# Simultaneous Localization of Multiple Jammers and Receivers Using Probability Hypothesis Density

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#### **Time Critical Applications**



#### Timing sources for Power Substations

Monitoring power substations via **Global Positioning Systems** Phasor Measurement Units (PMUs) PMU 10 H-M PMU PMU Han soften PMU PMU PMU min min PMU PMU PMU Precise Time Protocol (PTP) Clocks: TCXO, Atomic, XCXO t1 Pdelay Req t2 Clock A Clock B Pdelay Resp t3 t4 Pdelay Resp Follow Up delay = (t2-t1+t4-t3)/2

#### GPS Timing for PMUs



#### **Advantages**

Global coverage

Freely available

 $\mu s$ -level accurate global time

#### **Disadvantages**

Low signal power

Unencrypted structure

Vulnerable to attacks

#### Outline

#### **Background on GPS and Jamming Attacks**

Simultaneous Localization of Multiple Jammers and Receivers Experimental Verification and Validation

Summary



## Traditional GPS Algorithm

- Methodology
  - Trilateration with  $\geq 4$  satellites
  - Track carrier frequency and code phase
- Inputs
  - Center: 3D satellite position
  - Radius: Pseudoranges
- Unknowns to be estimated:
  - 3D position, Clock bias

By computing clock bias, we can estimate UTC time with satellite atomic clock level accuracy



#### Trilateration technique



[Larson GPS Research Group]

# What is GPS Jamming?

#### High powered signals transmitted in GPS frequency band



Jamming: Makes timing unavailable for PMUs

#### Authentic conditions



#### **GPS** Jamming Incidents

- Around 80 GPS jamming incidents between 2013 2016 [1]
- Few notable ones:
  - San Diego harbor, 2007 for 3 days [2]
  - Over 1000 planes, 250 ships in South Korea, 2012 for 16 days [3]
  - London Stock Exchange, 2012 everyday 10 mins [3]
  - Newark Liberty International Airport, 2013 2 months to track [1]
  - Cairo airport, 2016 [4]

Increasing number of GPS jamming incidents due to the ease of operation and low-cost availability

[1] Aviation today 01/31/2017

[2] GPS world 02/2014

[3] The economist "GPS jamming, Out of Sight" 07/2013

[4] Flight service bureau 05/24/2017

### Multiple jammers

- Increasing risk due of low cost jammers  $\sim$ \$50-100
- Challenges due to multiple jammers:
  - Presence of unknown number of jammers
  - Unknown contribution of each jammer at receiver
  - Increase in complexity of localization
- Existing GPS anti-jamming techniques
  - Directional antenna, time difference of arrival and so on
  - Address single jammer scenario
  - Mostly don't estimate receiver Position, Velocity and Time (PVT)



#### Our Objectives

- Locate multiple jammers instead of one
- Improve the robustness of the Position, Velocity and Time (PVT) solution of the receivers experiencing jamming



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### SLMR: Our Approach

- Multiple receivers
  - Geographical diversity
  - Variation in the received GPS signal power
- Probability Hypothesis Density (PHD) Filter [5]
  - Estimation of unknown number of jammers
- Inspired from Simultaneous Localization and Mapping (SLAM) [5] for robotics
  - Robots: GPS receivers
  - Features: jammers
  - Graph optimization

[5] Vo and Ma, IEEE Transactions on Signal Processing, 2006[6] Cadena, et.al, IEEE Transactions on Robotics, 2016



19 Illinois power substations in nearby 3 cities over 12x8miles

#### SLMR: Our Architecture



#### Intuitive Explanation of PHD Filter



- Multiple jammers are observed via multi-modal Gaussian distributed peaks
- State and measurements modelled as Random Finite Sets
- Cardinality modeled as a random variable
- Non-linearity is due to received signal strength measurements

### Non-Linear Gaussian Mixture PHD Filter

 Propagate posterior intensity modeled as Gaussian Mixture

$$v_t = \sum w_t \mathbb{N}(x; \mu_t, \Sigma_t)$$

• Estimated number of jammers  $M_t = \sum \mathbb{I}(w_t > \text{Threshold})$ 



Multi-modal peaks modeled as Gaussian Mixture (GM)

 $\mu_t$ : mean  $\Sigma_t$ : covariance  $w_t$ : weight  $S_t$ : jammers-receivers distance Measurement Time update update of PHD of PHD based Based on mison survival detection and and birth measurements  $M_t, S_t$ Subgraph optimization

## SLMR: Graph Framework

- Bipartite graph framework
  - $M_t$  number of jammers  $\vec{y}$
  - L receivers  $\vec{\mathbf{x}}$
  - Receiver dynamics *u* (Ex: static, uniform velocity or IMU)
- Sub-graph optimization at time each instant
- Periodically, full-graph optimization to account for drifts

Sub-graph at  $t^{th}$  time instant



# SLMR: Graph Optimization

- Levenberg-Marquardt minimizer [7]
  - Initial constraints of receivers
  - Constraints from PHD Filter
  - Constraints from receiver dynamics
- After jamming detected, SLMR initialized as follows:
  - Non-jammed received GPS signal power at each receiver
  - Single jammer with the initial location at the centroid of receivers
  - Graph based on the initial constraints of receivers and jammer

#### Graph framework across time







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#### Timing Attack Setup



According to IEEE C37.118, max allowable phase angle error is  $0.573^{\circ}$  (~time error of 26.5 µs)

#### Effect of Jamming on Power Grid



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# **Experimental Setup**

- Three stationary simulated jammers
  - Transmit power 50.3 W
  - Sweep continuous attack with frequency
    2.5 kHz to 2.5 kHz
- Five moving GPS receivers
- GPS signals collected
  - Sampling rate 5*MHz*
  - Received power computed using  $\Delta T = 10ms$
- Post-processed using our python framework pyGNSS



#### SLMR: Localization Accuracy of Jammers



Number of unknown jammers converges to 3 and positioning error of jammers estimated to within 5 m accuracy

#### SLMR: Different Levels of Jamming



Under 12 *dB* and 18 *dB* added jamming, mean position error of all jammers is within 4.8 *m* and mean position error of all receivers is within 5.6 *m*.

#### Summary

- Demonstrated the impact of GPS jamming attack on the stability of the power grid
- Proposed our Simultaneous Localization of Multiple Jammers and Receivers (SLMR) algorithm
- Demonstrated successful localization of jammers with 5 m accuracy while simultaneously locating receivers with 6 m accuracy under various levels of jamming attack

#### Future work | DT-NAVFEST Jamming Event



#### Heatmap of jammer to signal ratio





Teams from the University of Illinois Champagne Urbana and Stanford University, Calif., were invited to the first-ever DT NAVFEST at Edwards Air Force Base, Calif., to test projects in a GPS degraded environment. (U.S. Air Force photo by Wei

Teams from the **University of Illinois Champaign Urbana** and Stanford University, CA were invited to the first-ever DT NAVFEST at Edwards Air Force Base, CA, to test projects in a GPS degraded environment (U.S. Air Force photo by Wei Lee) <sub>25</sub>

# Our Published Work

- Position-Information Aided Vector Tracking [Chou, Heng and Gao ION GNSS 2014]
- Multi-Receiver Position-Information Aided Vector Tracking [Chou, Ng and Gao ION ITM 2015]
- Advanced Multi-Receiver Position-Information Aided Vector Tracking [Chou, Ng and Gao ION GNSS+ 2015]
- Direct Time Estimation [Ng and Gao IEEE PLANS 2016]
- Multi-Receiver Direct Time Estimation for PMUs [Bhamidipati, Ng and Gao ION GNSS+2016]
- Spoofer Localization based Multi-Receiver Direct Time Estimation [Bhamidipati and Gao ION GNSS+2017]
- Improved Jamming Resilience using Position-Information Aided Vector Tracking [Bhamidipati and Gao ION GNSS 2017]
- Simultaneous Localization of Multiple Jammers and Receivers using Probability Hypothesis Density [Bhamidipati and Gao ION PLANS 2018]

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# Thank You

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