

A particle with spin $S=1$ has spin operators S_x and S_z represented by the 3×3 matrices:

QM Spring 07 B

$$S_z = \hbar \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}, S_x = \frac{\hbar}{\sqrt{2}} \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$$

- (a) Determine the 3×3 matrix representing the spin operator S_y for this spin 1 particle.
- (b) The spin state for this particle is generally represented by a column vector

$$\psi = \begin{pmatrix} a \\ b \\ c \end{pmatrix}$$

Determine a , b , and c such that the spin state ψ is normalized and corresponds to the maximum possible value of S_x .

- (c) Now, consider a magnetic field B pointing in the $+z$ direction. Assume that the spin 1 particle has a magnetic moment μ , and at $t=0$ is placed in the magnetic field such that its initial spin state is that given in part (b), i.e., it is polarized along the $+x$ direction. Find the spin state ψ at later times.
- (d) What is the probability that the spin state of the particle will be polarized along the $+x$ direction at a time later than $t=0$?

Useful information: For a general angular momentum state

$$|j, m\rangle, (J_x \pm iJ_y)|j, m\rangle = \hbar\sqrt{(j \mp m)(j \pm m + 1)}|j, m \pm 1\rangle$$