

Consider the following model of a diatomic molecule free to move in 3 dimensions.

The model is that two point-like particles of mass m are connected by a spring with spring constant k_s . The spring has equilibrium length l and remains perfectly linear.

Assume all velocities are small compared to the speed of light. The molecule is in thermal equilibrium with a reservoir at temperature T. Express your answers in terms of m, k_S, l, Boltzmann's constant k_B, T, and Planck's constant h.

- A) State an inequality that ensures that the classical thermal oscillations have little effect on the moment of inertia.
- B) Assuming that inequality (A) holds, what is the expectation value of the total thermal energy in the classical regime?
- C) State an inequality needed to ensure that classical statistical mechanics does indeed apply to the oscillations.
- D) For the regime of (C), estimate the dimensionless entropy, S/k_B due to oscillations.
- E) State an inequality needed to ensure that classical statistical mechanics does indeed apply to the rotations.
- F) For the regime of (E), estimate the dimensionless entropy due to rotations.