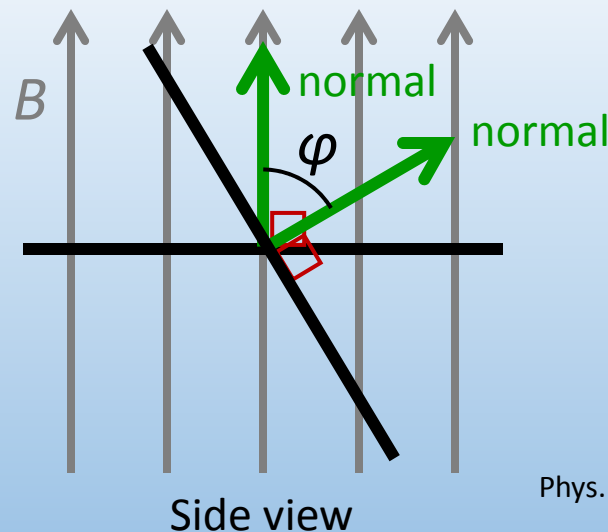
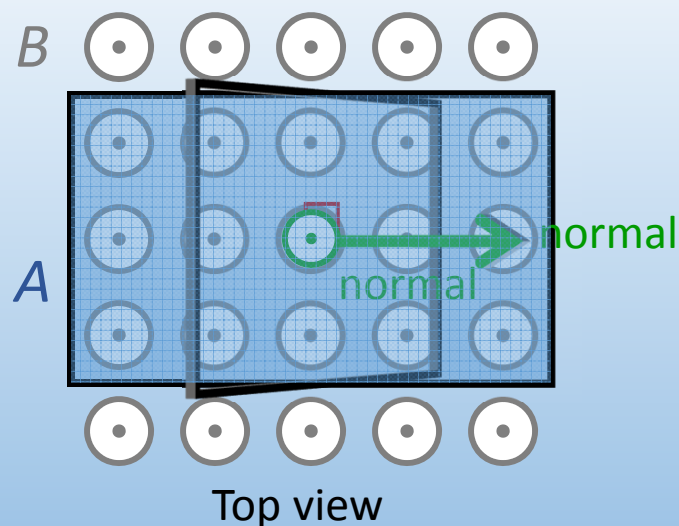
$B$  field in loop

Area inside loop filled with  $B$  field

Angle between normal vector and  $B$  field

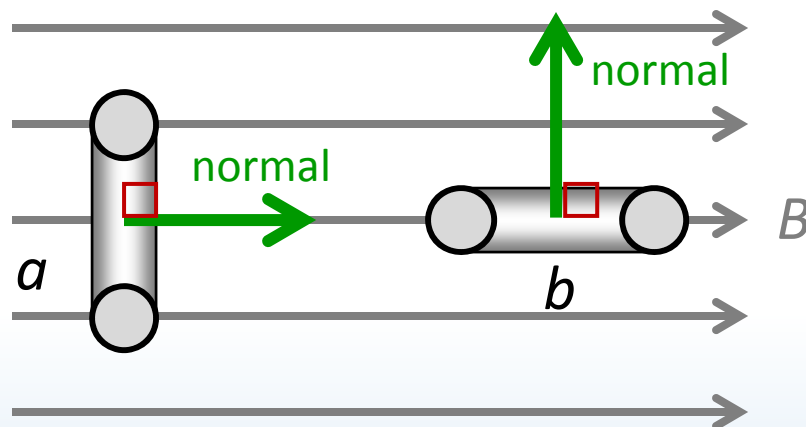
Unit: Wb (“Weber”)   
  $1 \text{ Wb} = 1 \text{ T} \cdot \text{m}^2$

Angle  $\varphi$  affects how many  $B$  field lines pass through loop



# CheckPoint 3.1

Compare the flux through loops  $a$  and  $b$



$$\Phi_a = BA \cos(0) = BA \quad \Phi_b = BA \cos(90) = 0$$

A.  $\Phi_a > \Phi_b$

56%

B.  $\Phi_a < \Phi_b$

17%

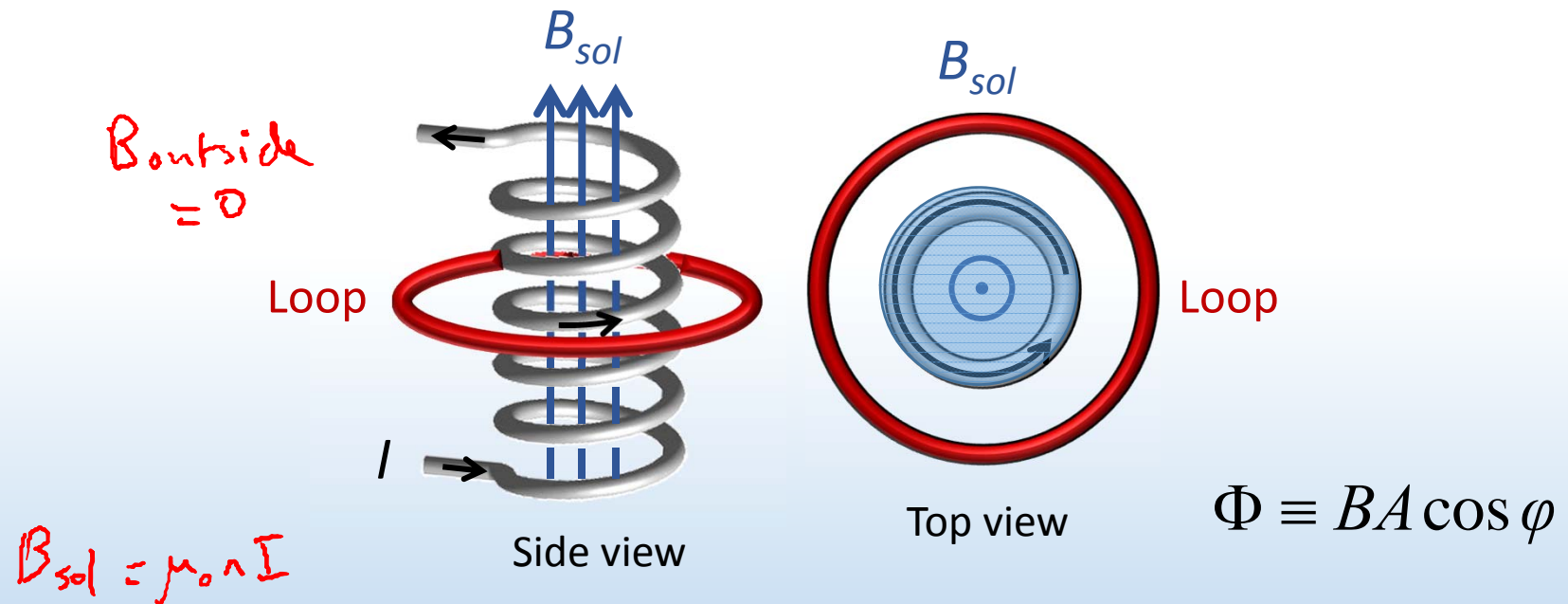
C.  $\Phi_a = \Phi_b$

27%



# Magnetic flux practice

A solenoid generating a  $B$  field is placed inside a conducting loop. What happens to the flux  $\Phi$  through the loop when...



The area of the solenoid increases?

$\Phi$  increases

The current in the solenoid increases?

$\Phi$  increases

The area of the loop increases?

$\Phi$  remains constant

# Lenz's law

Induced EMF  $\varepsilon$  opposes change in flux  $\Phi$

If  $\Phi$  increases:

$\varepsilon$  generates new  $B$  field  
*opposite* external  $B$  field

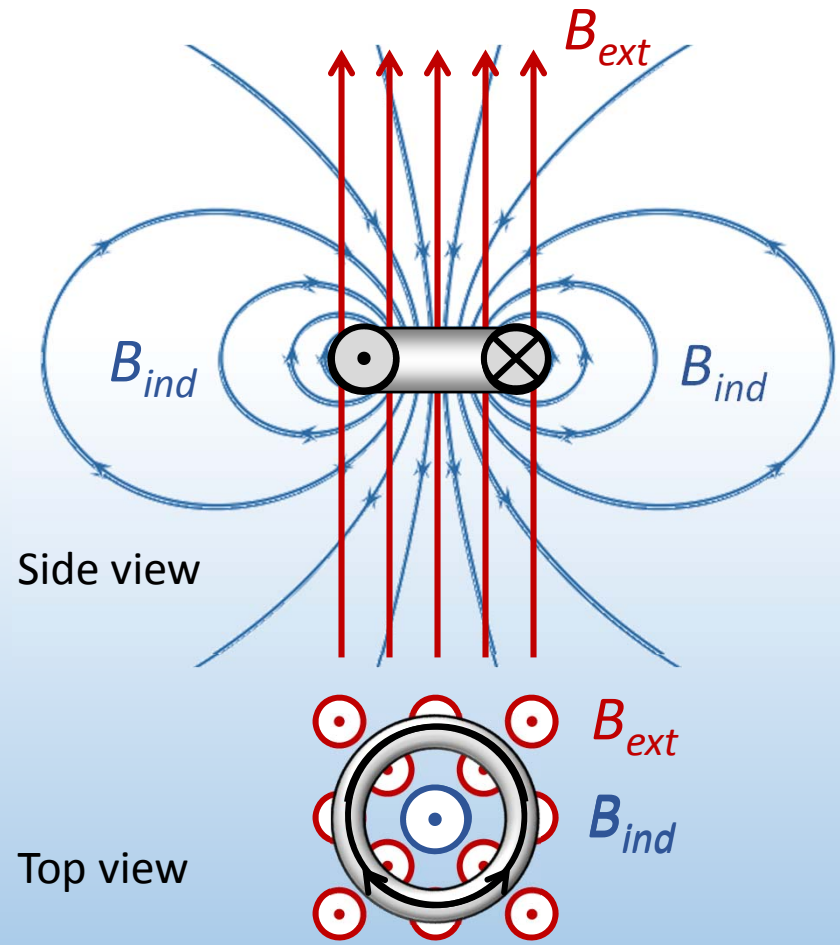
If  $\Phi$  decreases:

$\varepsilon$  generates new  $B$  field  
*along* external  $B$  field

If  $\Phi$  is constant:

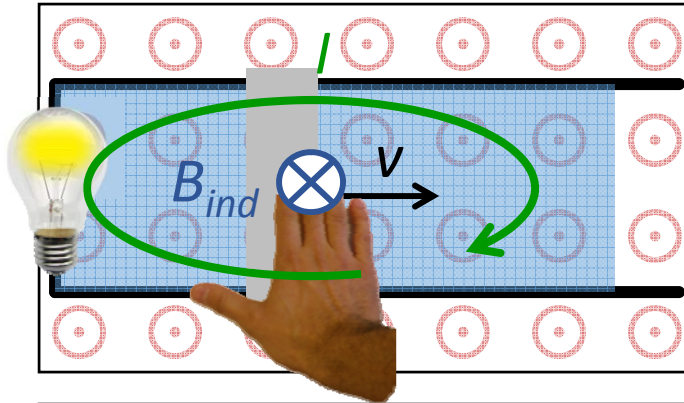
$\varepsilon$  is zero

One principle explains all  
the previous examples!



# Lenz's law: changing loop area

EX 1

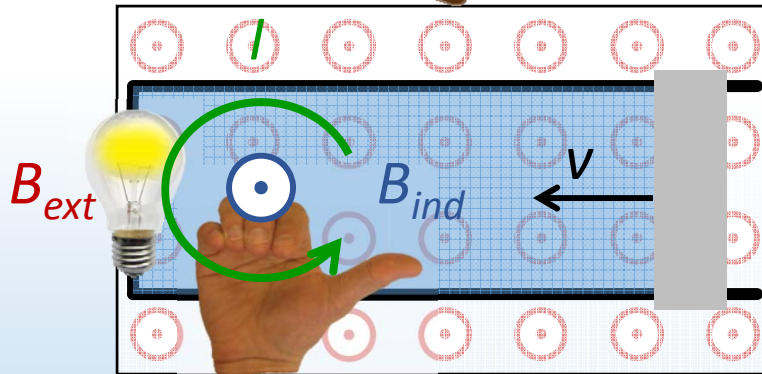


$\epsilon$  opposes change in flux  $\Phi$

A &  $\Phi$  increases

$\epsilon$  generates  $B_{ind}$  opposite  $B_{ext}$

EX 2

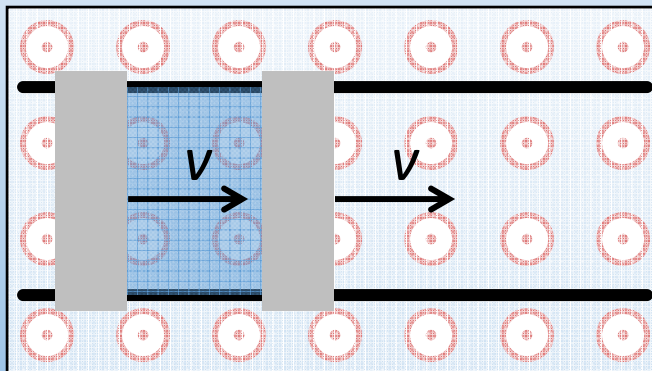


A &  $\Phi$  decreases

$\epsilon$  generates  $B_{ind}$  along  $B_{ext}$

**Same answers as before!**

EX 3



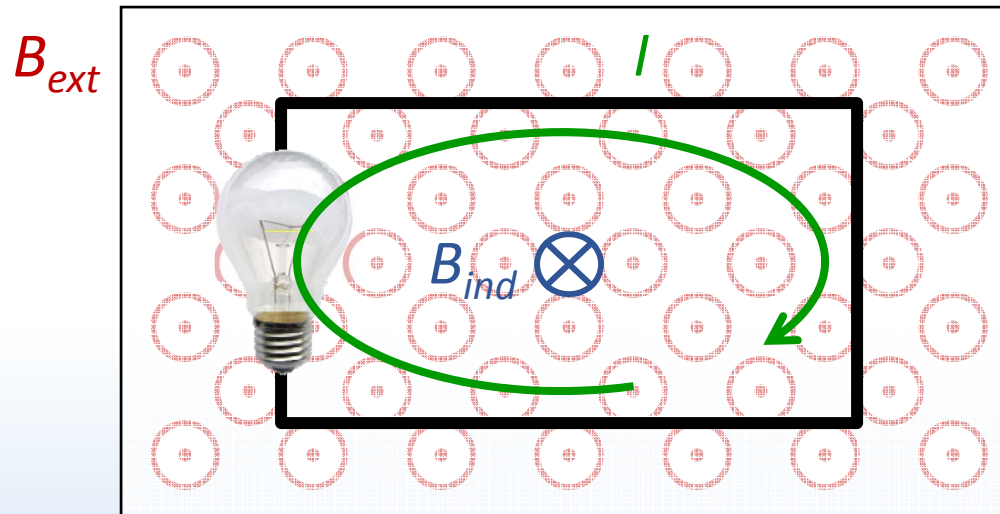
A &  $\Phi$  remains constant

$\epsilon$  is zero



# ***ACT: Lenz' law: changing $B$ field***

A loop is placed in a uniform, increasing  $B$  field



In which direction does the induced  $B$  field from the loop point?

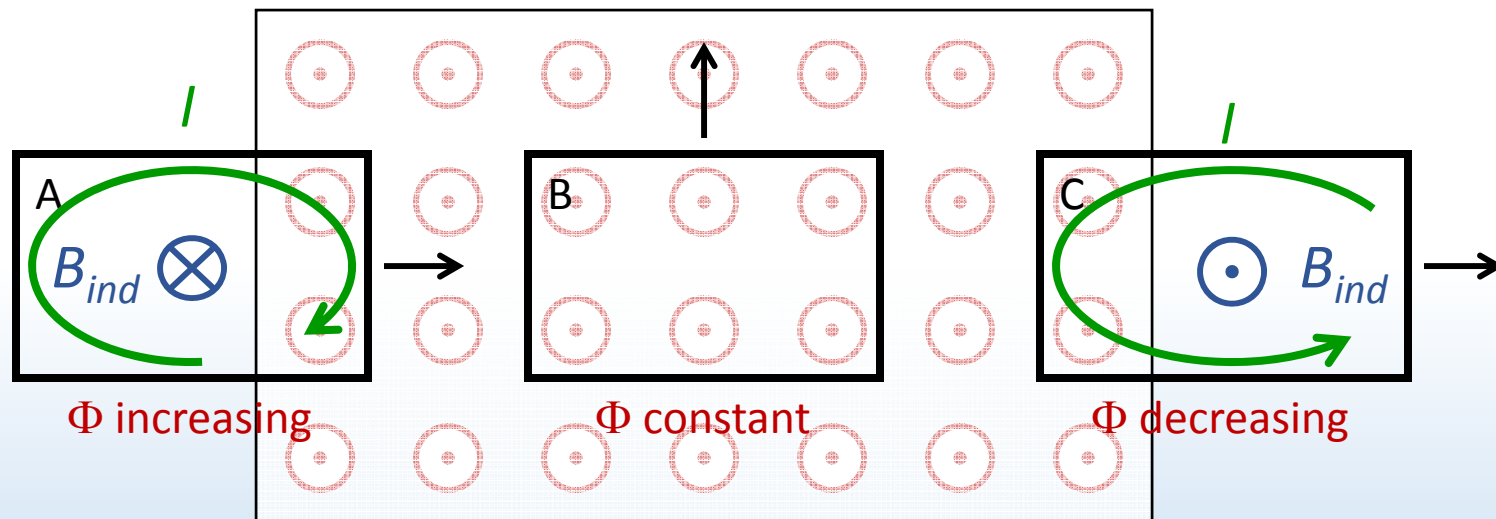
- A. Into the page
- B. Out of the page
- C. There is no induced  $B$  field

$\Phi$  is increasing, so  $B_{ind}$  must point in opposite direction. By RHR current must be clockwise.



# ACT: moving loops

Three loops are moving in a region containing a uniform  $B$  field. The field is zero everywhere outside.



In which loop does current flow counterclockwise at the instant shown?

A. Loop A

B. Loop B

C. Loop C

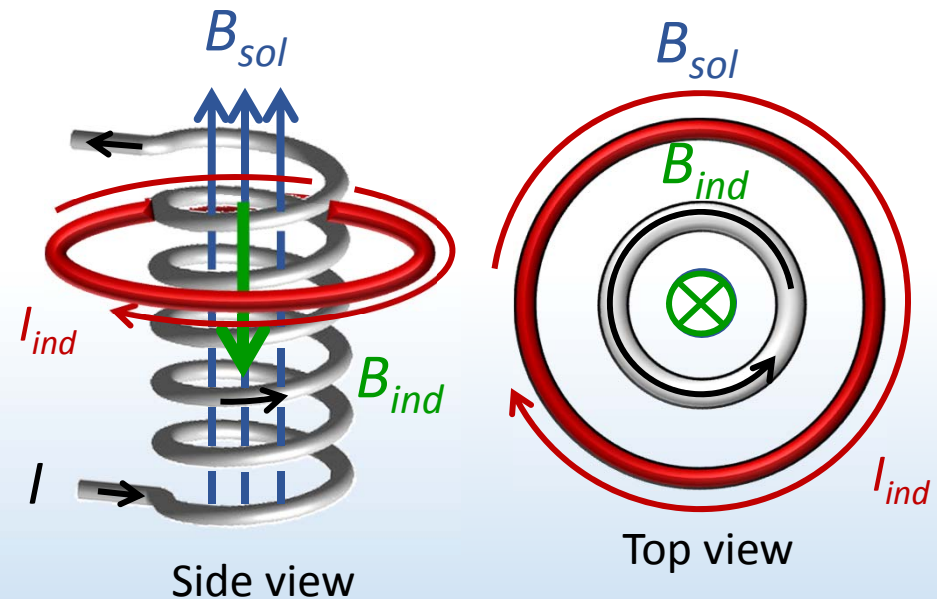
$\epsilon$  opposes change in flux  $\Phi$



# ACT: Solenoid & loop

A solenoid is driven by an increasing current. A loop of wire is placed around it. In which direction does current in the loop flow?

- A. Clockwise
- B. Counterclockwise
- C. The current is zero



$B_{sol}$  points up,  $\Phi$  through loop increasing  
 $\epsilon$  creates opposing  $B$  field ( $B_{ind}$  points down)  
Induced loop current  $I_{ind}$  must be clockwise

# Induction cannon

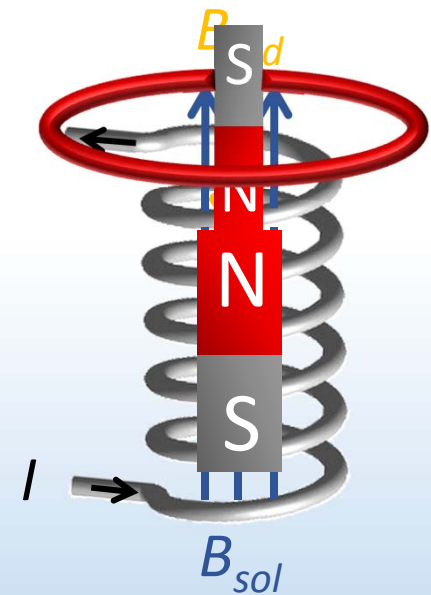
A solenoid is driven by an increasing current. A loop of wire is placed around it.

Current loop and solenoid behave like magnetic dipoles

Opposite currents = opposite polarities

Recall Lect. 11

Like poles repel, so loop shoots up!



What happens if loop is broken?

What happens if loop has more/less resistance?

DEMO

# *Summary of today's lecture*

- Electric fields are created from
  - Motion in magnetic fields (“motional EMF”)
  - Changing magnetic fields
- Lenz’ Law: EMF  $\varepsilon$  opposes change in flux  $\Phi$

$\varepsilon$  does NOT oppose  $\Phi$   
 $\varepsilon$  opposes change in  $\Phi$

Lenz’ law gives direction of EMF

Faraday’s law gives us magnitude of EMF (next lecture!)