

Name: _____ DISC: _____ Score: _____ / 20

Instructions:

- Do your own work.
- Answer the questions below in the space provided.
- Make sure you show all your work and any equations that you use.
- Please place a box around your answers.
- Remember to give the correct units with all numerical answers

Q1

Q2

Q3

Q4

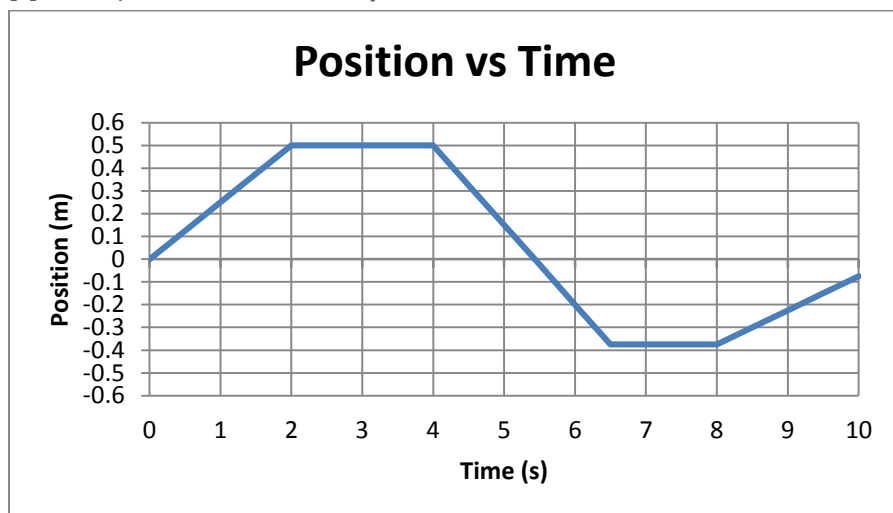
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1. You observe a cart moving in a straight line and plot its position versus time as shown in the graph (**Lecture 3 pp. 5-7; Discussion 3-2**):



Speeds: 1 pt each

- a. Using the graph fill in the following table of velocities:

TIME	VELOCITY
From 0 s to 2 s	$\frac{(0.5 - 0)m}{(2 - 0)s} = \frac{0.5 m}{2 s} = 0.25 \frac{m}{s}$
From 2 s to 4 s	$\frac{(0.5 - 0.5)m}{(4 - 2)s} = \frac{0.0 m}{2 s} = 0 \frac{m}{s}$
From 4 s to 6.5 s	$\frac{(-0.375 - 0.5)m}{(6.5 - 4)s} = \frac{-0.875 m}{2.5 s} = -0.35 \frac{m}{s}$
From 6.5 s to 8 s	$\frac{(-0.375 - (-0.375))m}{(8 - 6.5)s} = \frac{0 m}{1.5 s} = 0 \frac{m}{s}$
From 8 s to 10 s	$\frac{(-0.375 - (-0.075))m}{(10 - 8)s} = \frac{-0.36 m}{2 s} = -0.15 \frac{m}{s}$

Remember, the velocity is the *slope* of a position vs. time graph. We can calculate the velocity between each time point on the graph using $v = \Delta x / \Delta t$.

- b. What is the average speed of the cart?

The average speed of the cart can be calculated by taking the sum of the speeds and dividing by the total number of speeds measured:

$$v = \frac{[0.25 + 0 + 0.35 + 0 + 0.15] \text{ m/s}}{5} = 0.15 \frac{\text{m}}{\text{s}}.$$

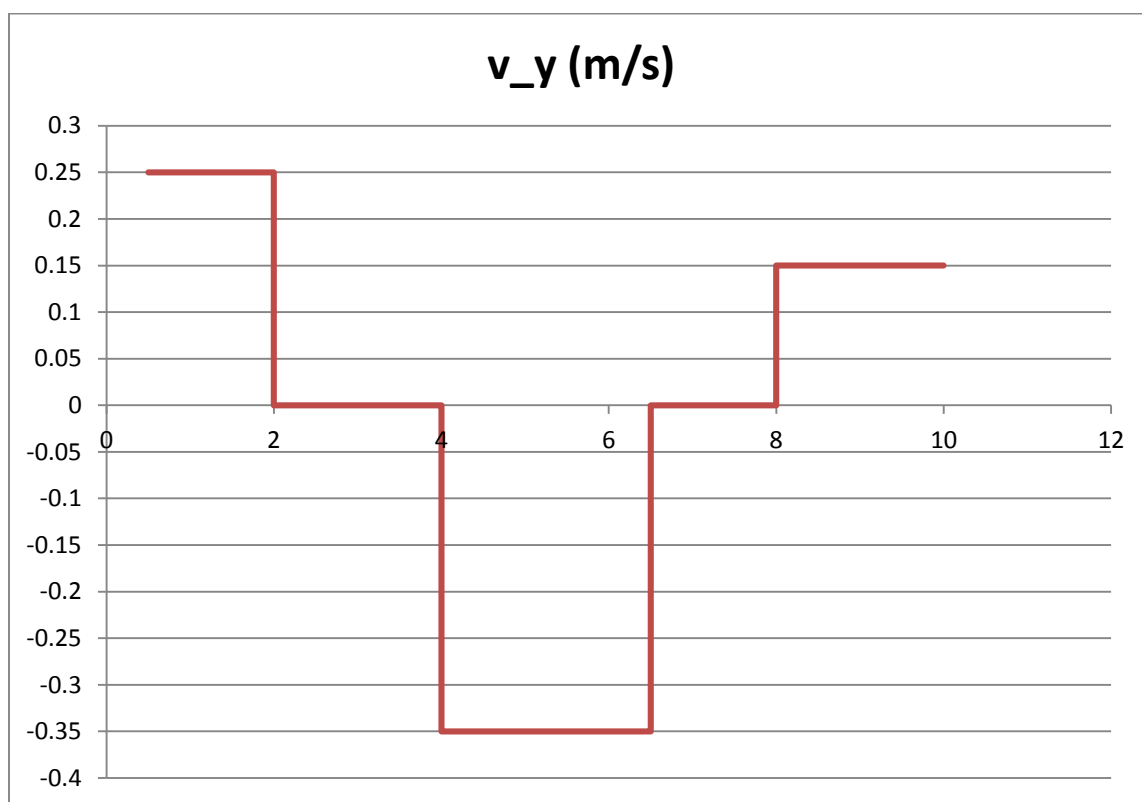
Full credit to be given for any other correct averaging technique including:

The time-weighted average:

$$v = \frac{\left[0.25 \frac{\text{m}}{\text{s}} \times 2 \text{ s} + 0 \frac{\text{m}}{\text{s}} \times 2 \text{ s} + 0.35 \frac{\text{m}}{\text{s}} \times 2.5 \text{ s} + 0 \frac{\text{m}}{\text{s}} \times 1.5 \text{ s} + 0.15 \frac{\text{m}}{\text{s}} \times 2 \text{ s}\right]}{10 \text{ s}} = 0.1675 \frac{\text{m}}{\text{s}}.$$

Simple point averages (i.e. picked a couple of points and took the average).

- c. Sketch the *velocity versus time* for the cart:



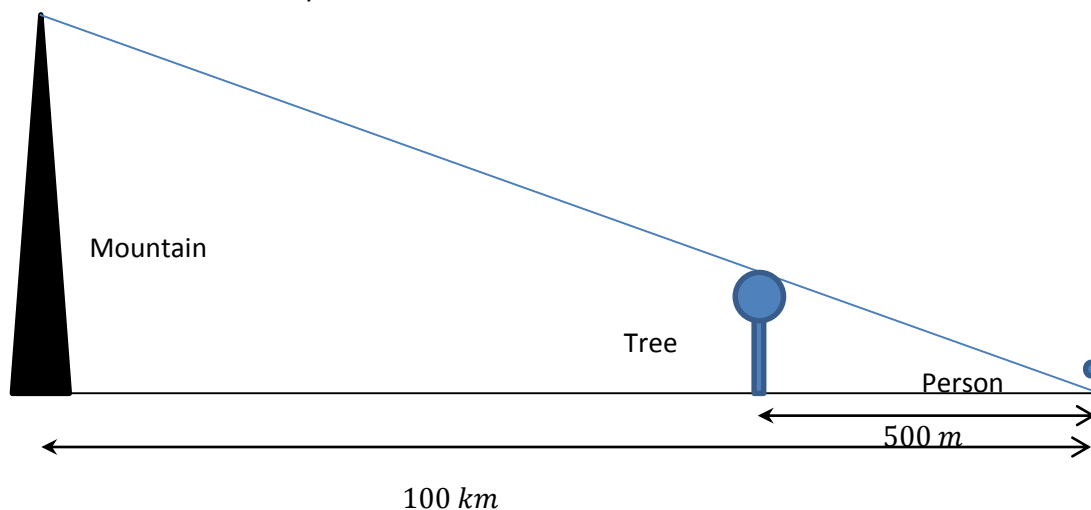
Average Speed (2 pts):

Sketch (3 pts):

2. You want to determine the height of a mountain 100 km from your current position. You look around and notice that about 500 m away from you is a tall tree. You look up and notice that the peak of the mountain and the top of the tree are aligned. **(Homework 2)**

- a. Make a sketch of this system. Remember to label all features.

Sketch (3 pts):



Description (2 pts):

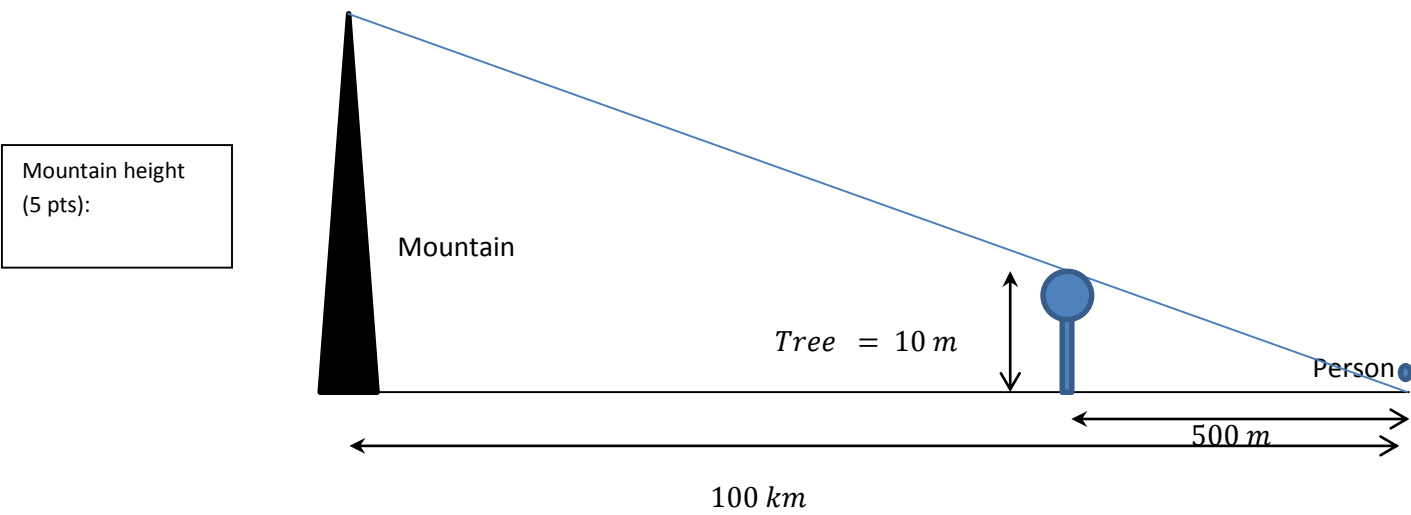
- b. Since you cannot measure the height of the mountain directly, describe the technique or techniques you would use to determine the height of the mountain.

The easiest way to solve this problem is to triangulate using similar triangles, if you know the height of the tree.

Otherwise if you can measure the angle (using an astrolabe or protractor, for example) at which you view the mountain and the tree-top simultaneously, you can use your trig functions (you know how far the tree is from you and how far the mountain is from you) to calculate the height of the mountain.

- c. The tree is 10 m tall. Find the height of the mountain.

Given this new information, the method of similar triangles is the easiest technique:



$$\frac{\text{Mountain}}{100 \text{ km}} = \frac{10 \text{ m}}{500 \text{ m}} = \frac{1}{50}$$
$$\text{Mountain} = \frac{100 \text{ km}}{50} = 2 \text{ km}$$