

**X-ray analysis:  
Mauro Sardela Jr.  
Advanced Materials Characterization Workshop  
AMC2019  
University of Illinois at Urbana-Champaign**

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**SPONSORS**

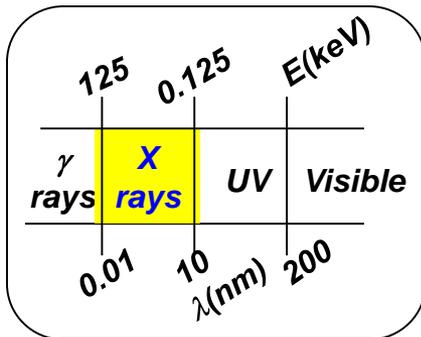
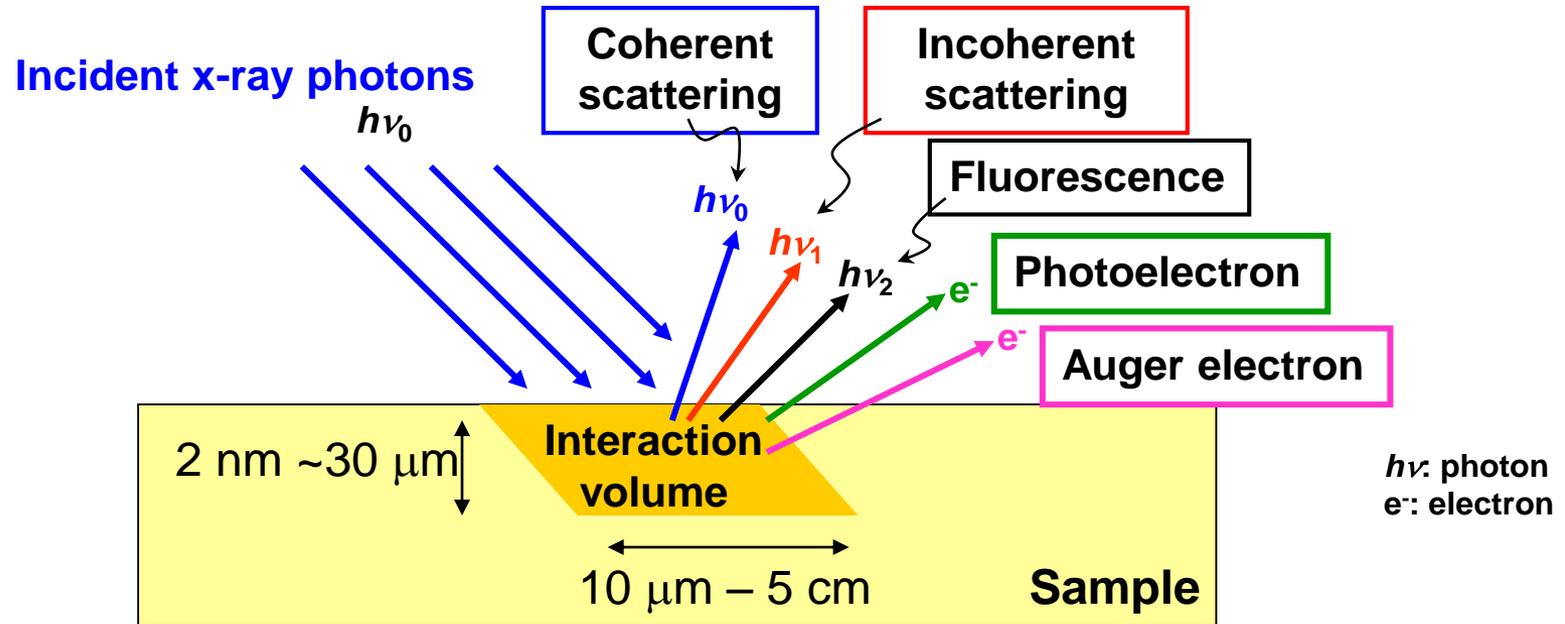


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# X-ray interactions with matter



X-ray radiation mostly used in lab instruments:  
Cu radiation

- Cu  $K\alpha$ :  $\lambda = 0.15418$  nm (8.05 keV, conventional resolution)

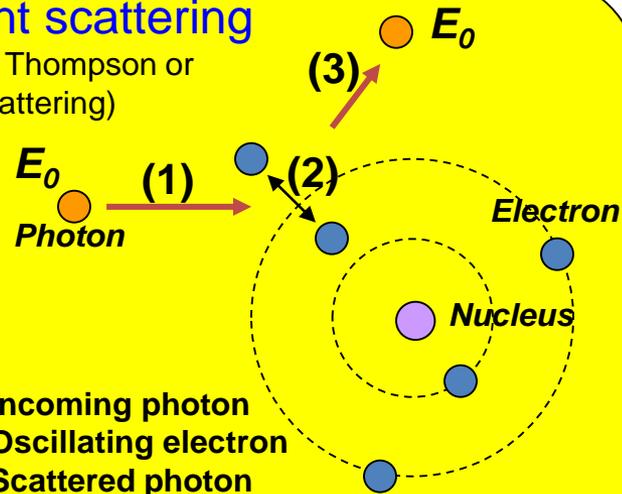
- Cu  $K\alpha_1$ : ( $\lambda = 0.15056$  nm (high resolution))



# X-ray interactions with matter

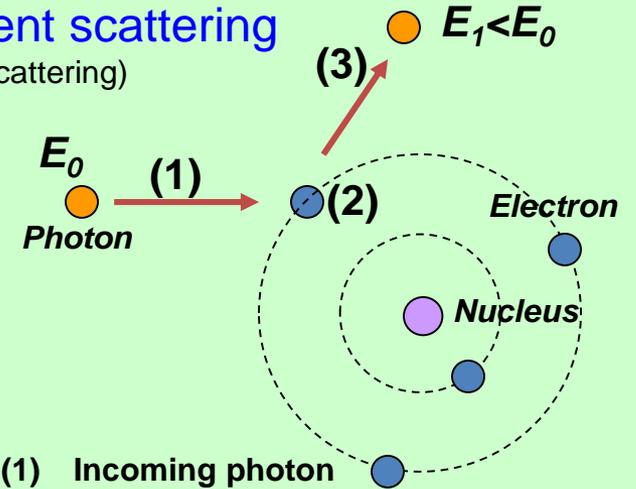
## Coherent scattering

(Diffraction, Thompson or Rayleigh scattering)

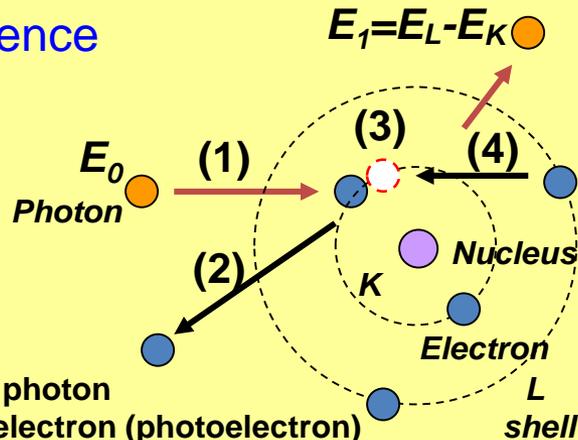


## Incoherent scattering

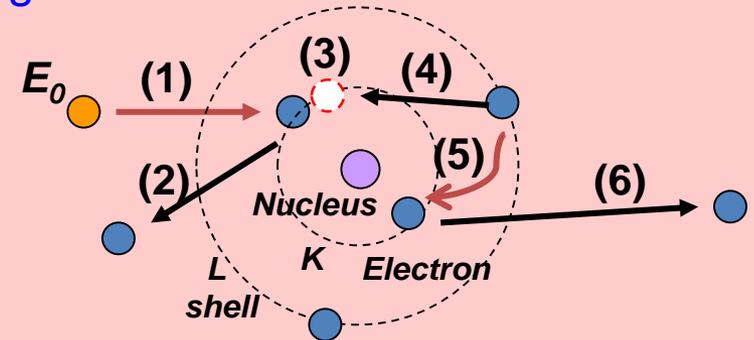
(Compton scattering)



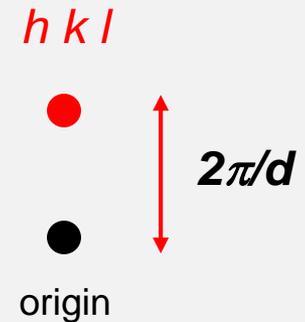
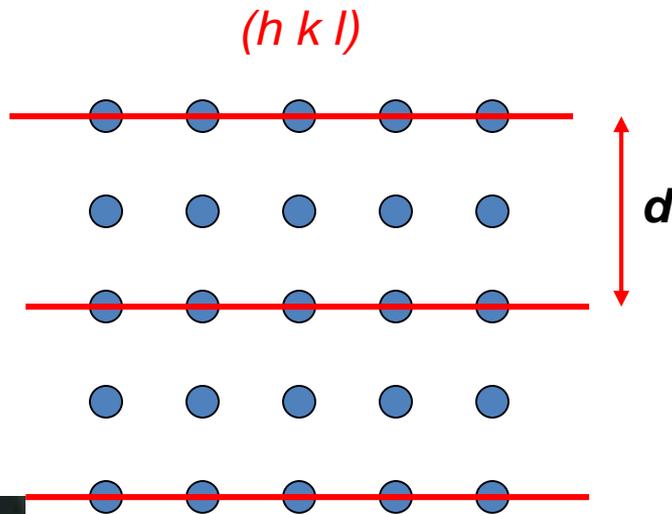
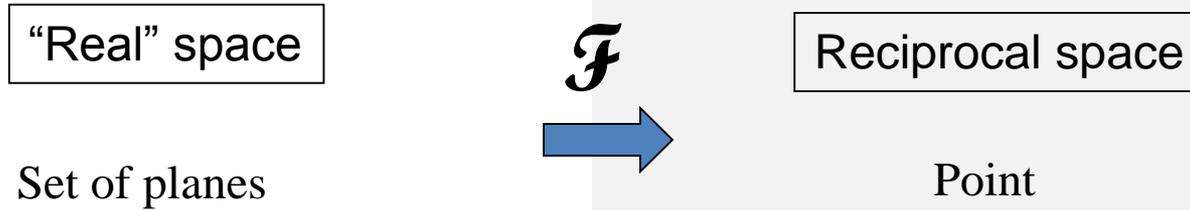
## Fluorescence



## Auger electron

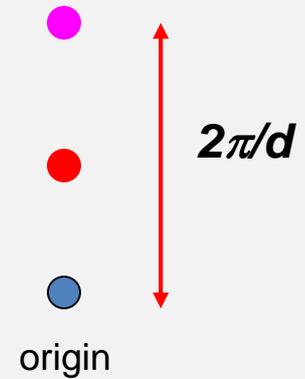
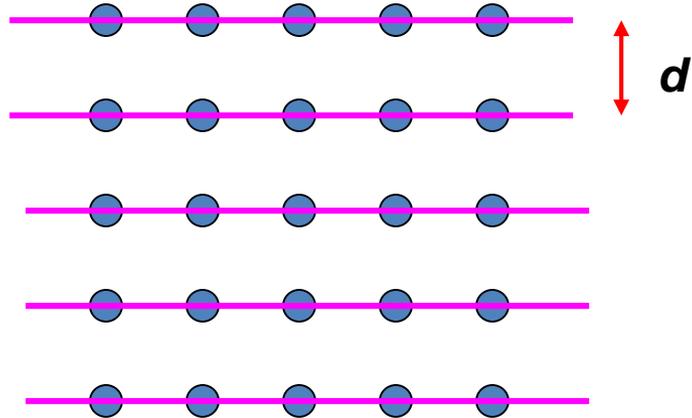


# Fundamentals of diffraction

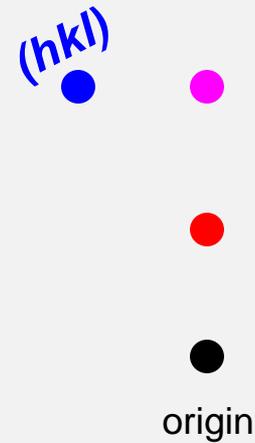
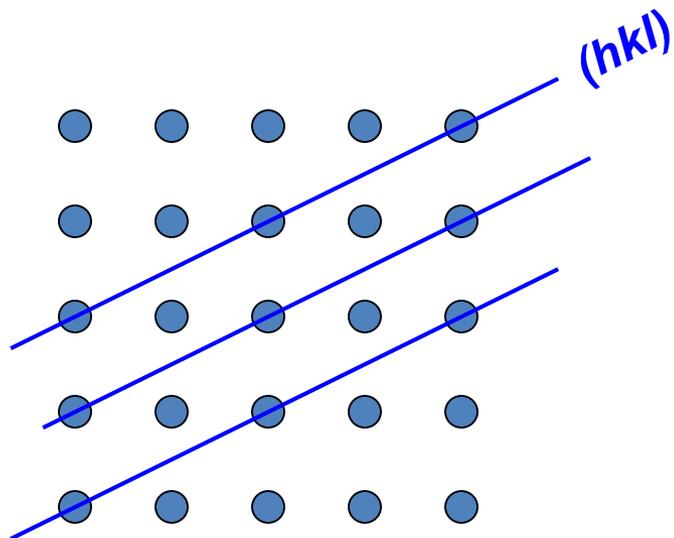


M. von Laue 1879-1960  
X-rays from crystals, 1912.

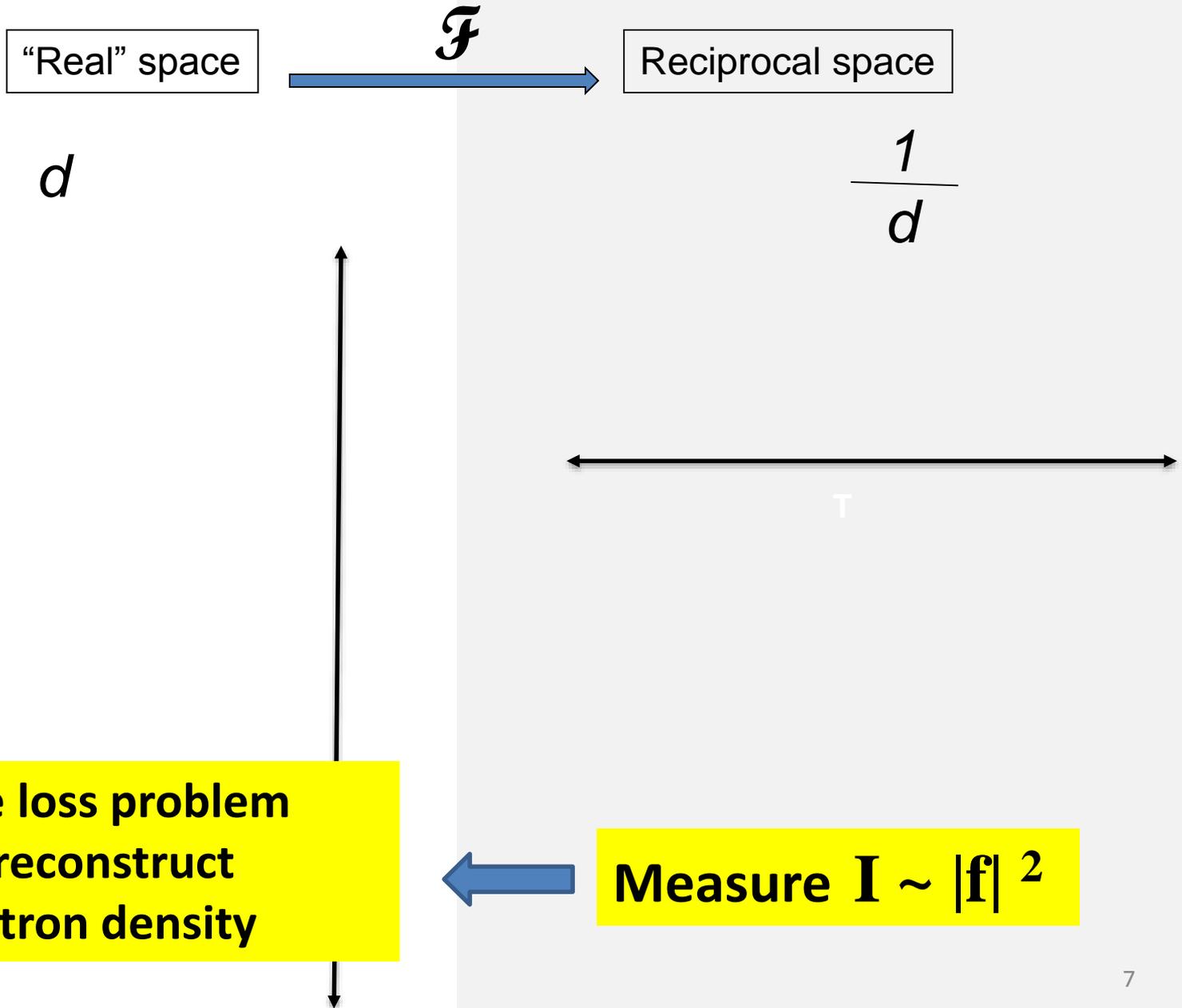
# Fundamentals of diffraction



# Fundamentals of diffraction



# Fundamentals of diffraction

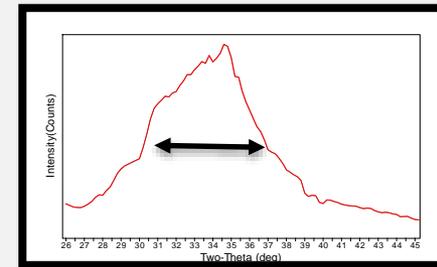
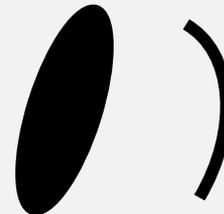
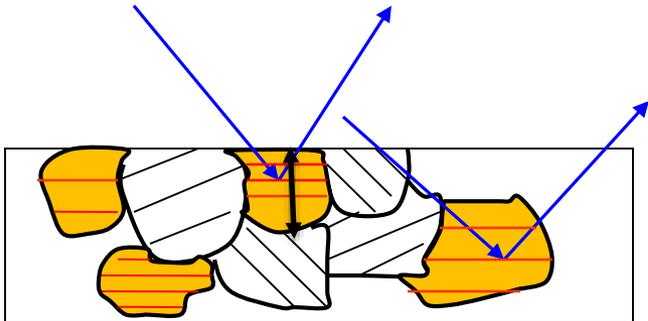
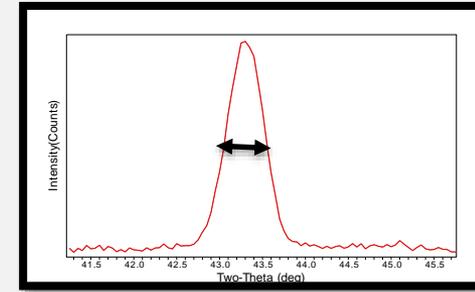
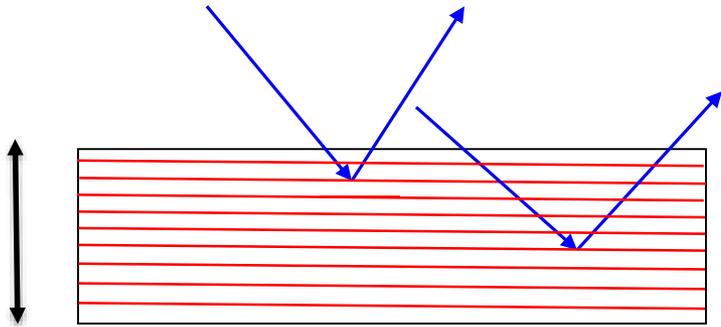


# Fundamentals of diffraction



$d$

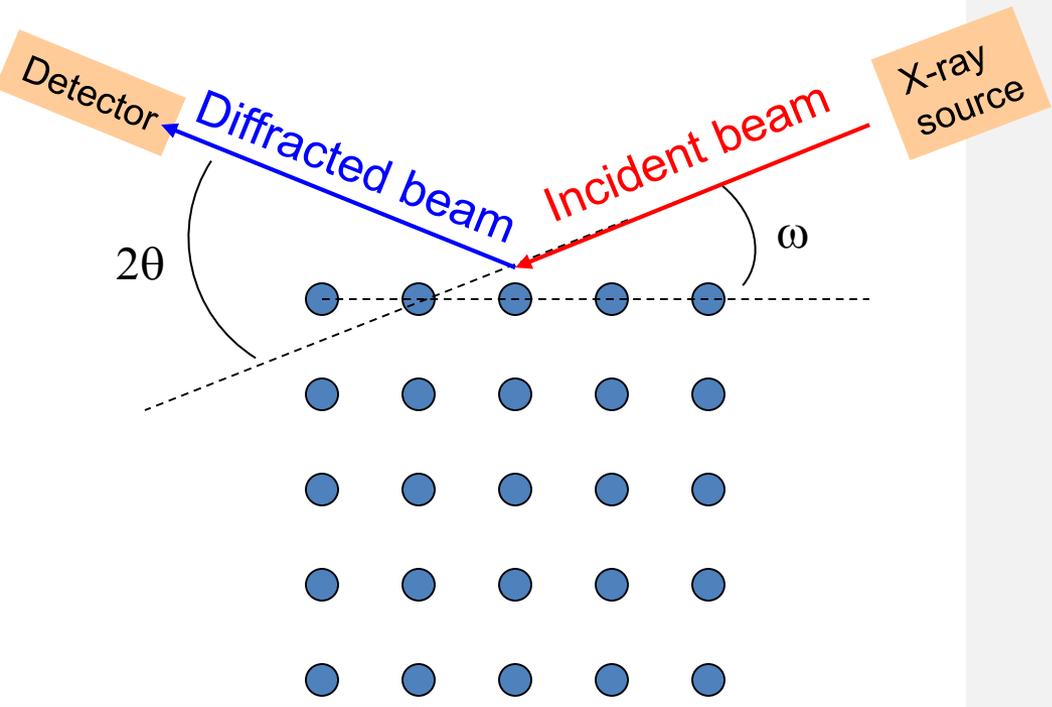
$\frac{1}{d}$



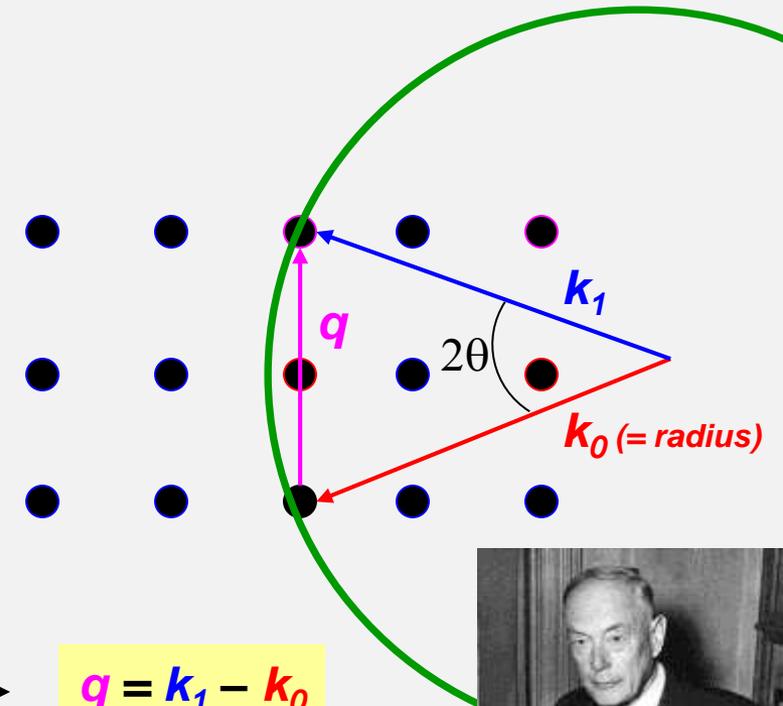
# Bragg's law and Ewald's sphere



## Bragg's law



## Ewald's sphere

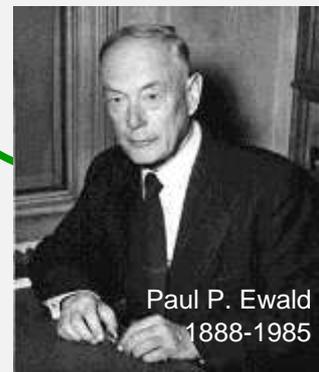


$2 d \sin \theta = n \lambda$

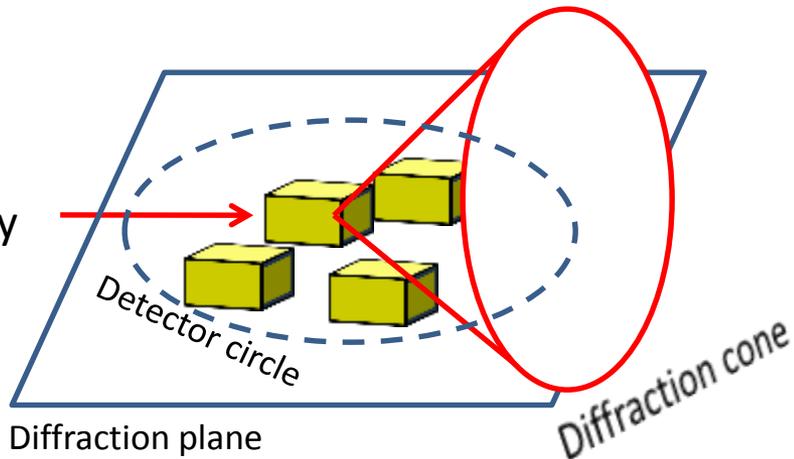
$q = k_1 - k_0$

← Elastic (Thompson's) scattering →

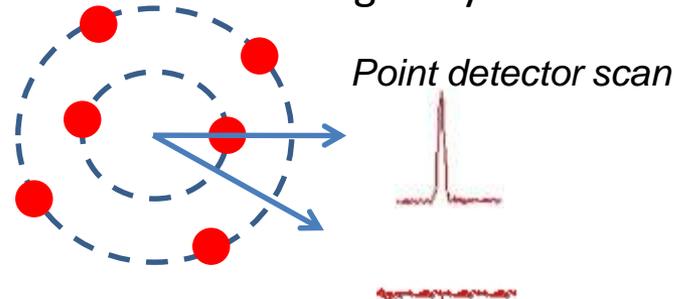
$q$ : scattering vector  
 $q = (4 \pi / \lambda) \sin \theta$



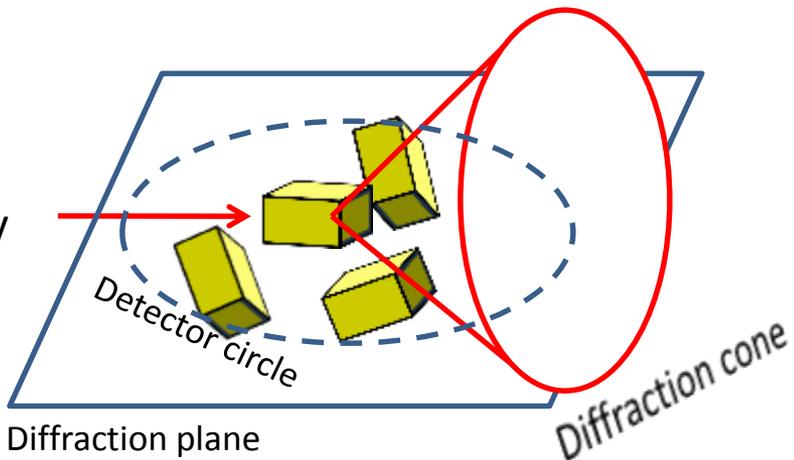
X-ray



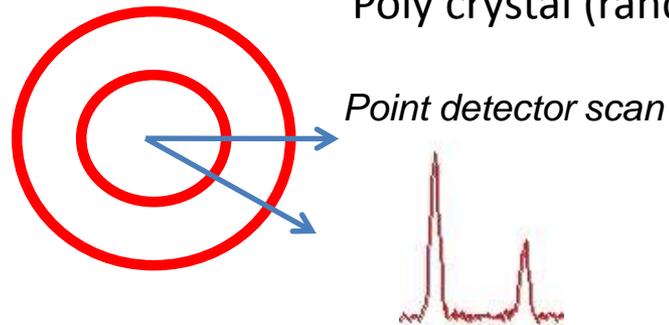
Single crystal



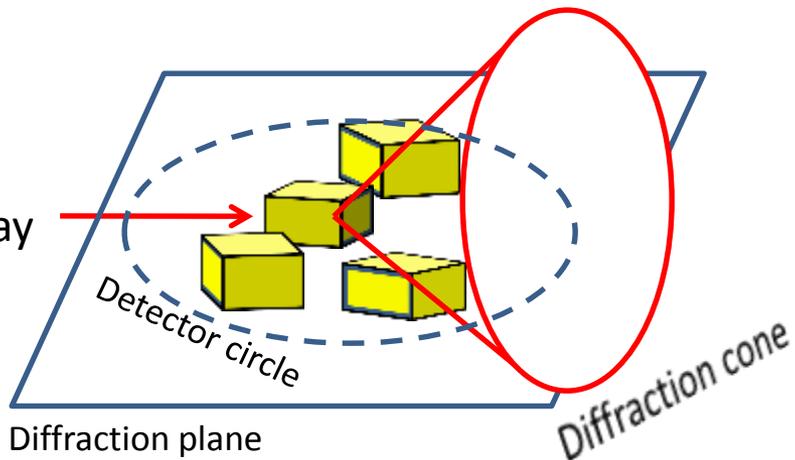
X-ray



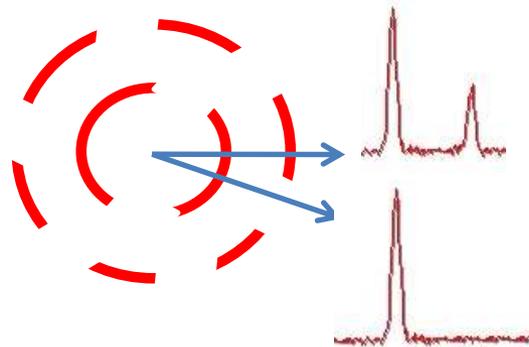
Poly crystal (random)



X-ray



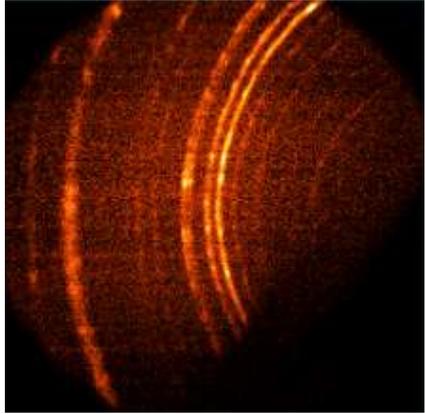
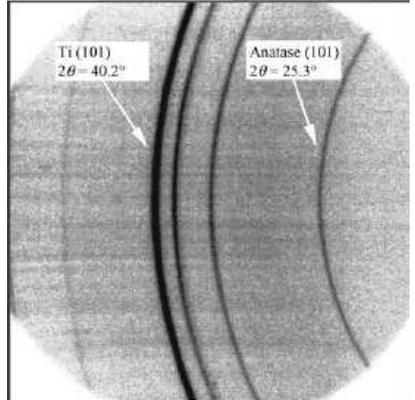
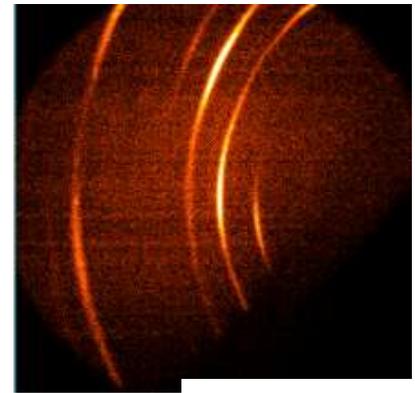
Poly crystal (texture)



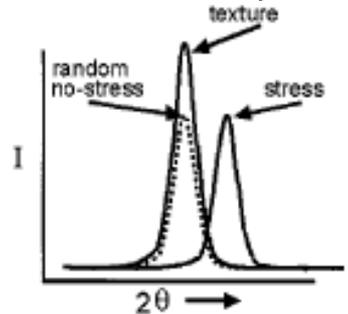
# Two-dimensional XRD:

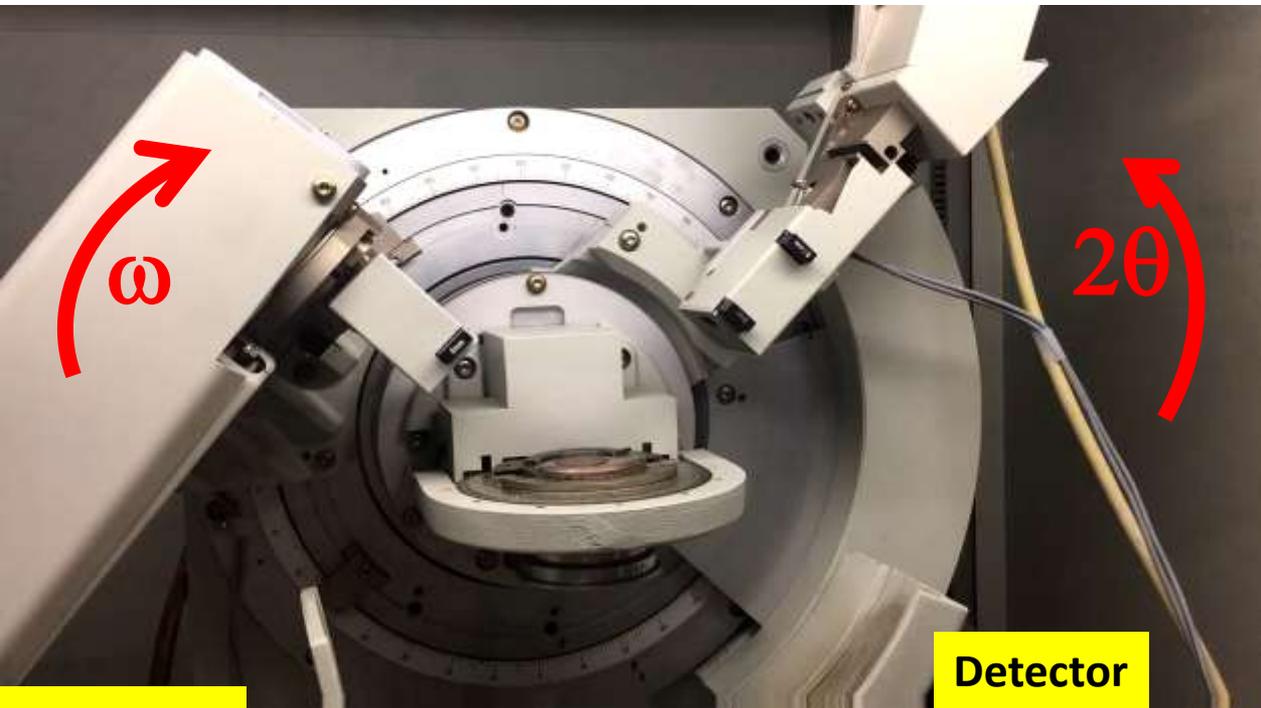


Continuous intensity distribution along diffraction ring, no distortion	Intensity varies along the ring	Distortion / shift of the diffraction ring	Spotty features in the diffraction ring
No texture. Homogenous grain size distribution.	Texture	Residual stress	Non homogenous distribution of grain sizes; spots due to large grains

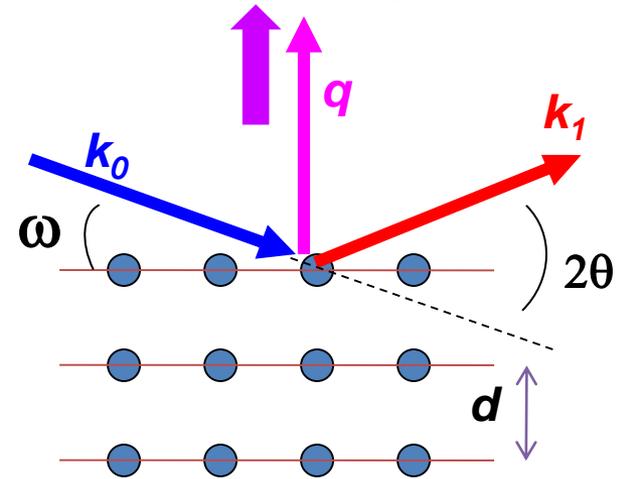


Data from: He et al, Adv in X-ray Analysis 37, vol 46 (2003)



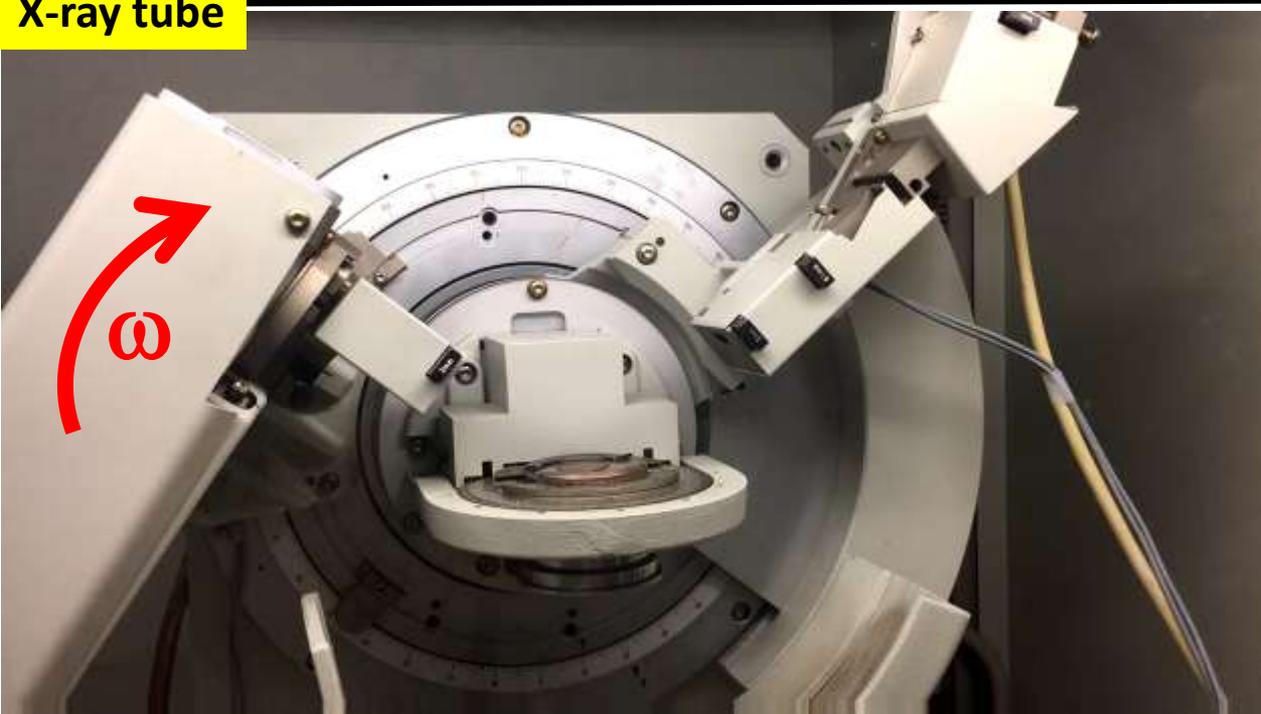


### 2theta/omega scan

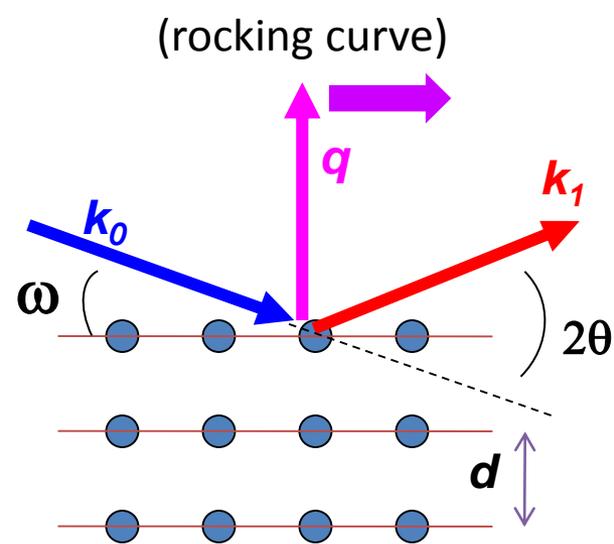


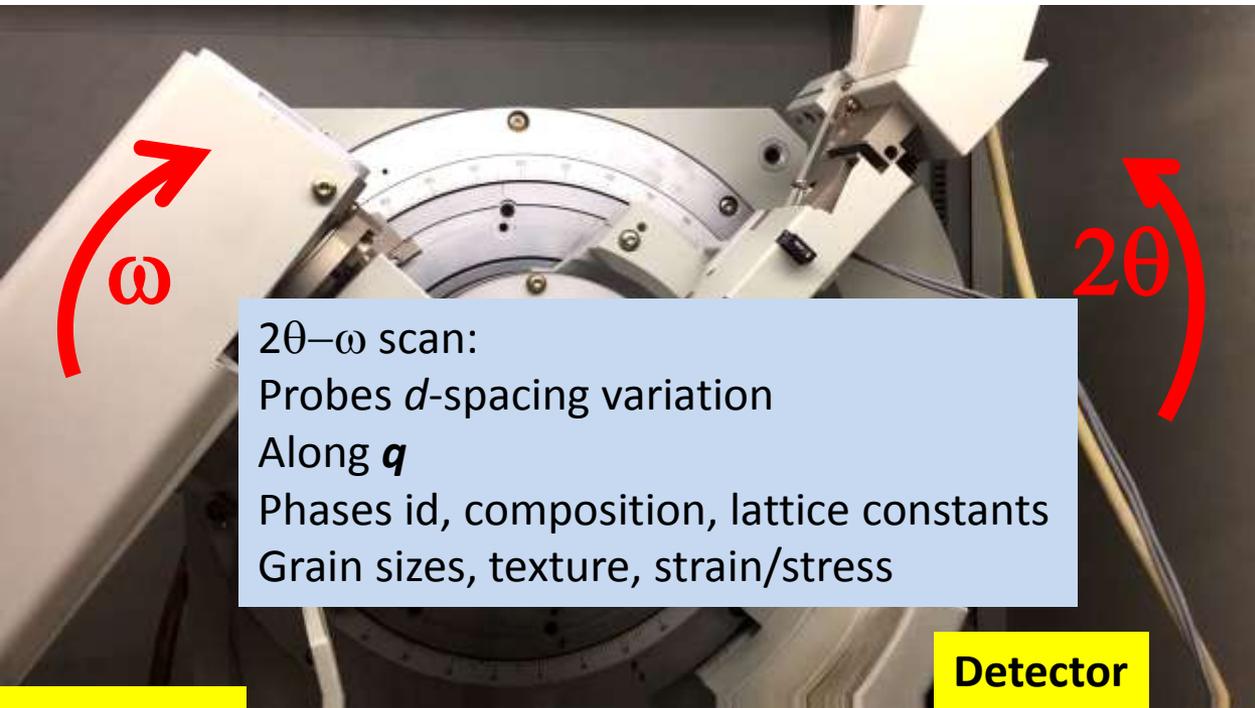
X-ray tube

Detector

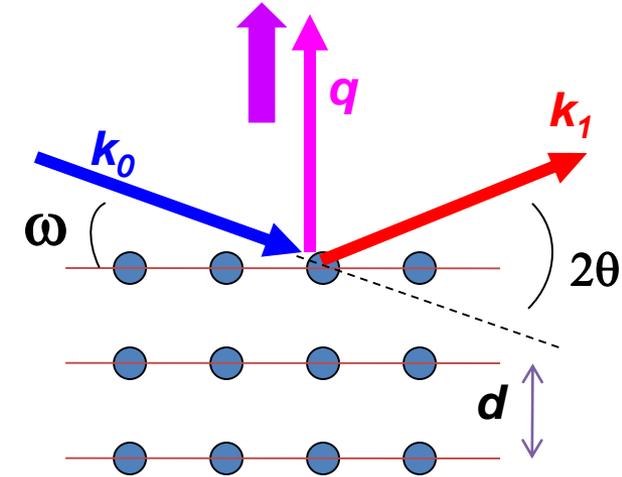


### omega scan (rocking curve)

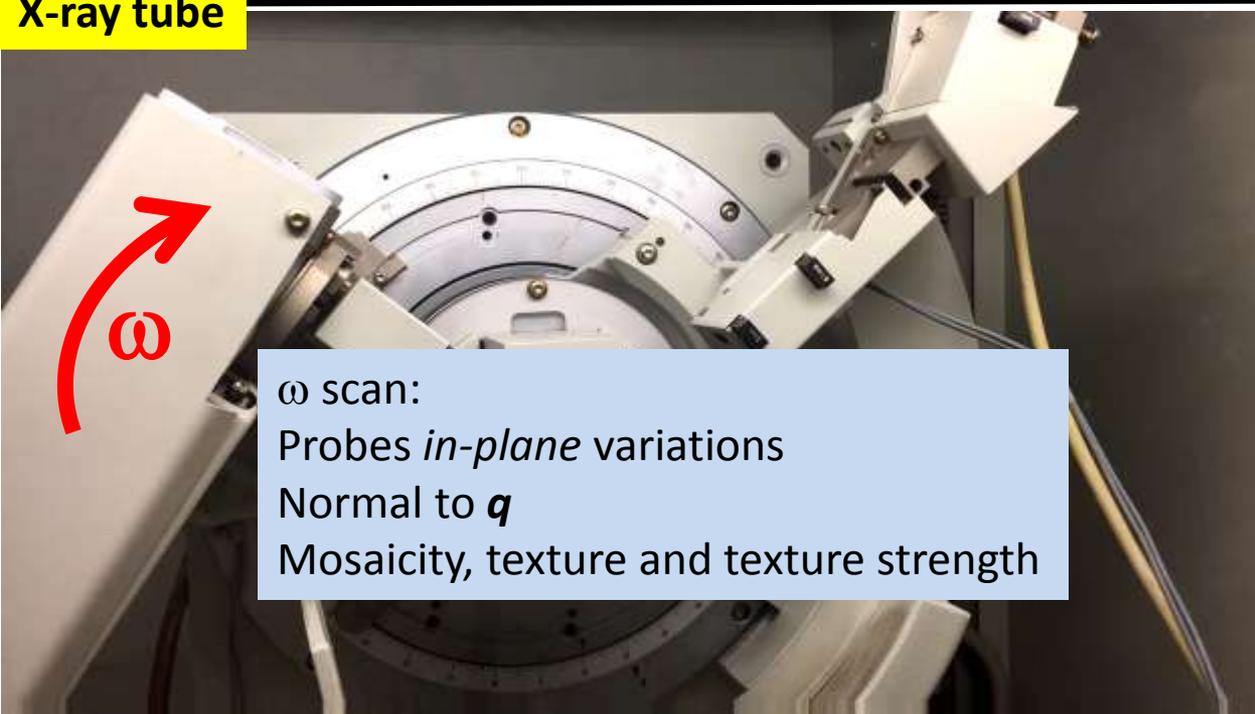




## 2theta/omega scan

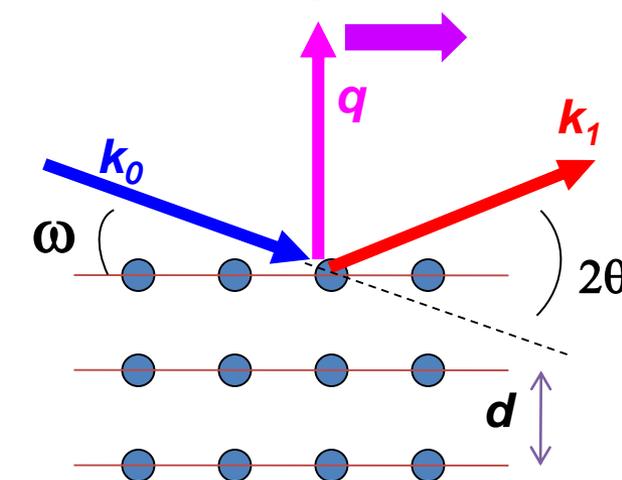


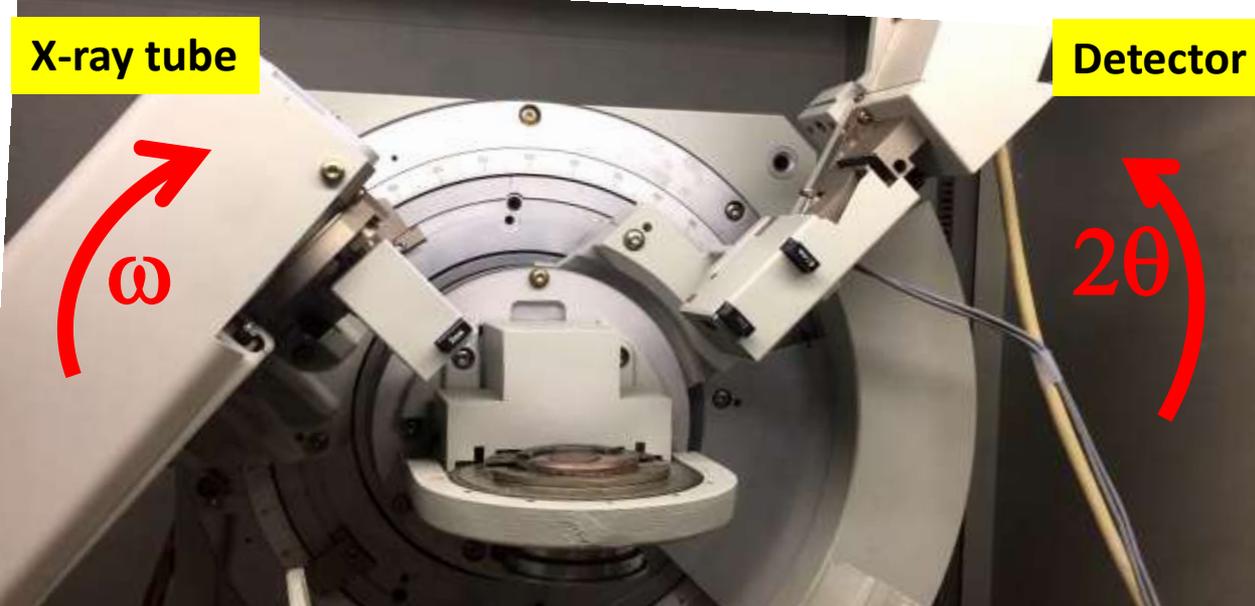
**X-ray tube**



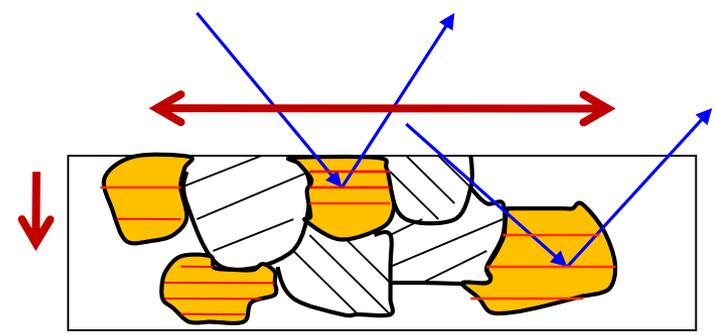
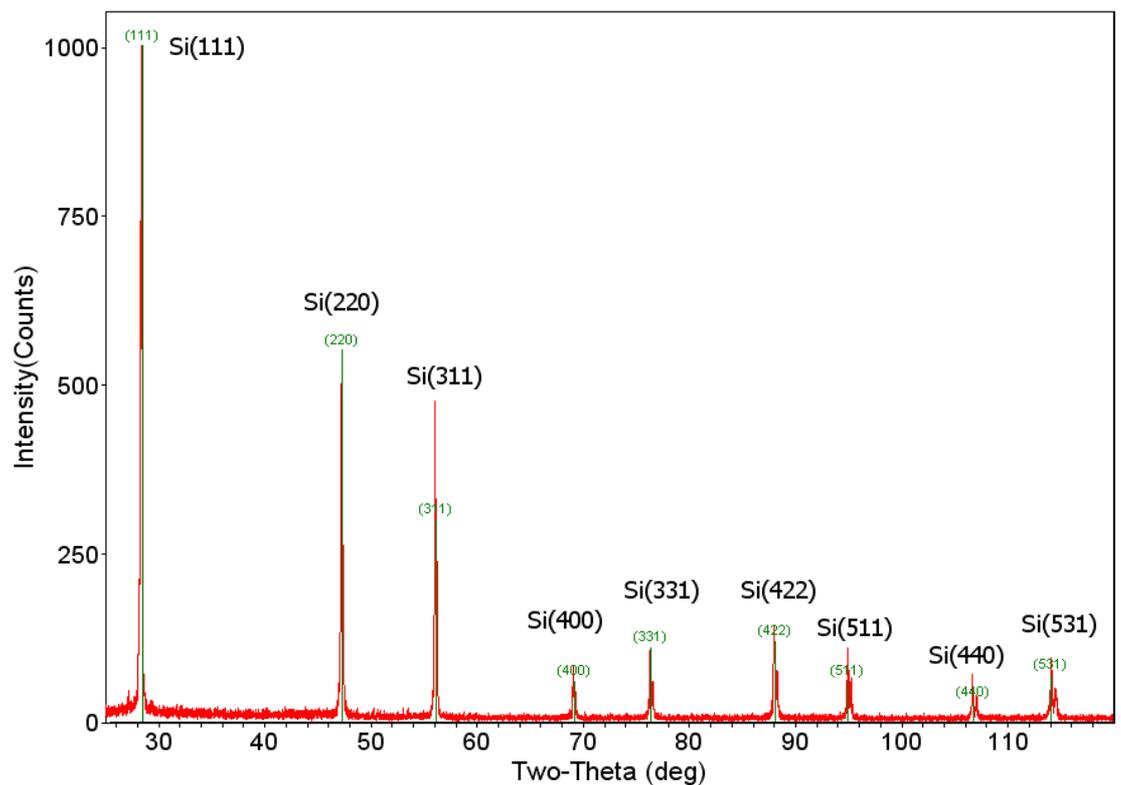
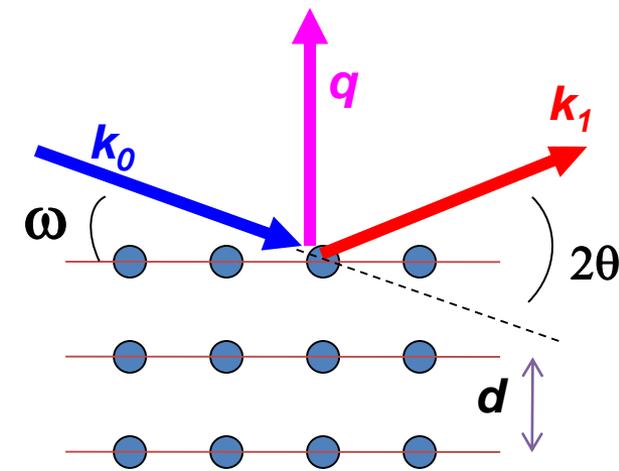
## omega scan

(rocking curve)





2theta/omega scan



X-ray tube

Detector

2theta/omega scan



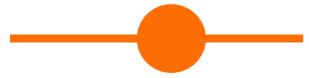
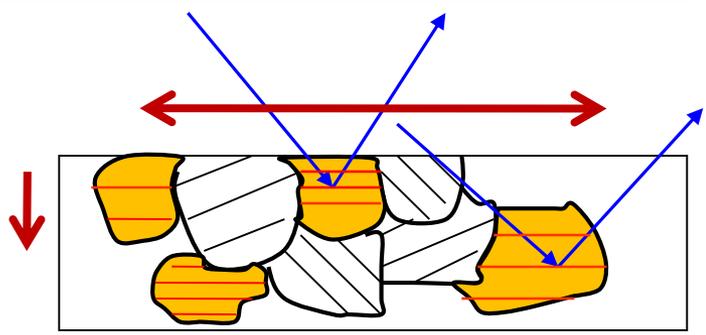
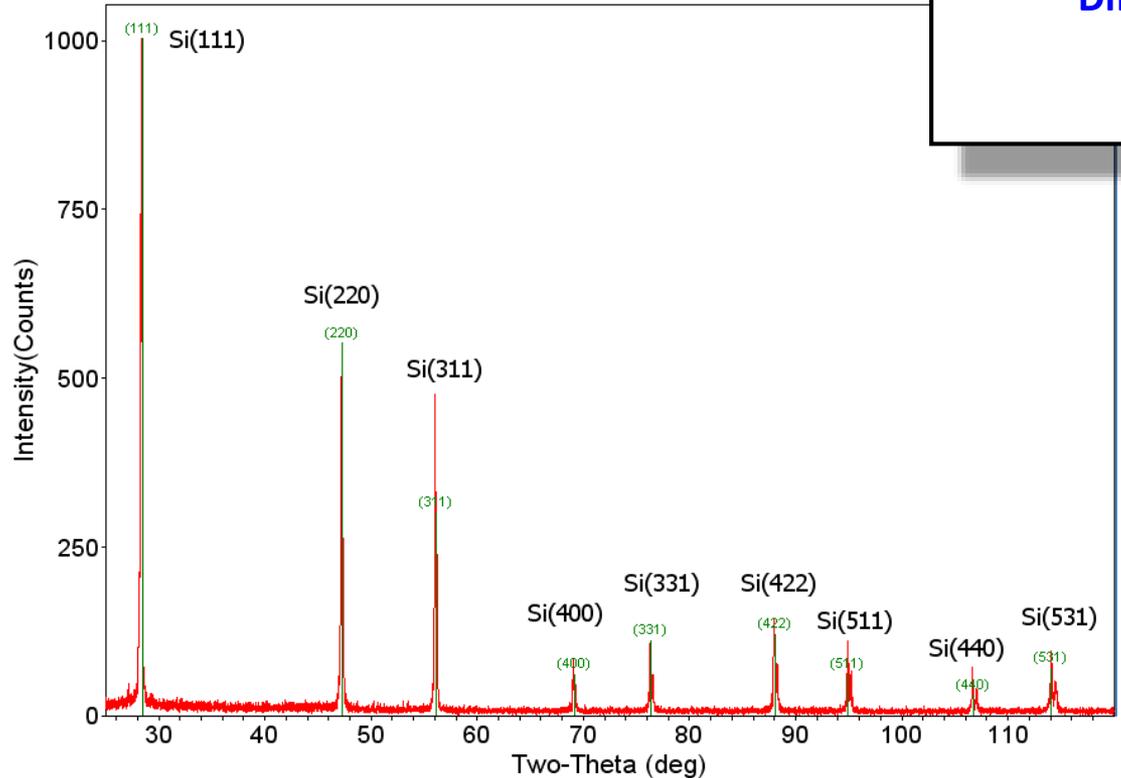
**Peak position:**  
 identification, structure, lattice parameter

**Peak width:**  
 crystallite size, strain, defects

**Peak area or height ratio:**  
 preferred orientation

**Peak tails:**  
 Diffuse scattering, point defects

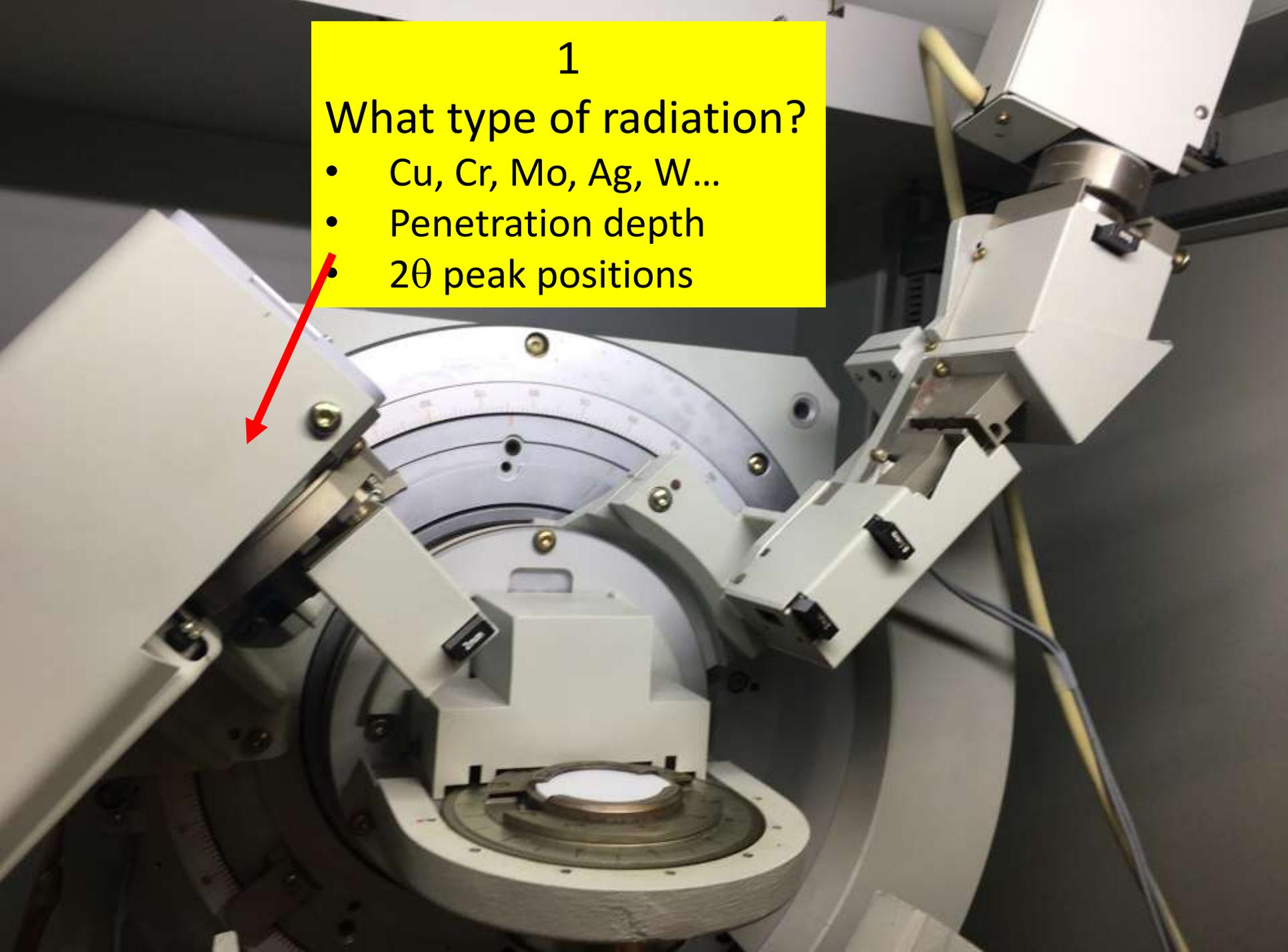
**Background:**  
 amorphous contents



1

What type of radiation?

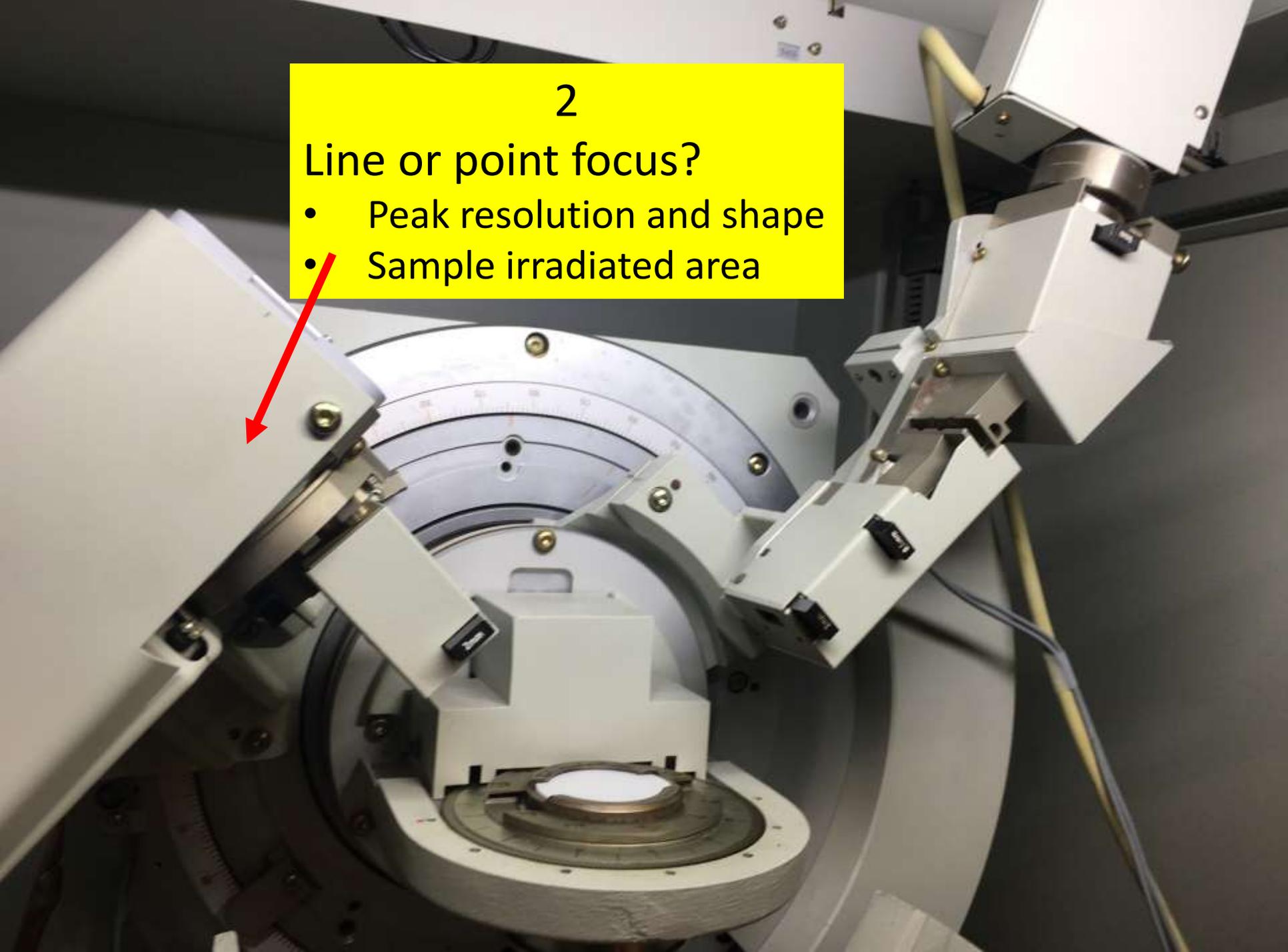
- Cu, Cr, Mo, Ag, W...
- Penetration depth
- $2\theta$  peak positions



2

Line or point focus?

- Peak resolution and shape
- Sample irradiated area



3

What type of monochromator?

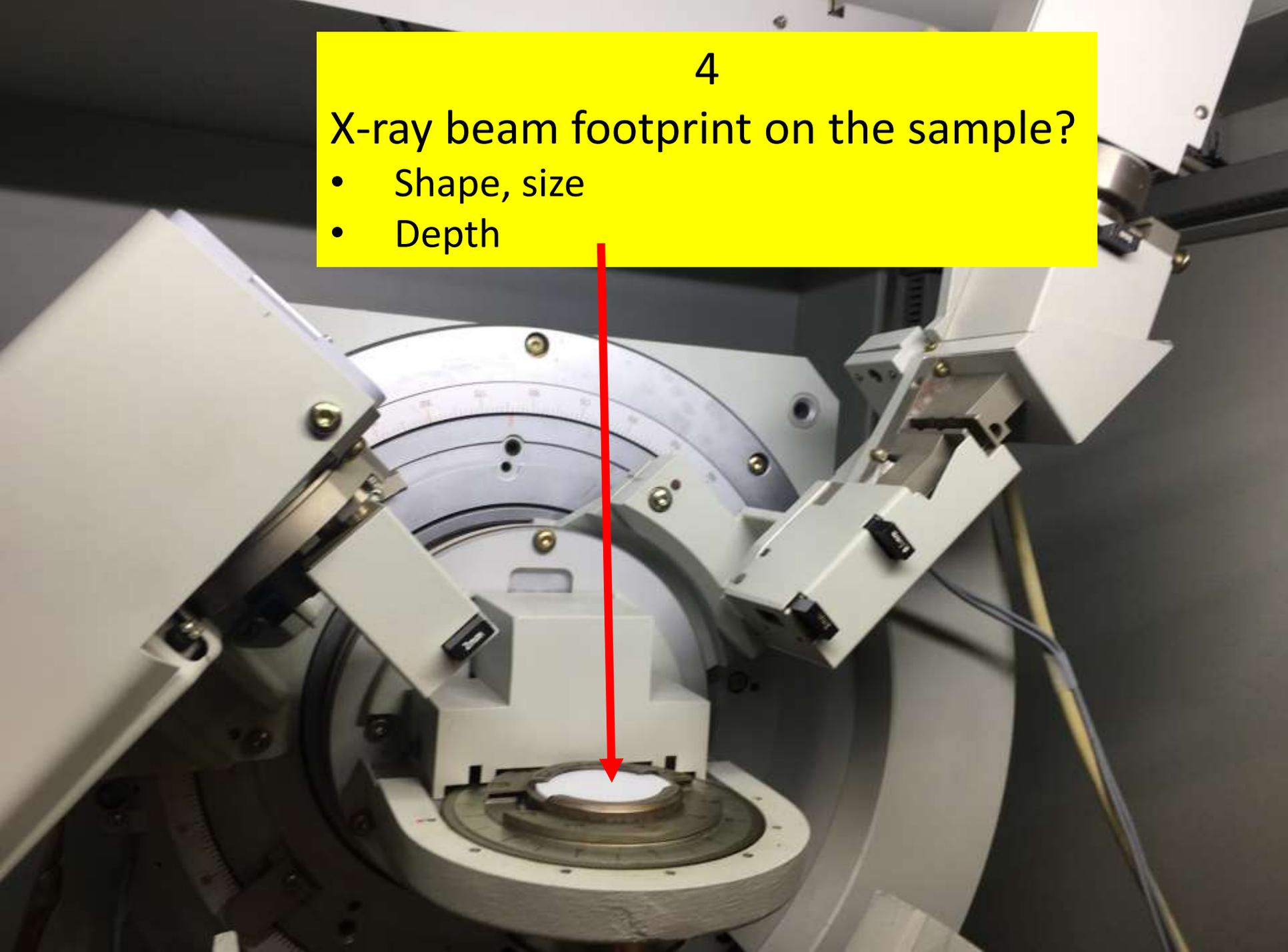
- Filter, x-ray mirror, crystal monochromator
- White radiation,  $K\alpha_1+K\alpha_2$ ,  $K\alpha_1$



4

X-ray beam footprint on the sample?

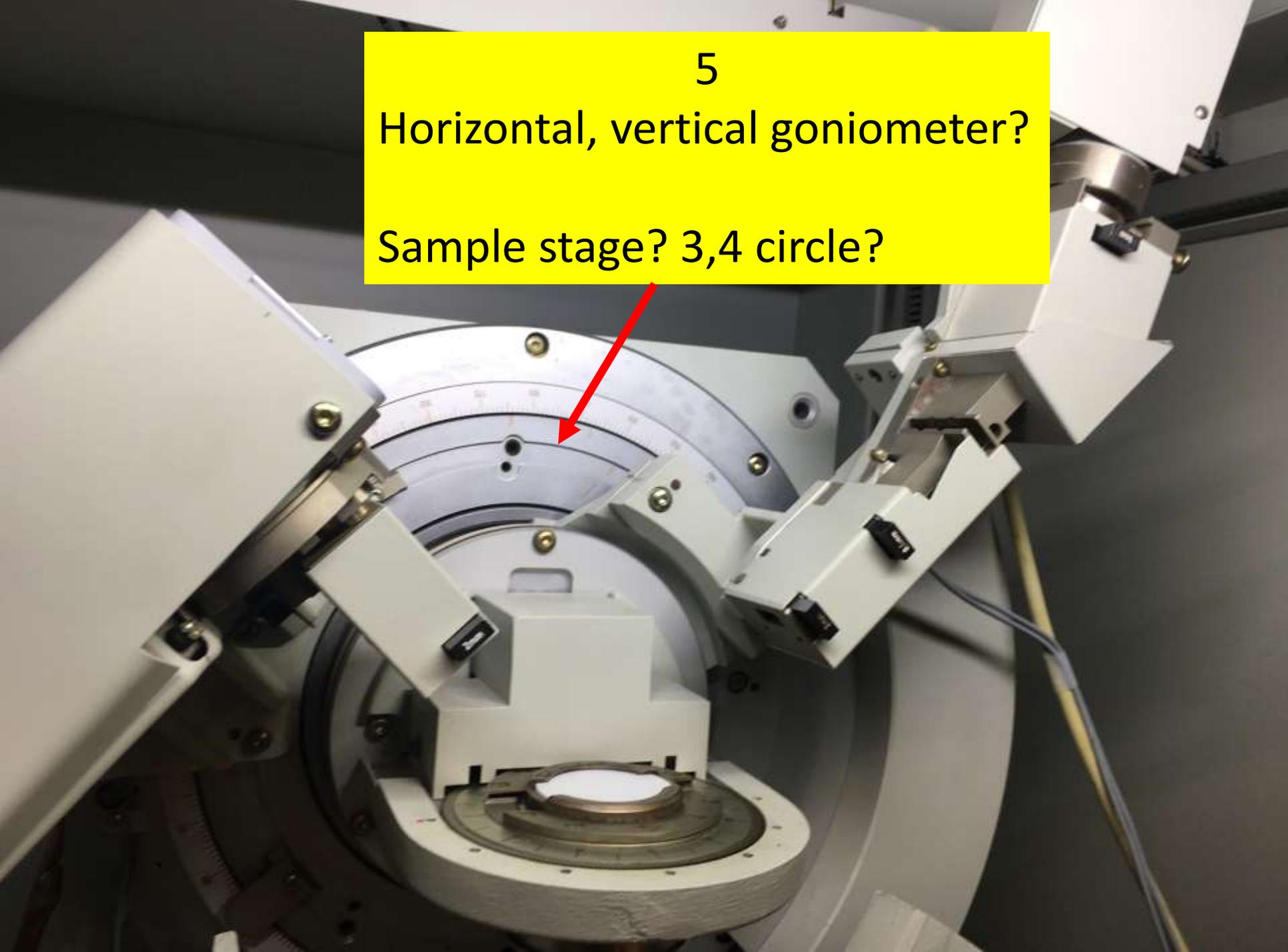
- Shape, size
- Depth



5

Horizontal, vertical goniometer?

Sample stage? 3,4 circle?

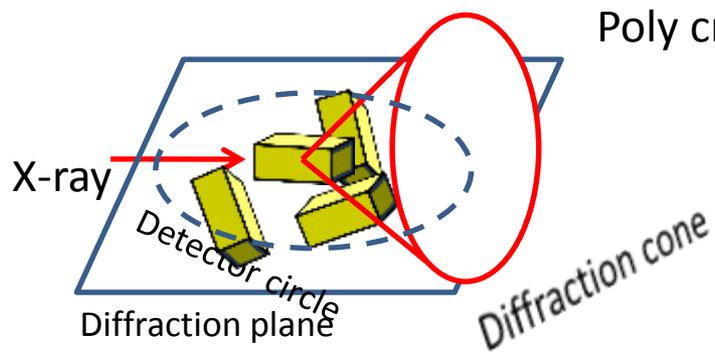


6

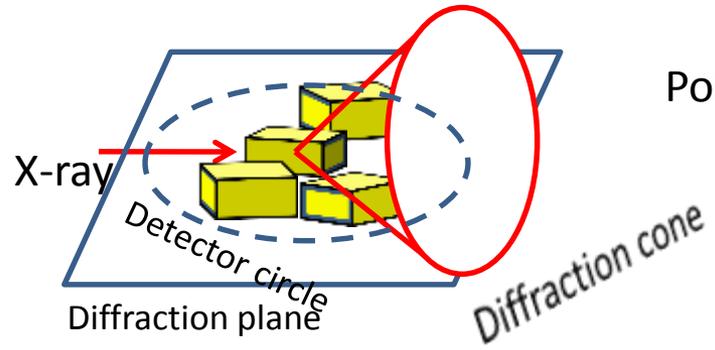
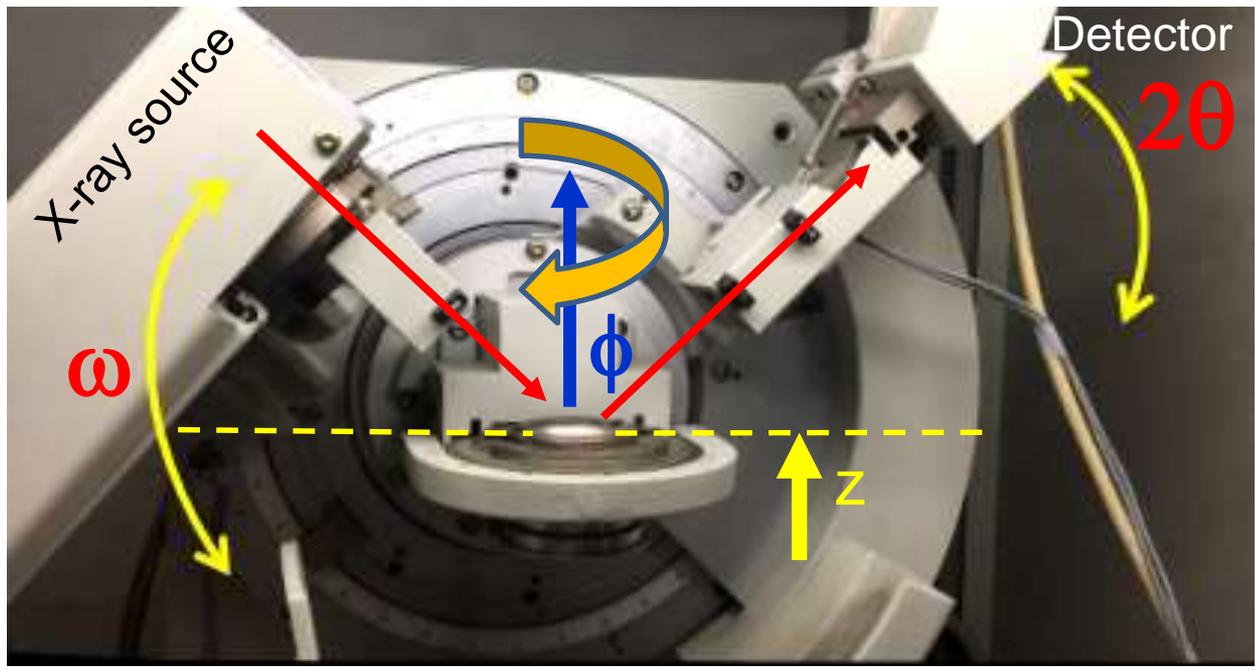
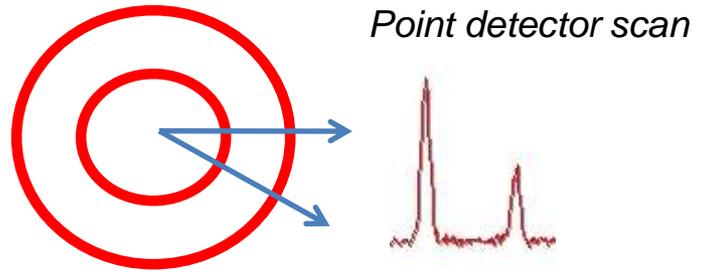
What type of detector?

- Resolution
- Point, Line, Area

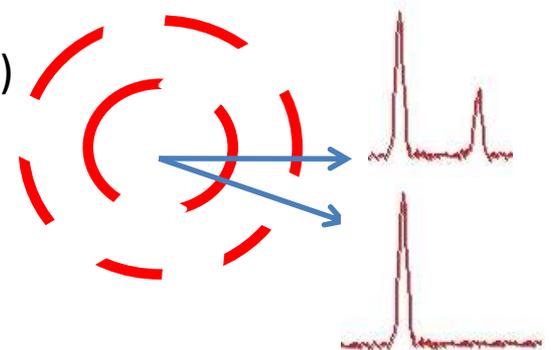




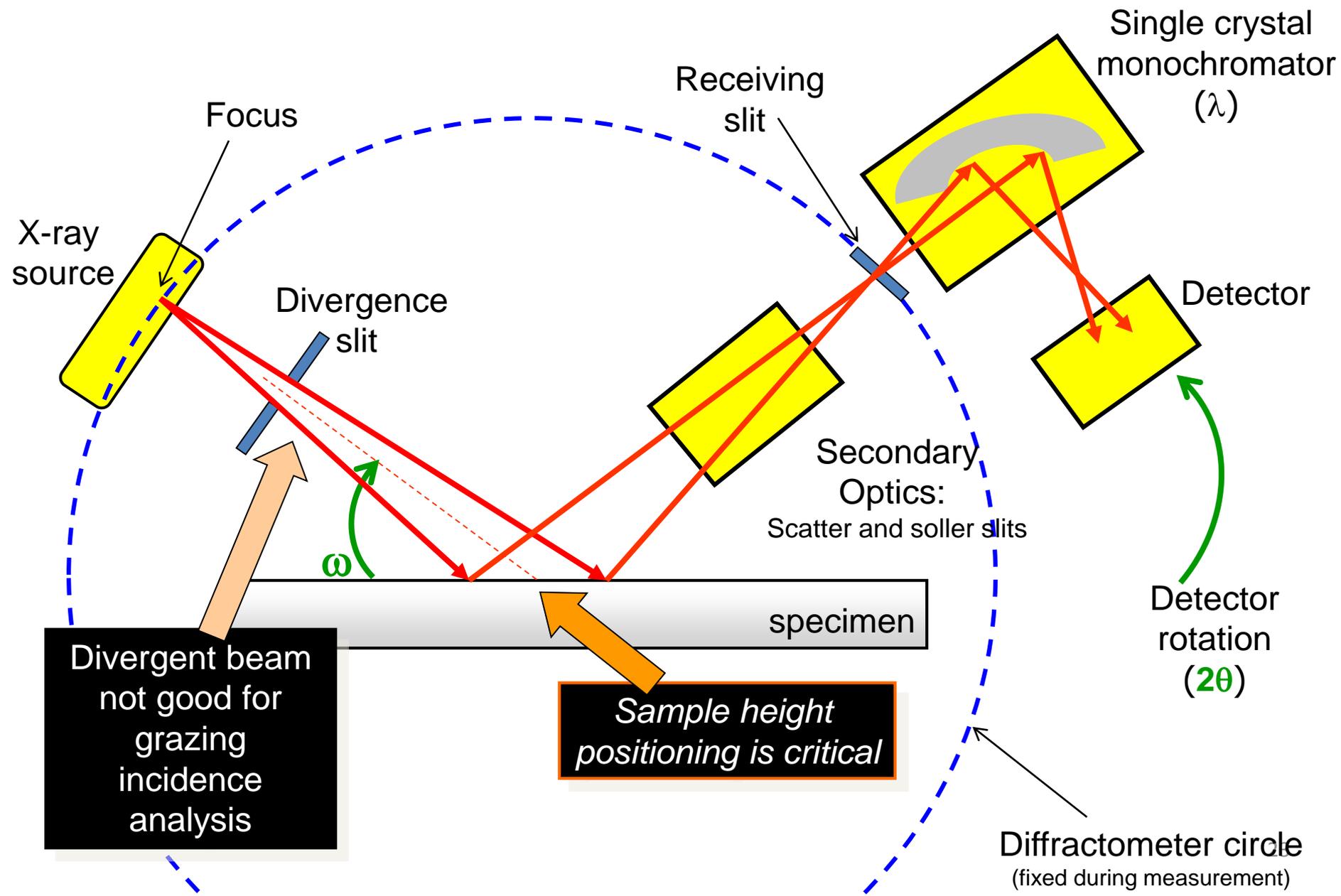
Poly crystal (random)



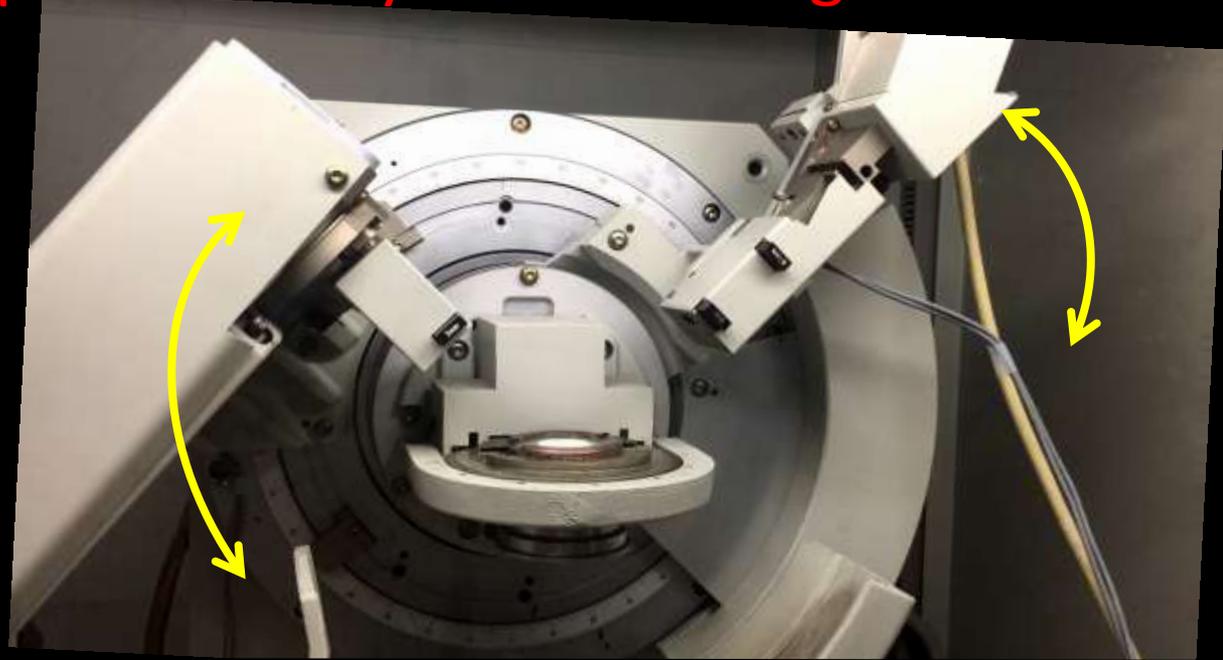
Poly crystal (texture)



# Bragg-Brentano focusing configuration

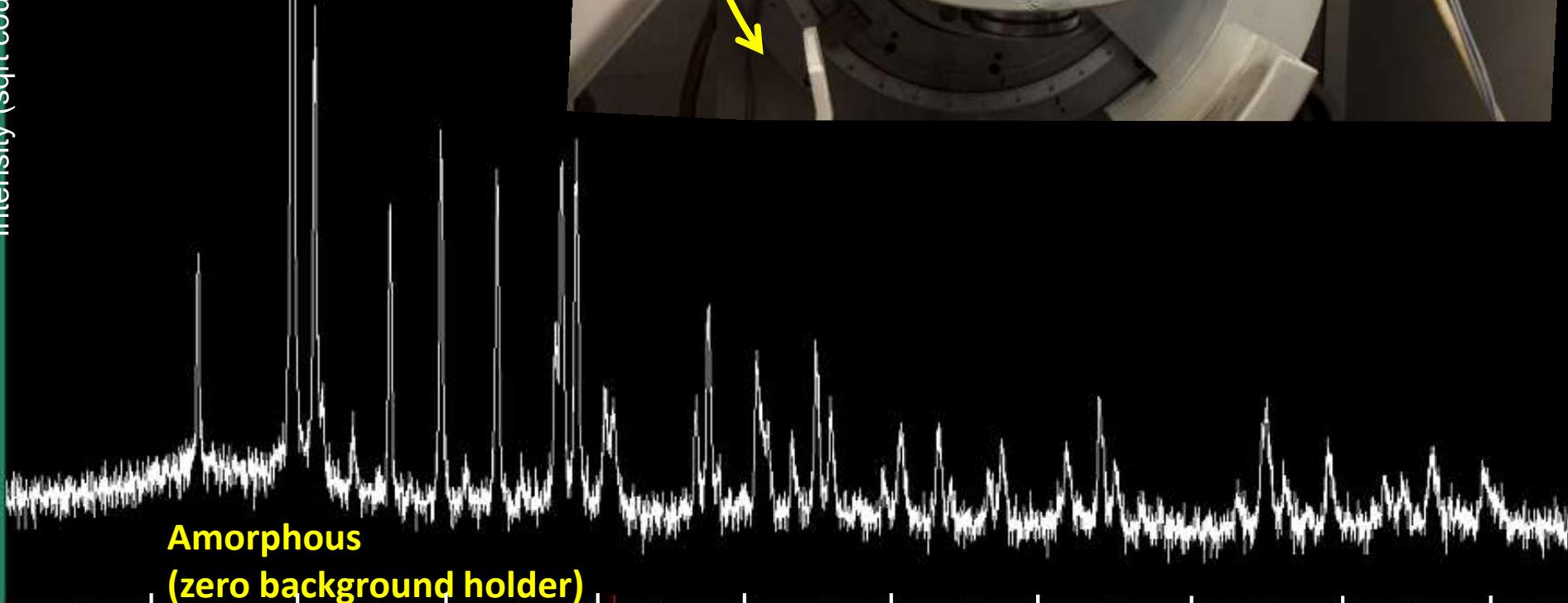


# XRD powder analysis walkthrough



**Crystalline phases**

Intensity (sqrt counts)

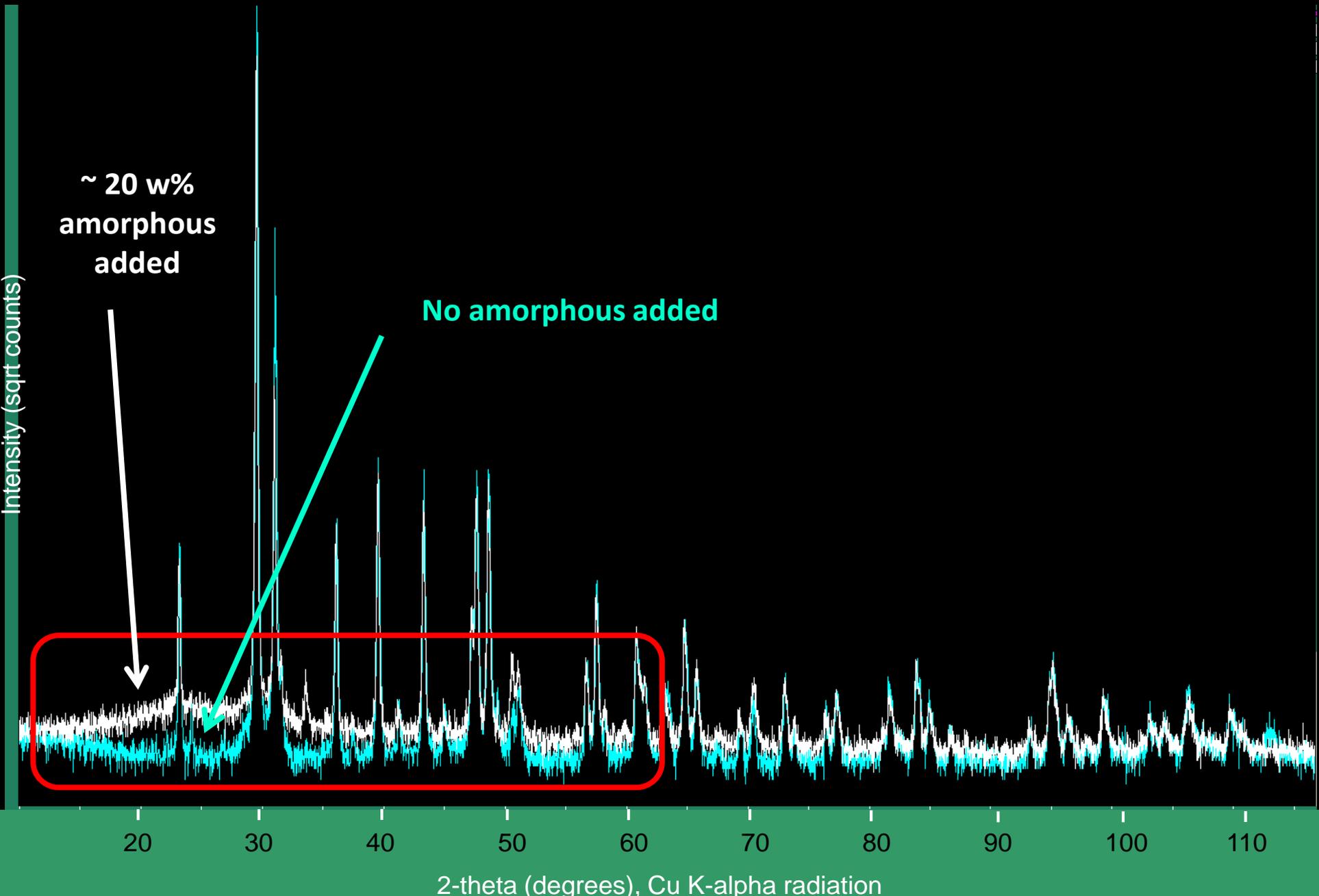


**Amorphous  
(zero background holder)**

20 30 40 50 60 70 80 90 100 110

2-theta (degrees), Cu K-alpha radiation

# XRD powder pattern



# Peak fit and shape analysis

**Peak fit:** Data + Peak shape + function + Instrument resolution  
 $\text{FWHM} = f(2\theta)$

$$\text{Crystallinity} = \frac{\sum \text{Peak areas}}{\text{Total area}} = 81.7 \%$$

$$\text{Amorphous contents} = 1 - (\text{crystallinity}) = 18.3 \%$$

Intensity (sqrt counts)

20 30 40 50 60 70 80 90 100 110

2-theta (degrees), Cu K-alpha radiation

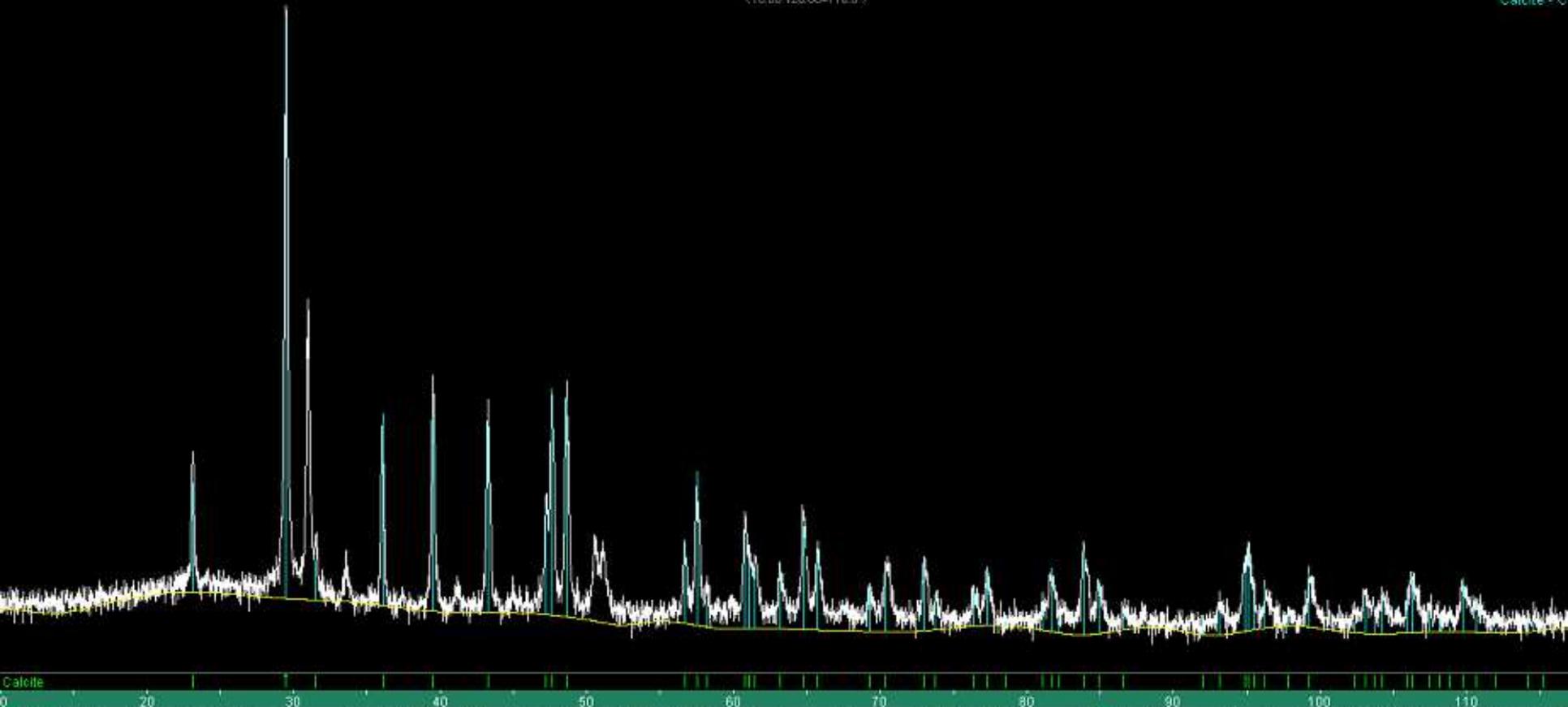
# Search / match

Peak position  
+ intensity ratio

Search against...

ICDD PDF4 database  
ICSD, etc.

Match! Fingerprinting  
identification of phases



Hits	Formula	FOM	PDF	RIR	Space group
Calcite	$\text{CaCO}_3$	1.1	04-012-0489	3.45	R-3c(167)
Dolomite	$\text{Ca}_{1.07}\text{Mg}_{0.93}(\text{CO}_3)_2$	15.0	04-011-9830	2.51	R-3(148)

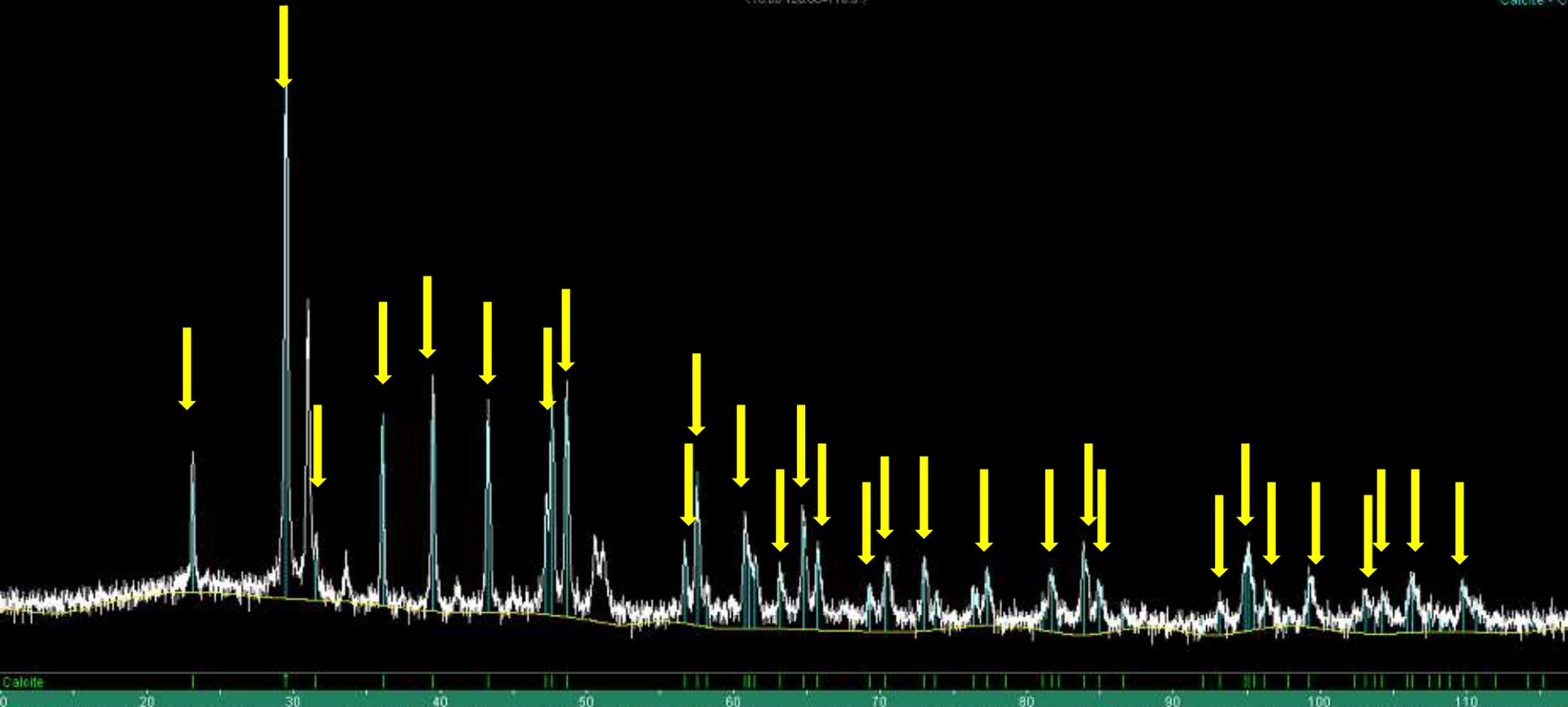
# Search / match

Peak position  
+ intensity ratio

Search against...

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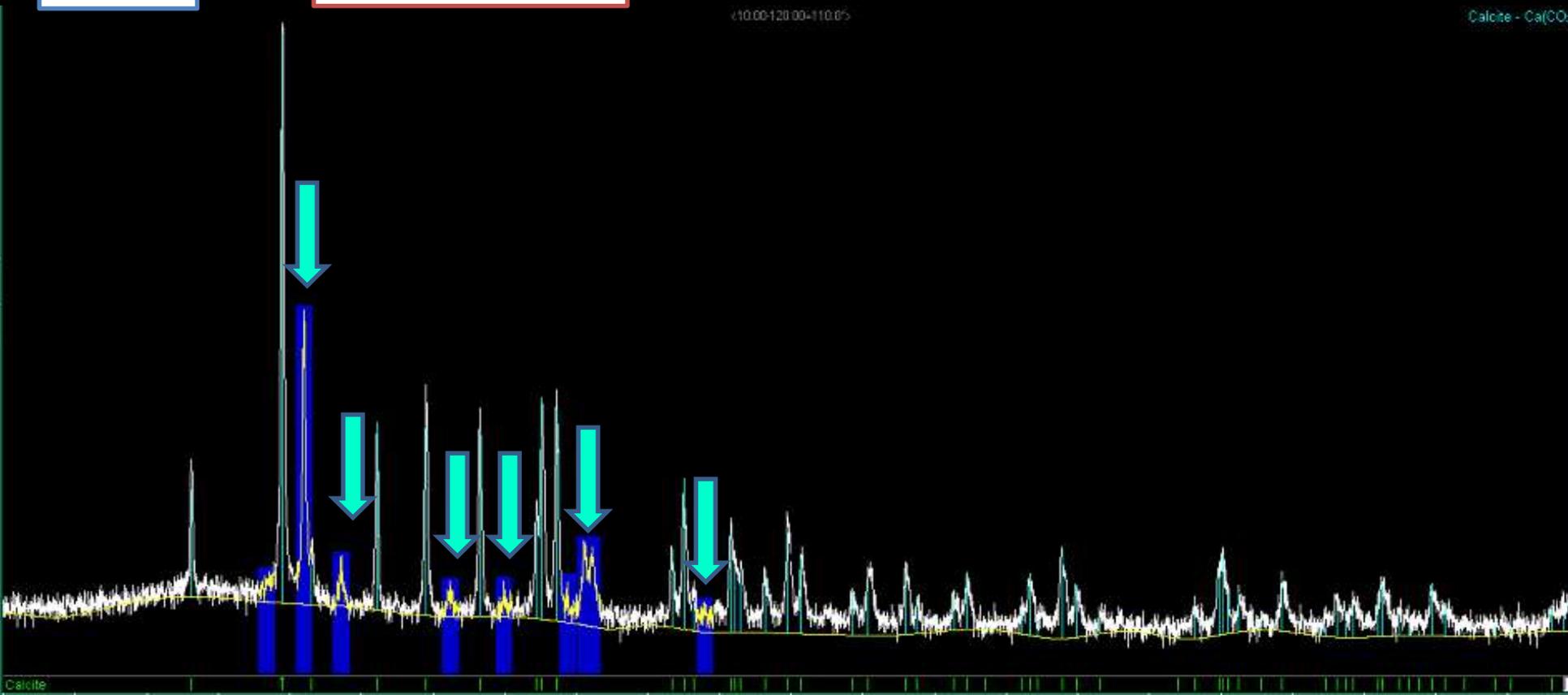


	Hits	Formula	FOM	PDF	RIR	Space group
v	Calcite	CaCO <sub>3</sub>	1.1	04-012-0489	3.45	R-3c(167)
	Dolomite	Ca <sub>1.07</sub> Mg <sub>0.93</sub> (CO <sub>3</sub> ) <sub>2</sub>	15.0	04-011-9830	2.51	R-3(148)

# Search / match

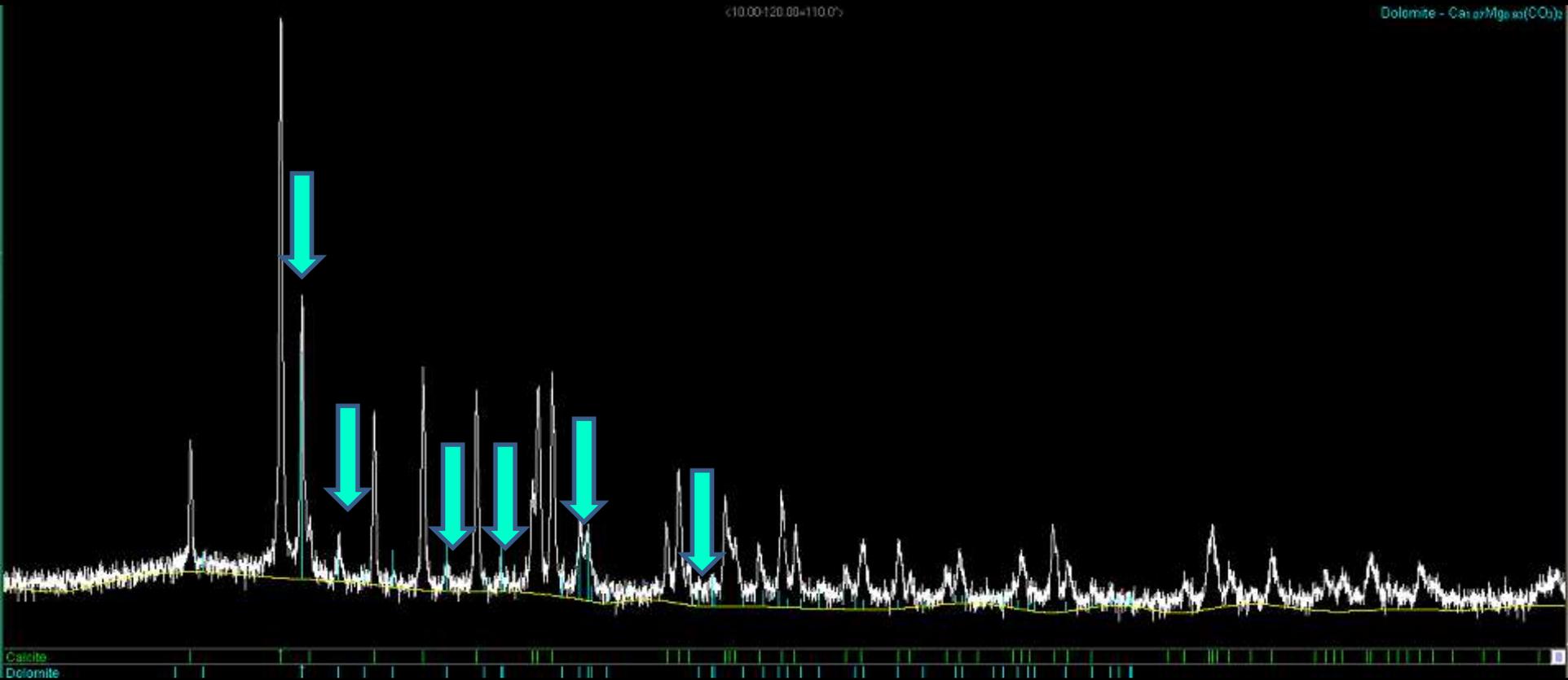
Second round

Focus on unmatched peaks



	Hits	Formula	FOM	PDF	RIR	Space group
v	Calcite	CaCO <sub>3</sub>	1.1	04-012-0489	3.45	R-3c(167)
	Dolomite	Ca <sub>1.07</sub> Mg <sub>0.93</sub> (CO <sub>3</sub> ) <sub>2</sub>	15.0	04-011-9830	2.51	R-3(148)

# Search / match



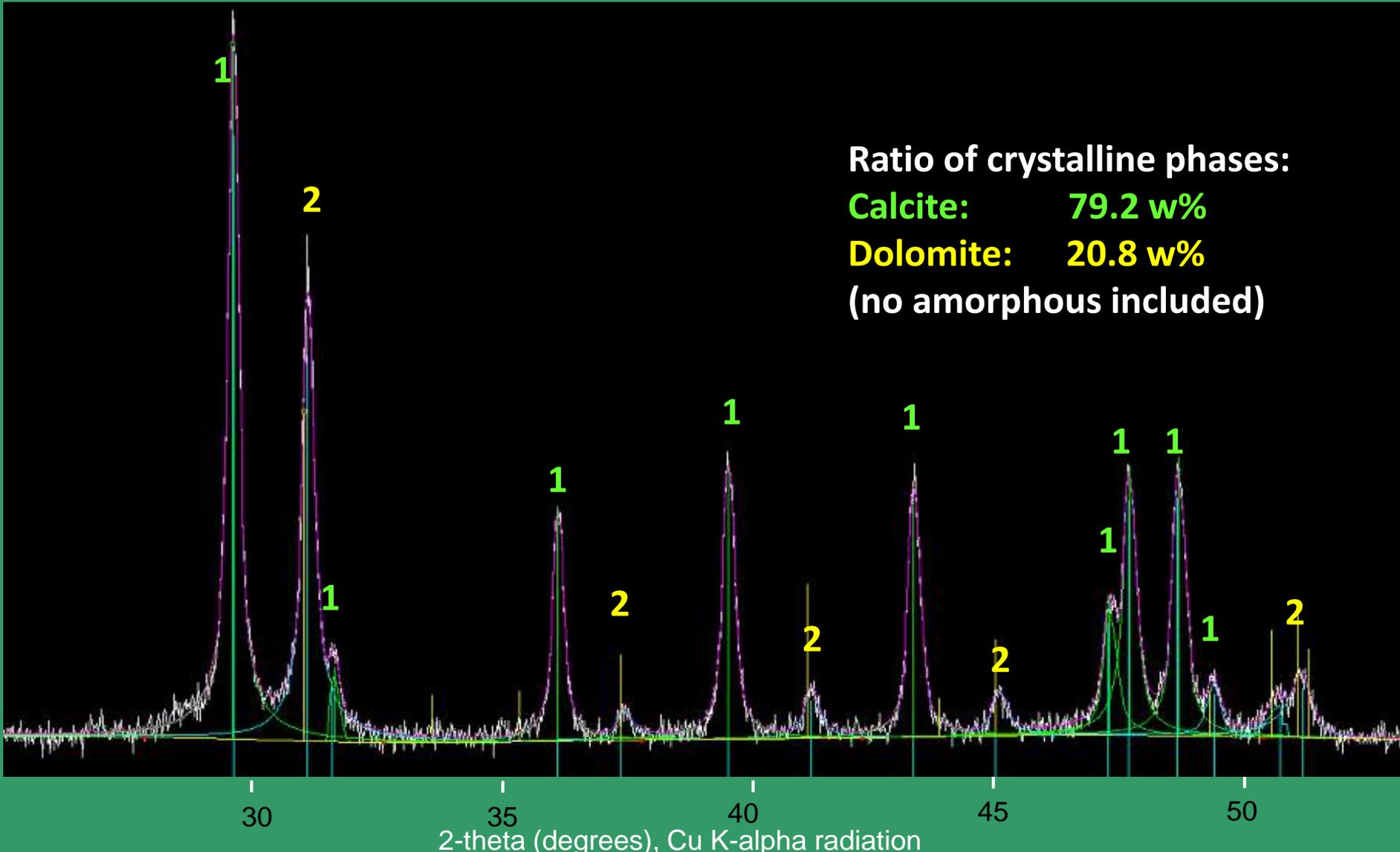
	Hits	Formula	FOM	PDF	RIR	Space group
✓	Calcite	$\text{CaCO}_3$	1.1	04-012-0489	3.45	R-3c(167)
✓	Dolomite	$\text{Ca}_{1.07}\text{Mg}_{0.93}(\text{CO}_3)_2$	15.0	04-011-9830	2.51	R-3(148)

# Quant: RIR reference intensity ratio

$$\left( \begin{array}{c} \text{Ratio of} \\ \text{crystalline} \\ \text{phases} \end{array} \right) \sim \left( \begin{array}{c} \text{Ratio of peak areas corrected} \\ \text{by RIR of each phase} \end{array} \right)$$

$$\text{RIR} \sim I / I_{\text{corundum}}$$

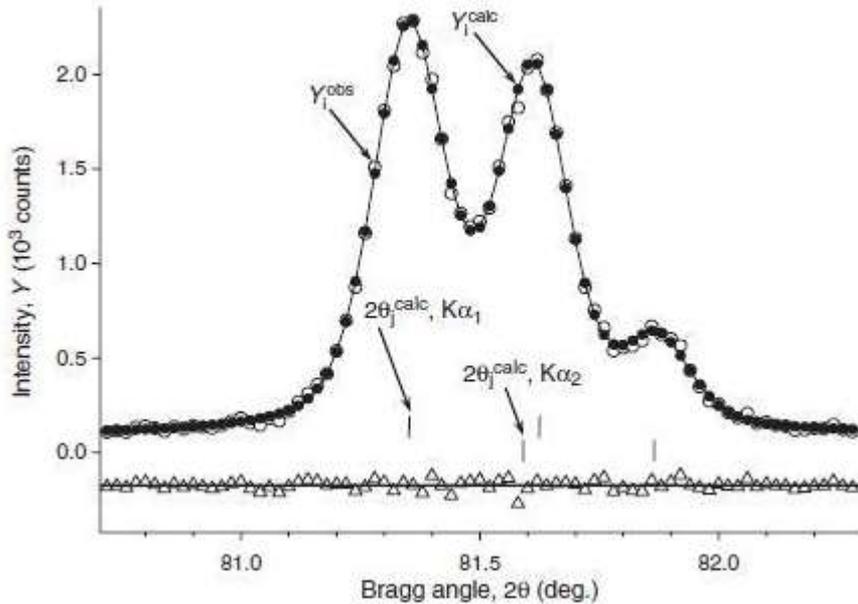
Intensity (sqrt counts)



# Rietveld refinement



H. Rietveld  
(1932-2016)



Non-linear least square minimization

For each data point  $i$ :

$$Y_1^{calc} = kY_1^{obs}$$

$$Y_2^{calc} = kY_2^{obs}$$

...

$$Y_n^{calc} = kY_n^{obs}$$

Minimize this function:

$$\Phi = \sum_{i=1}^n w_i (Y_i^{obs} - Y_i^{calc})^2$$

Sum over  $n$  data points

$$\Phi = \sum_{i=1}^n w_i (Y_i^{obs} - [b_i + \sum_{l=1}^p K_l \sum_{j=1}^m I_{l,j} y_{l,j}(x_{l,j})])^2$$

$n$  data points

$p$  phases

$m$  Bragg reflections for each data  $i$

$w_i, b_i, K_p, Y_{l,j}$  weight, background, scale factor and peak shape function

Data + preliminary structure:



Refinement of parameters:

Background

Sample displacement, transparency and zero-shift correction

Peak shape function

Unit cell dimensions

Preferred orientation

Scale factors

Atom positions in the structure

Atomic displacement parameters

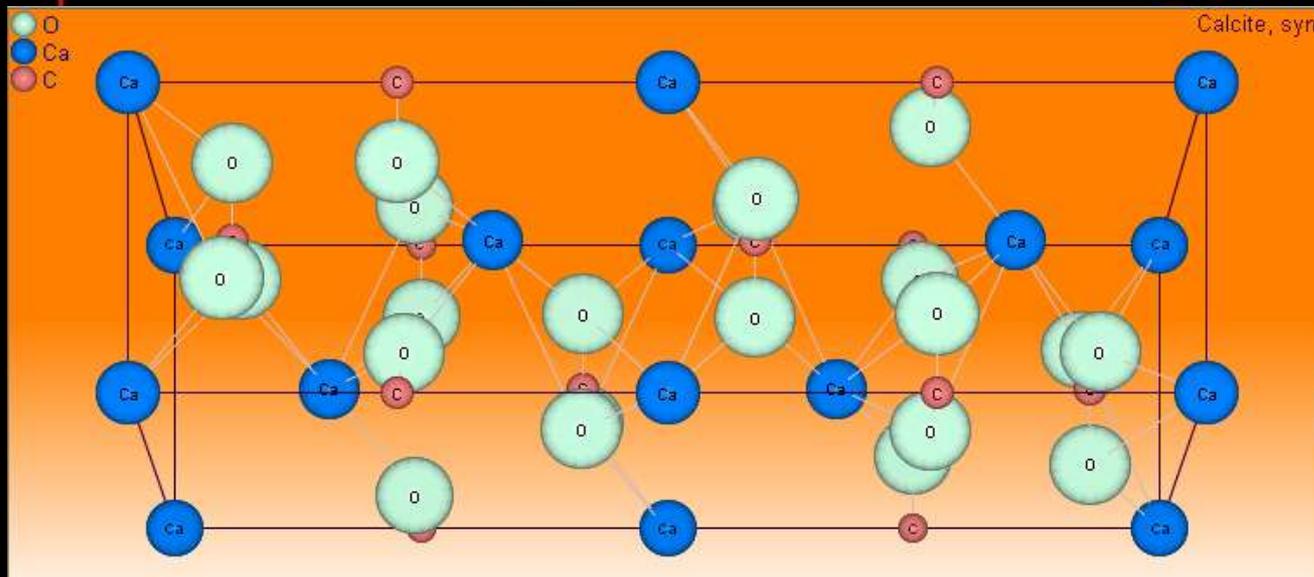
Minimize and converge figures of merit/quality:

$R$



# Rietveld refinement

Intensity (sqrt counts)



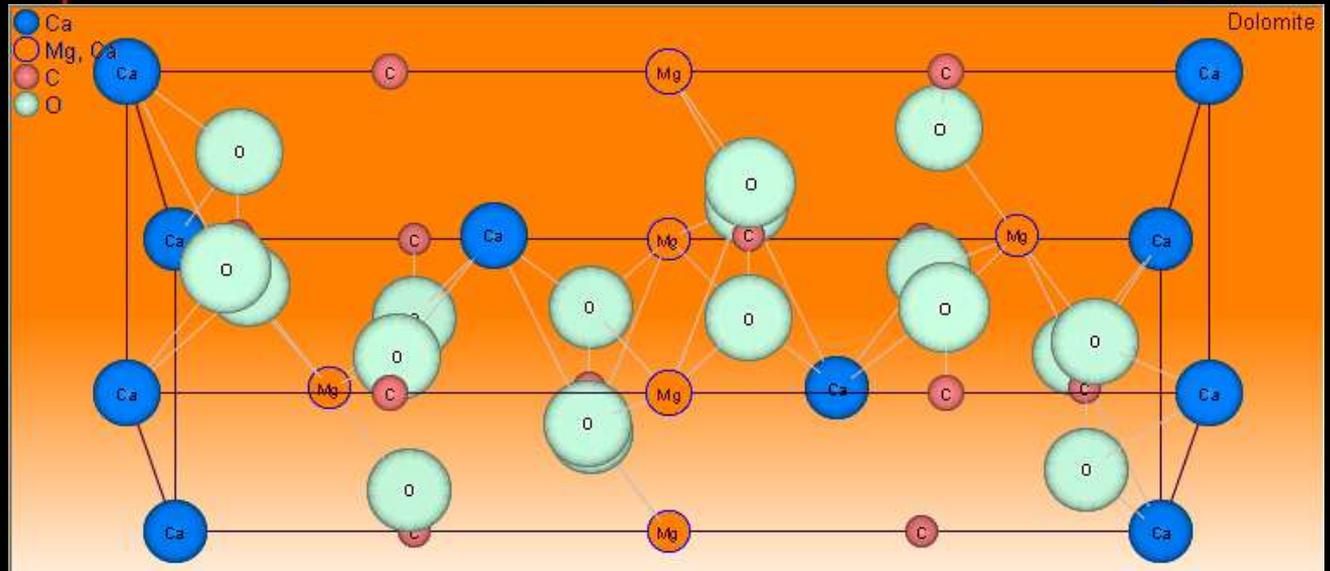
Calcite, CaCO<sub>3</sub>, hexagonal, R $\bar{3}c$  (167)  
0.499 nm/ 0.499 nm / 1.705 nm <90.0/90.0/120.0>

20 30 40 50 60 70 80 90 100 110

2-theta (degrees), Cu K-alpha radiation

# Rietveld refinement

Intensity (sqrt counts)



Dolomite,  $\text{Ca}_{1.07}\text{Mg}_{0.93}(\text{CO}_3)_2$ , hexagonal,  $R3\ (\bar{1}48)$   
0.481 nm / 0.4819 nm / 1.602 nm  $\langle 90.0/90.0/120.0 \rangle$

20 30 40 50 60 70 80 90 100 110

2-theta (degrees), Cu K-alpha radiation

~ XRD, TEM

~ SEM

~ SEM (number average)  
SAXS (volume average),  
DLS (volume<sup>2</sup> average), ...

**Crystallite  
size**

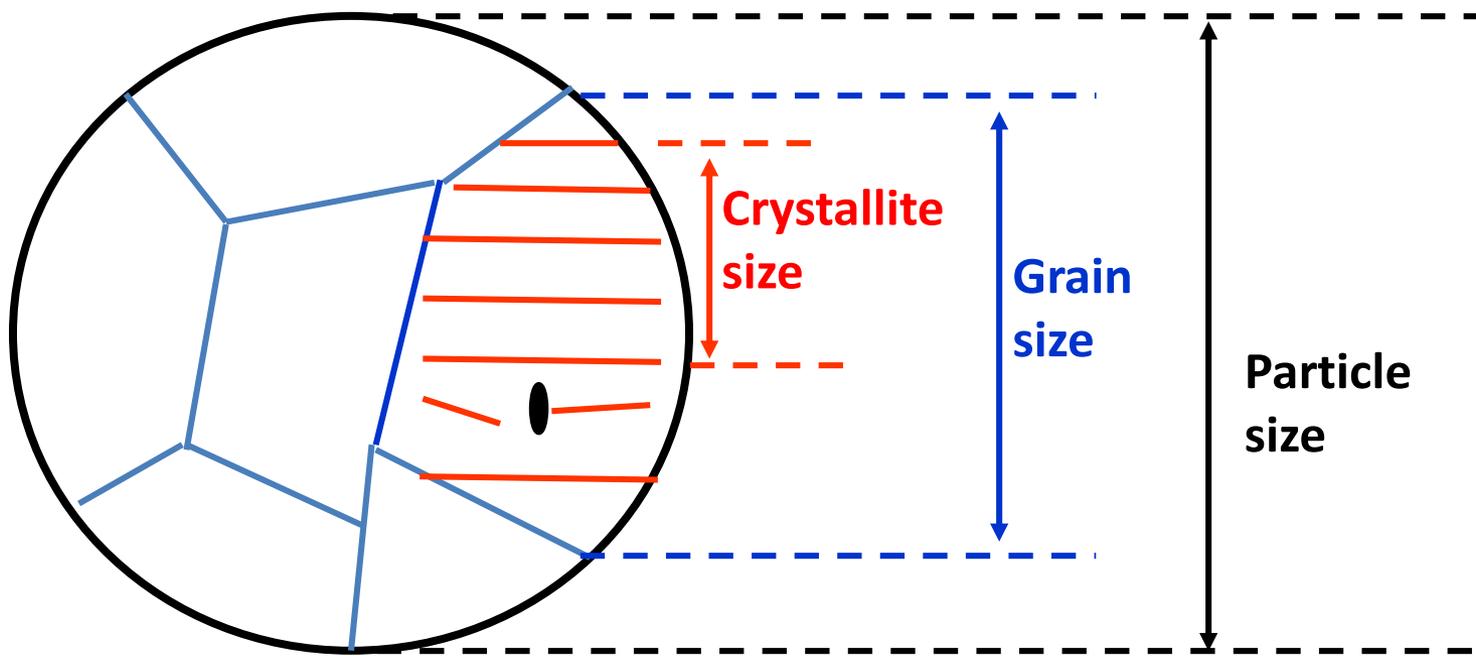
$\leq$

**Grain  
size**

$\leq$

**Particle  
size**

Domain of  
coherent  
diffraction



# Crystallite size analysis

## Scherrer's equation:

$$\text{Size} = \frac{k * \lambda}{\cos(\theta) * (\text{FWHM})}$$

$k$ : shape factor (0.8-1.2)

$\lambda$ : x-ray wavelength

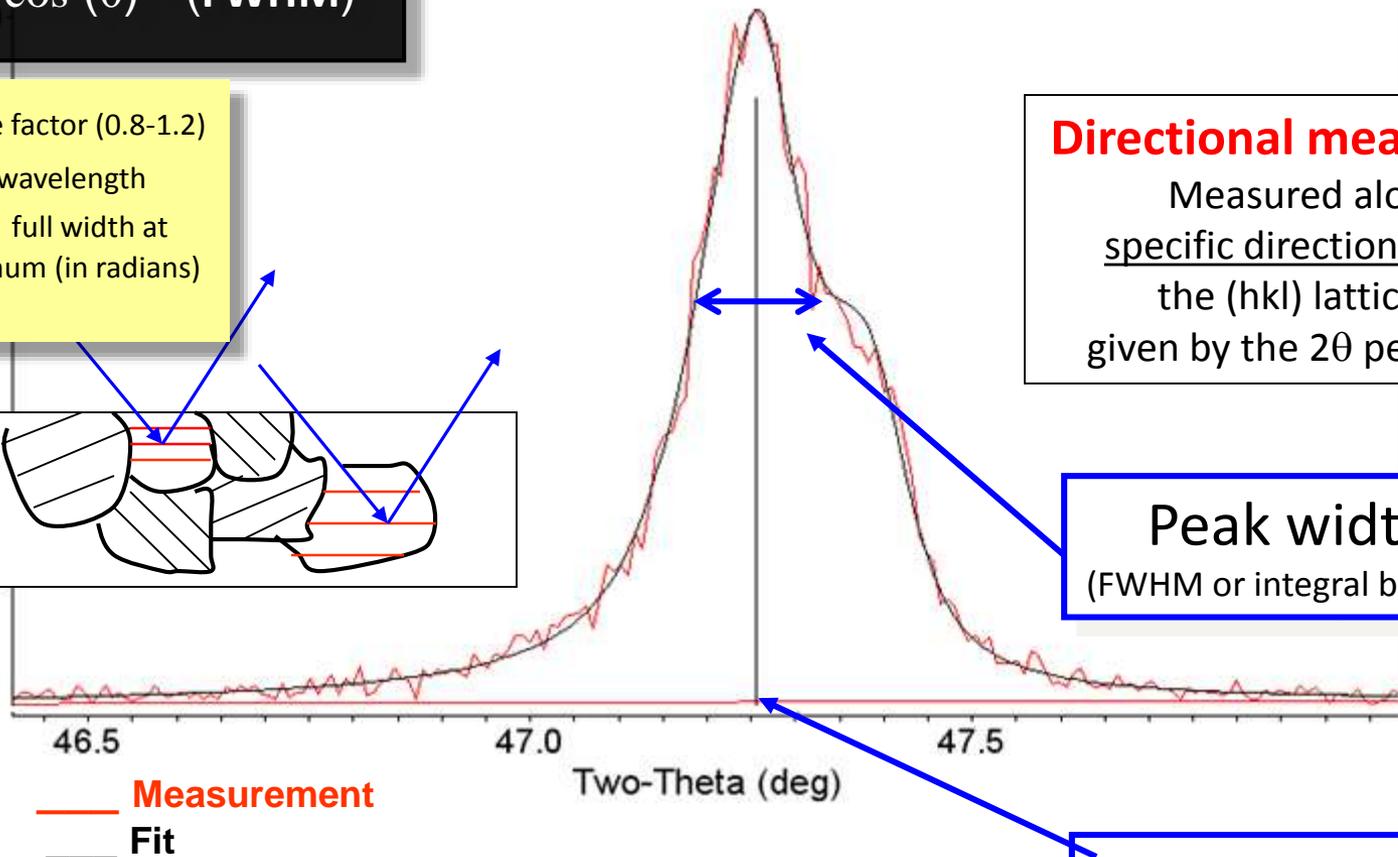
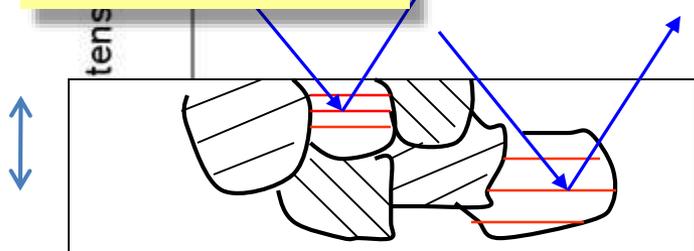
**FWHM**: full width at half maximum (in radians)

**Simplistic approximation!**

Not accounting for peak broadening from strain and defects

**Directional measurement!**

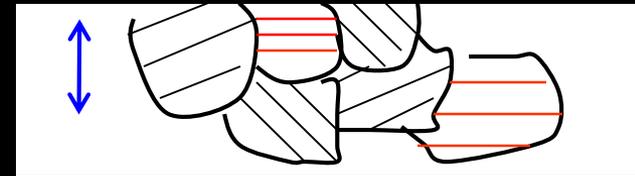
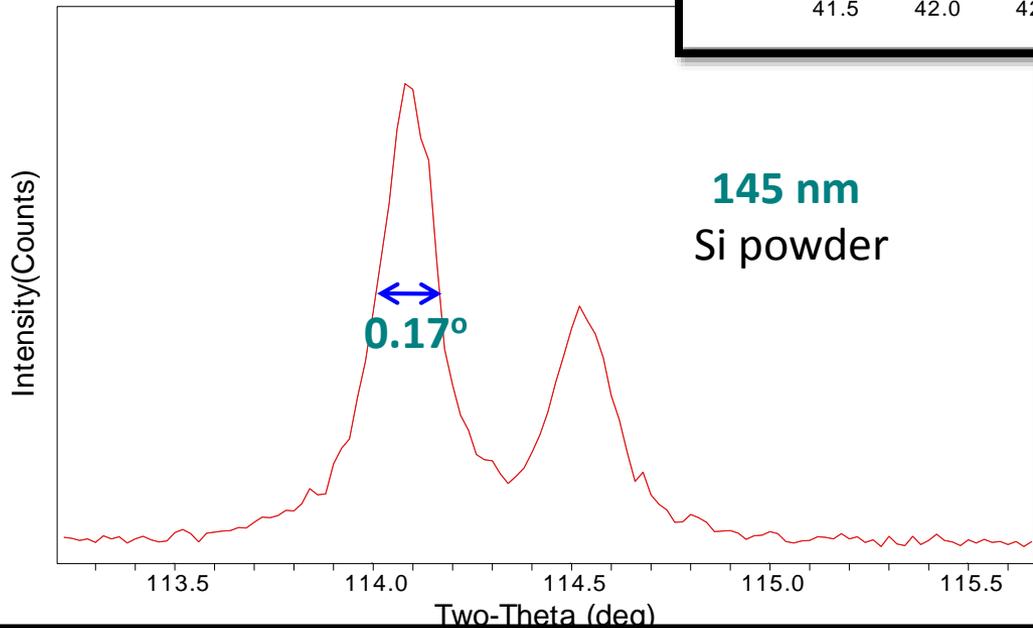
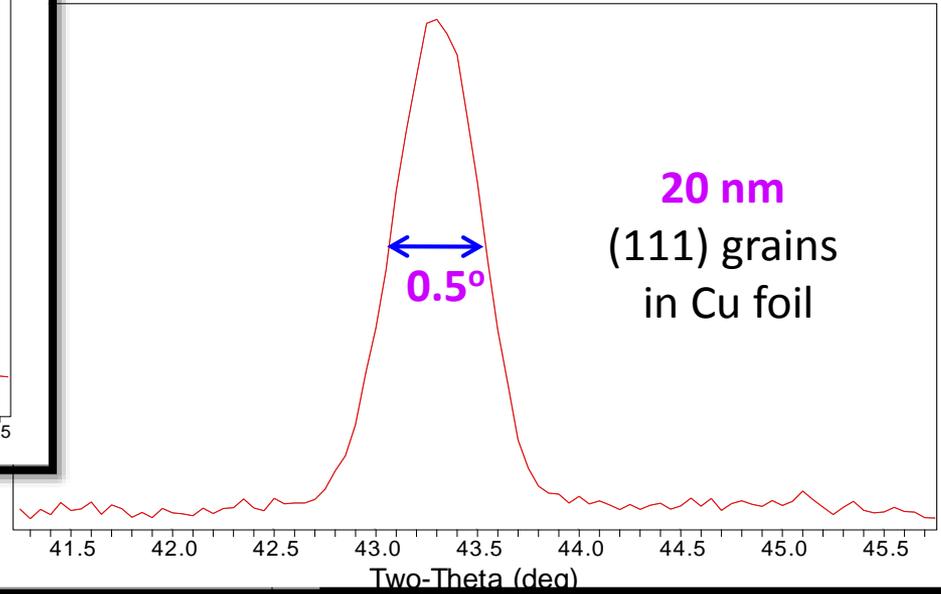
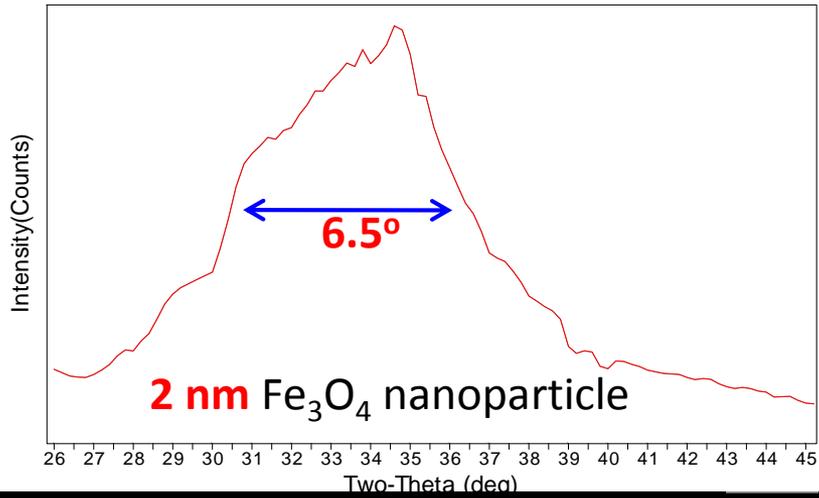
Measured along the specific direction normal to the (hkl) lattice plane given by the  $2\theta$  peak position



**Peak width**  
(FWHM or integral breadth)

**Peak position  $2\theta$**

# Crystallite size analysis



# Peak shape analysis

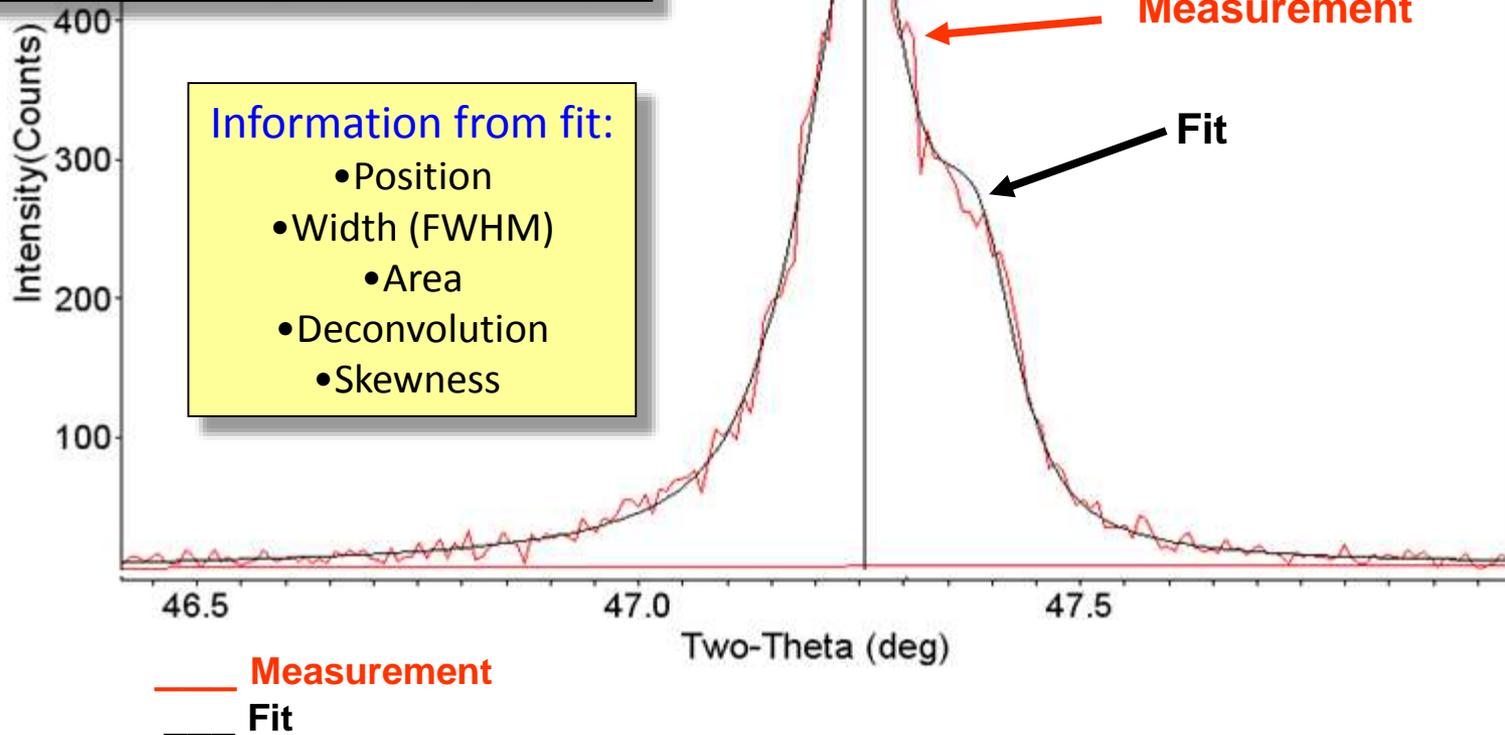
## Peak fit functions:

*Gaussian*

*Lorentzian*

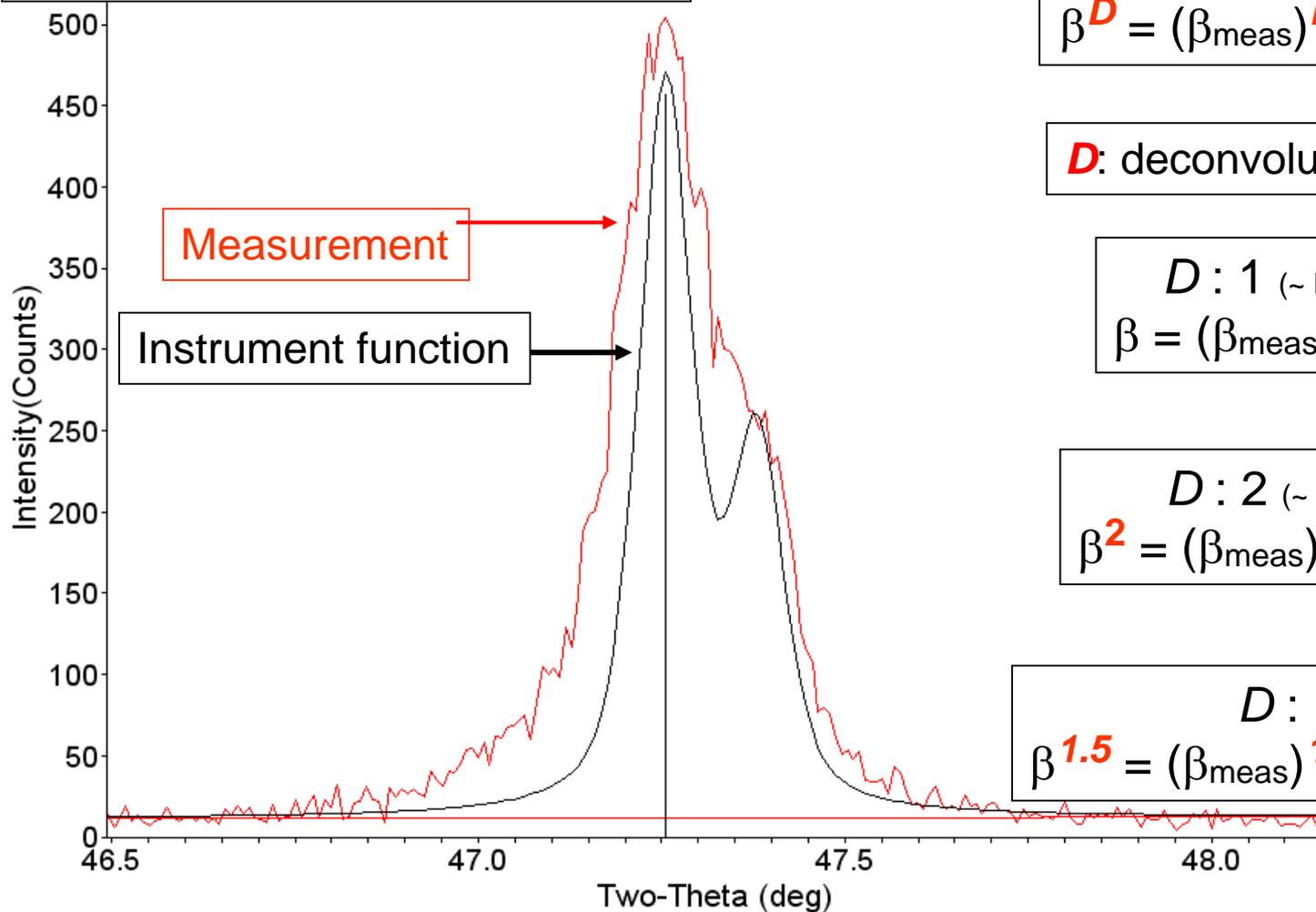
*Pearson-VII* (sharp peaks)

*Pseudo-Voigt* (round peaks)



# Correction for instrument resolution

Use FWHM curve as a function of  $2\theta$  from standard sample (NIST LaB<sub>6</sub>): specific for each diffractometer



FWHM:  $\beta$

$$\beta^D = (\beta_{\text{meas}})^D - (\beta_{\text{instr}})^D$$

$D$ : deconvolution parameter

$D : 1$  (~ Lorentzian)

$$\beta = (\beta_{\text{meas}}) - (\beta_{\text{instr}})$$

$D : 2$  (~ Gaussian)

$$\beta^2 = (\beta_{\text{meas}})^2 - (\beta_{\text{instr}})^2$$

$D : 1.5$

$$\beta^{1.5} = (\beta_{\text{meas}})^{1.5} - (\beta_{\text{instr}})^{1.5}$$

# Potential artifacts in size determination

For this calculation assume:

- Instrument resolution  $\sim 0.15^\circ$
- Cu radiation

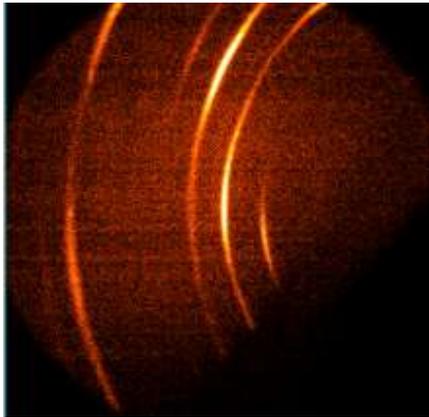
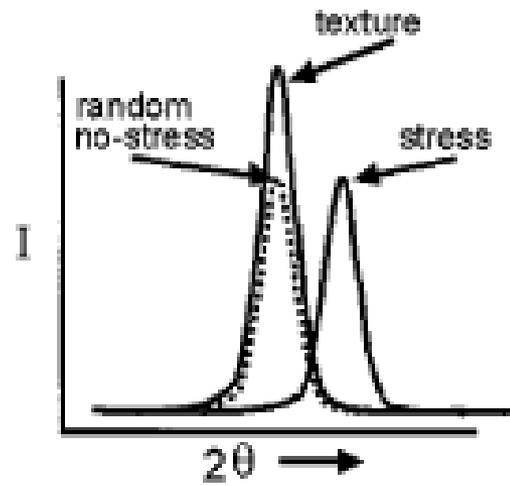
$2\theta = 40^\circ$ Measured peak width	Size, nm $D = 1$ (Lorentzian) $\beta = \beta_{\text{meas}} - \beta_{\text{instr}}$	Size, nm $D = 1.5$ $\beta^{1.5} = (\beta_{\text{meas}})^{1.5} - (\beta_{\text{instr}})^{1.5}$	Size, nm $D = 2$ (Gaussian) $\beta^2 = (\beta_{\text{meas}})^2 - (\beta_{\text{instr}})^2$
<b>0.30°</b>	<b>56.4</b>	<b>38.0</b>	<b>32.6</b>
<b>0.50°</b>	<b>24.2</b>	<b>19.2</b>	<b>17.7</b>
<b>0.75°</b>	<b>14.1</b>	<b>12.0</b>	<b>11.5</b>
<b>1.00°</b>	<b>10.1</b>	<b>8.8</b>	<b>8.6</b>
<b>1.50°</b>	<b>6.3</b>	<b>5.8</b>	<b>5.7</b>
<b>2.00°</b>	<b>4.6</b>	<b>4.3</b>	<b>4.2</b>

**~ 48% difference for narrow peaks (large sizes)**

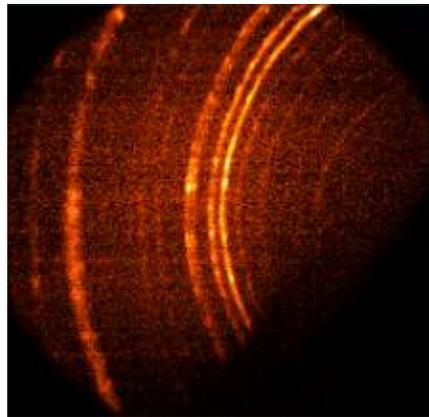
**Smaller difference (~ 10%) for broad peaks (small sizes)**



Small grains,  
No texture

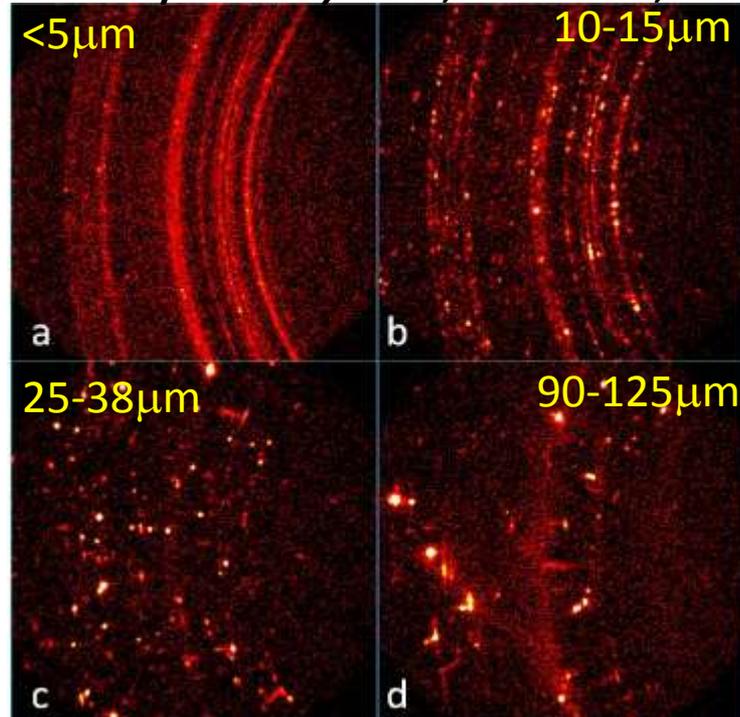


Non uniform  
rings  
(texture)

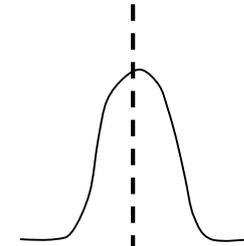


Spotty  
rings  
(large  
grain  
size)

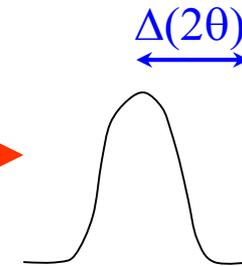
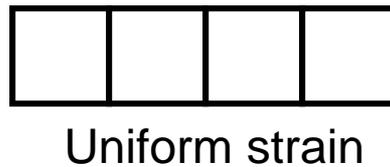
**Pyroxene: increasing grain sizes**  
Collected by *Curiosity* rover, Gale crater, Mars



# Strain effects in diffraction lines

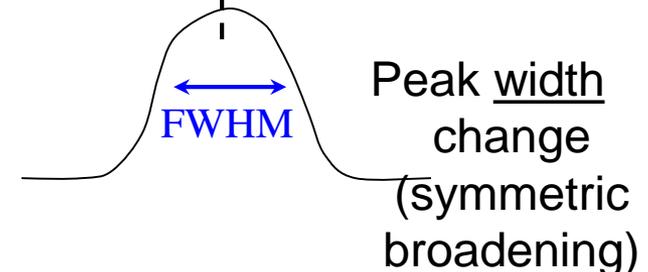
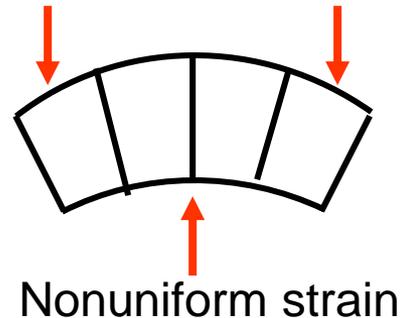


**Macrostrain**  
uniform tensile or  
compressive stress  
(lattice expansion or  
contraction)



Peak position  
shift  
(lattice constant  
change)

**Microstrain**  
nonuniform strain  
(both tensile and  
compressive stresses)  
(lattice distortion).  
Dislocations, vacancies,  
defects, thermal effects.



Peak width  
change  
(symmetric  
broadening)

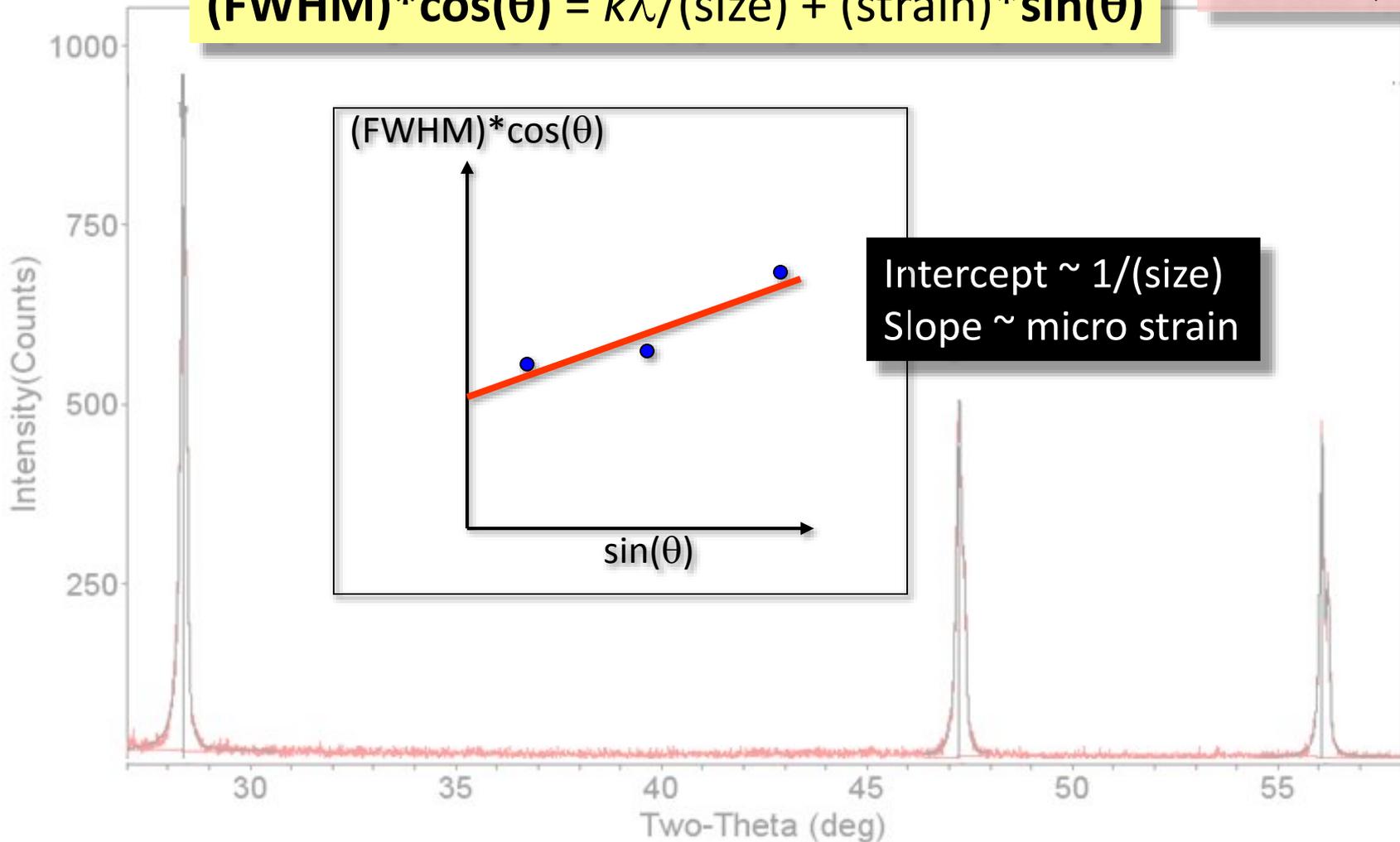
# Size and strain in peak shape analysis

$$\text{FWHM}_{\text{strain}} = 4 * (\text{strain}) * \tan \theta$$

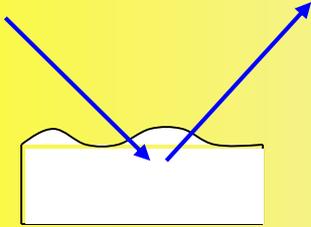
Williamson-Hall  
Method

*Acta Metall.* 1 (1953) 22.

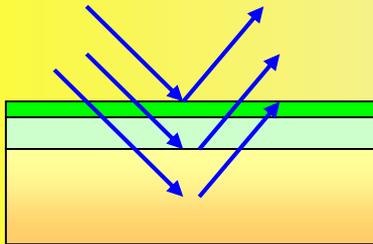
$$(\text{FWHM}) * \cos(\theta) = k\lambda / (\text{size}) + (\text{strain}) * \sin(\theta)$$



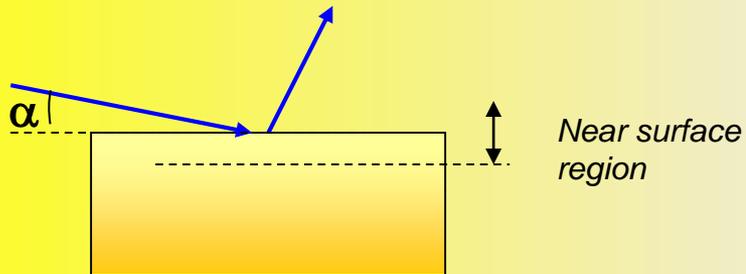
# X-ray parallel beam methods



Rough, irregular surfaces

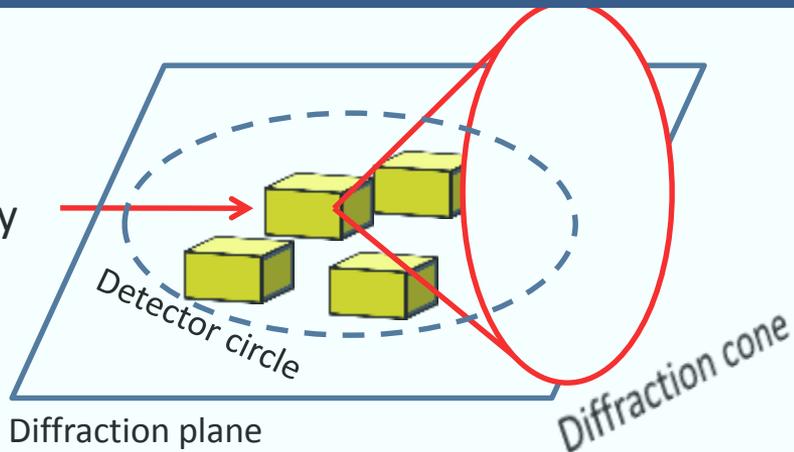


Film / Substrate systems

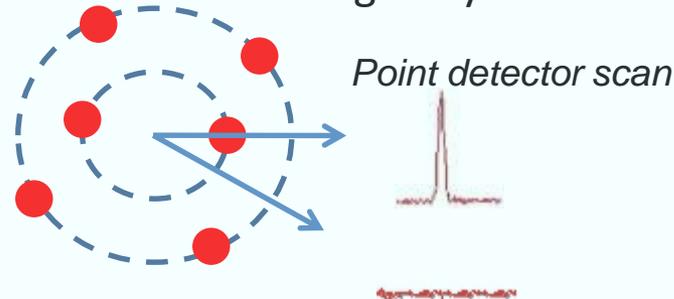


Glancing / grazing angle applications.  
Phase, stress gradients (depth profiles)

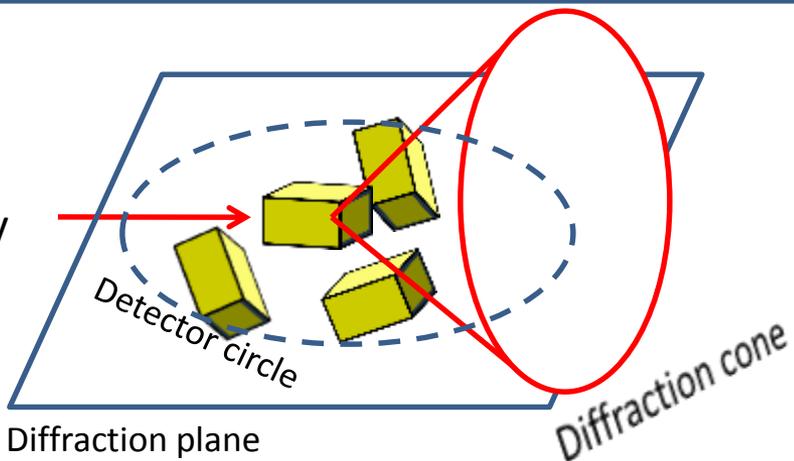
X-ray



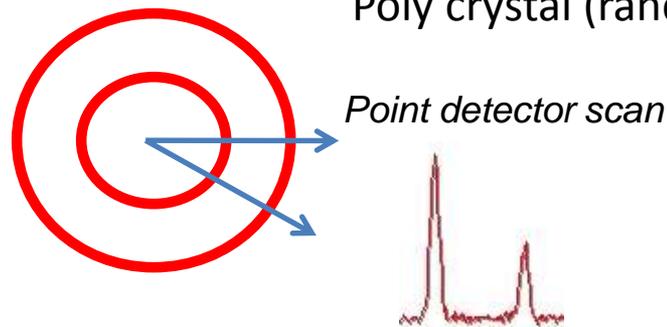
Single crystal



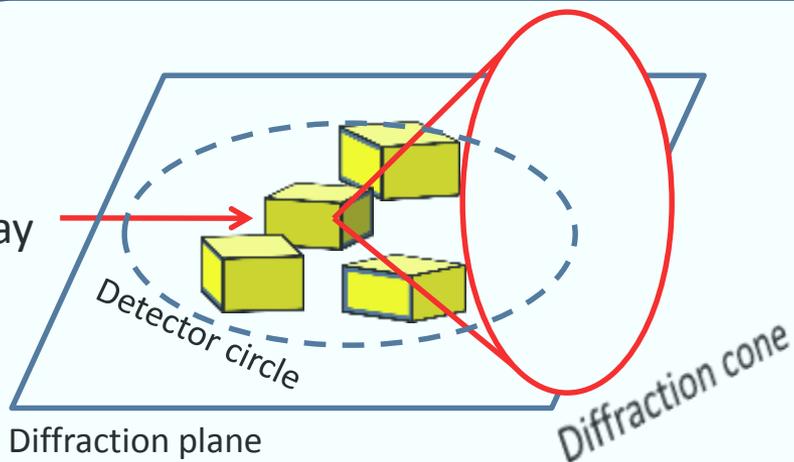
X-ray



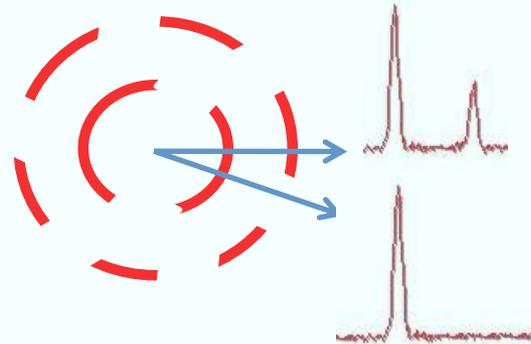
Poly crystal (random)



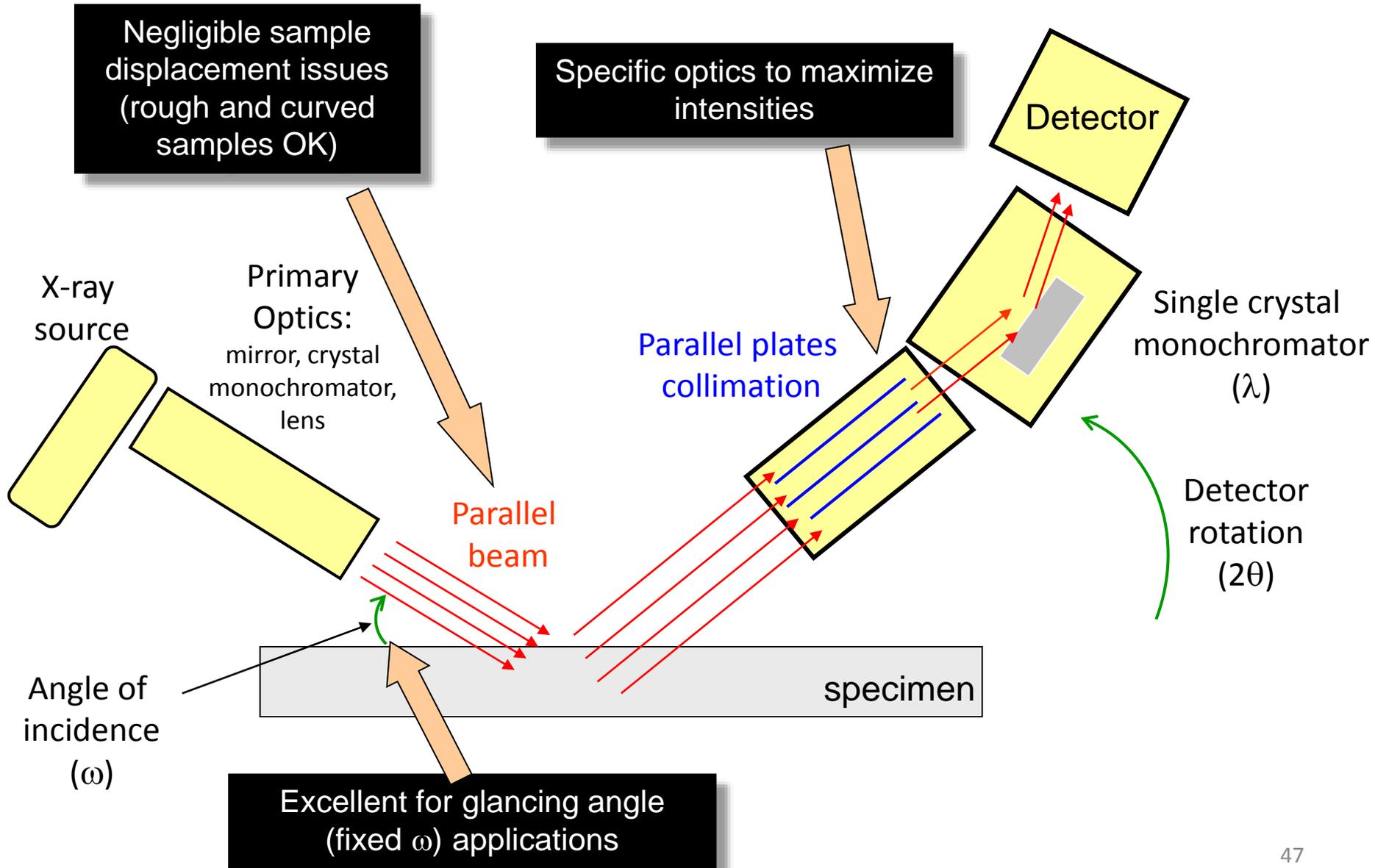
X-ray



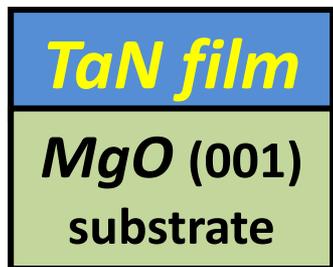
Poly crystal (texture)



# Parallel beam configuration



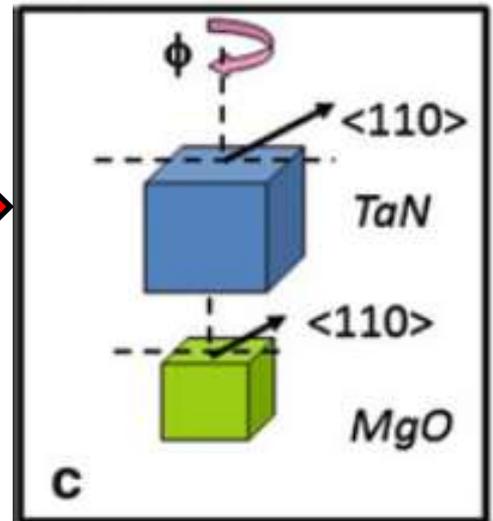
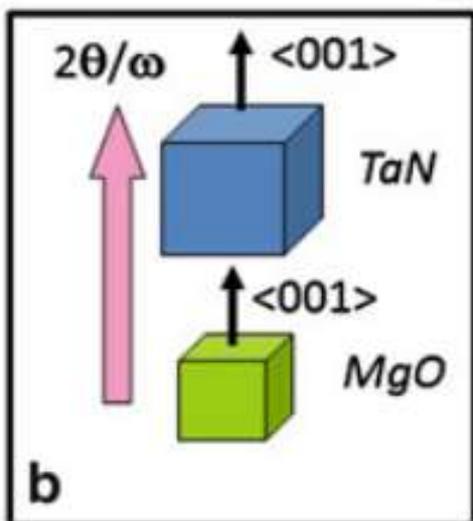
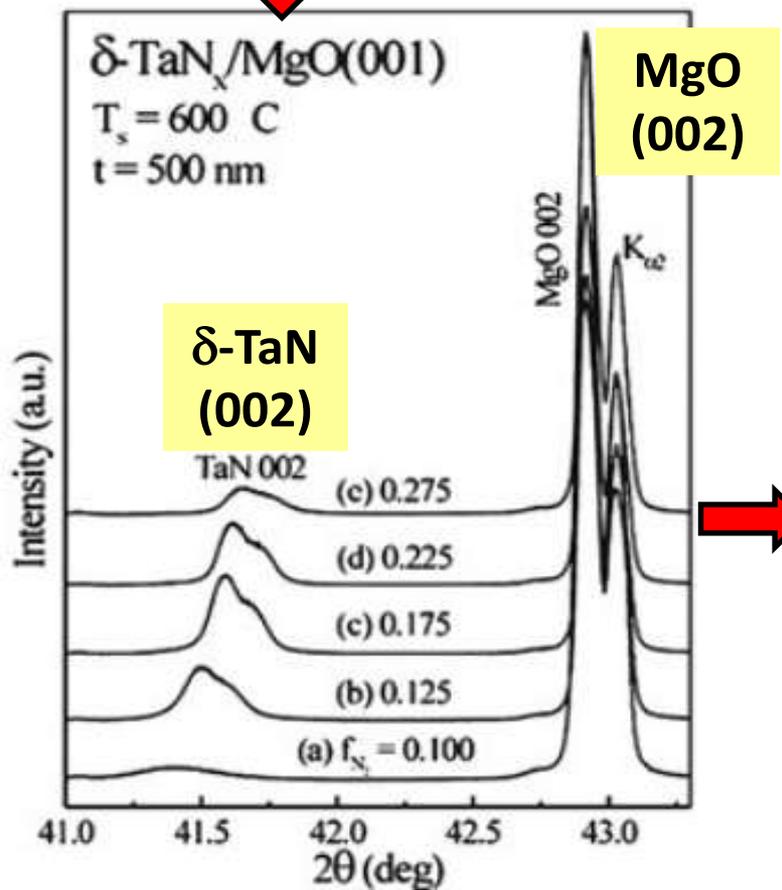
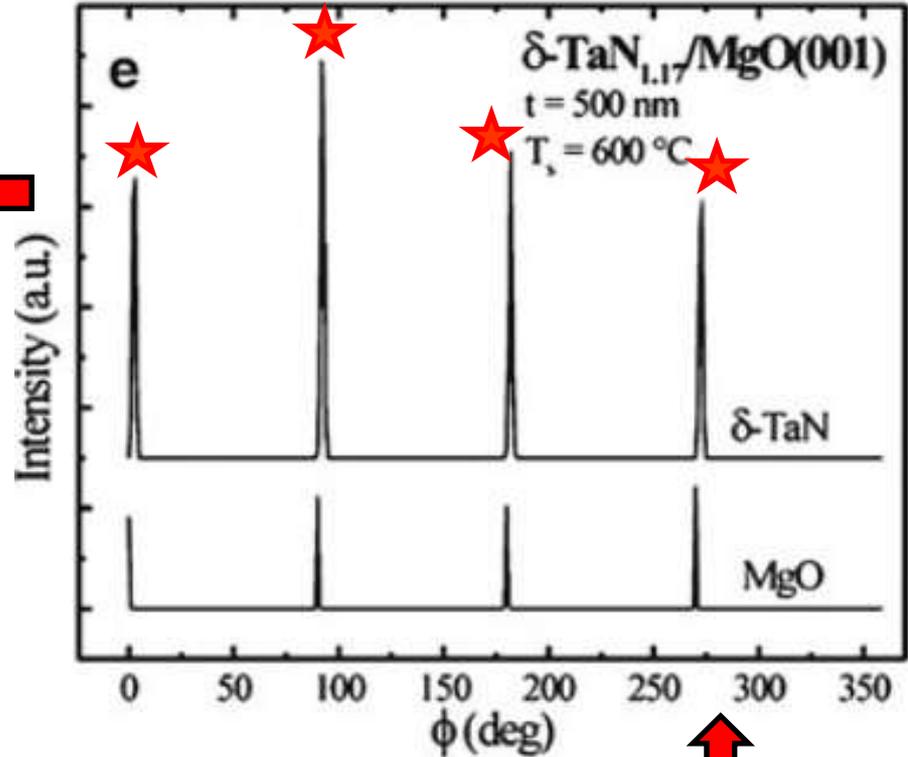
# Thin film analysis walkthrough:



Cube on cube epitaxy:

$(001)_{\text{TaN}} // (001)_{\text{MgO}}$

$(100)_{\text{TaN}} // (100)_{\text{MgO}}$

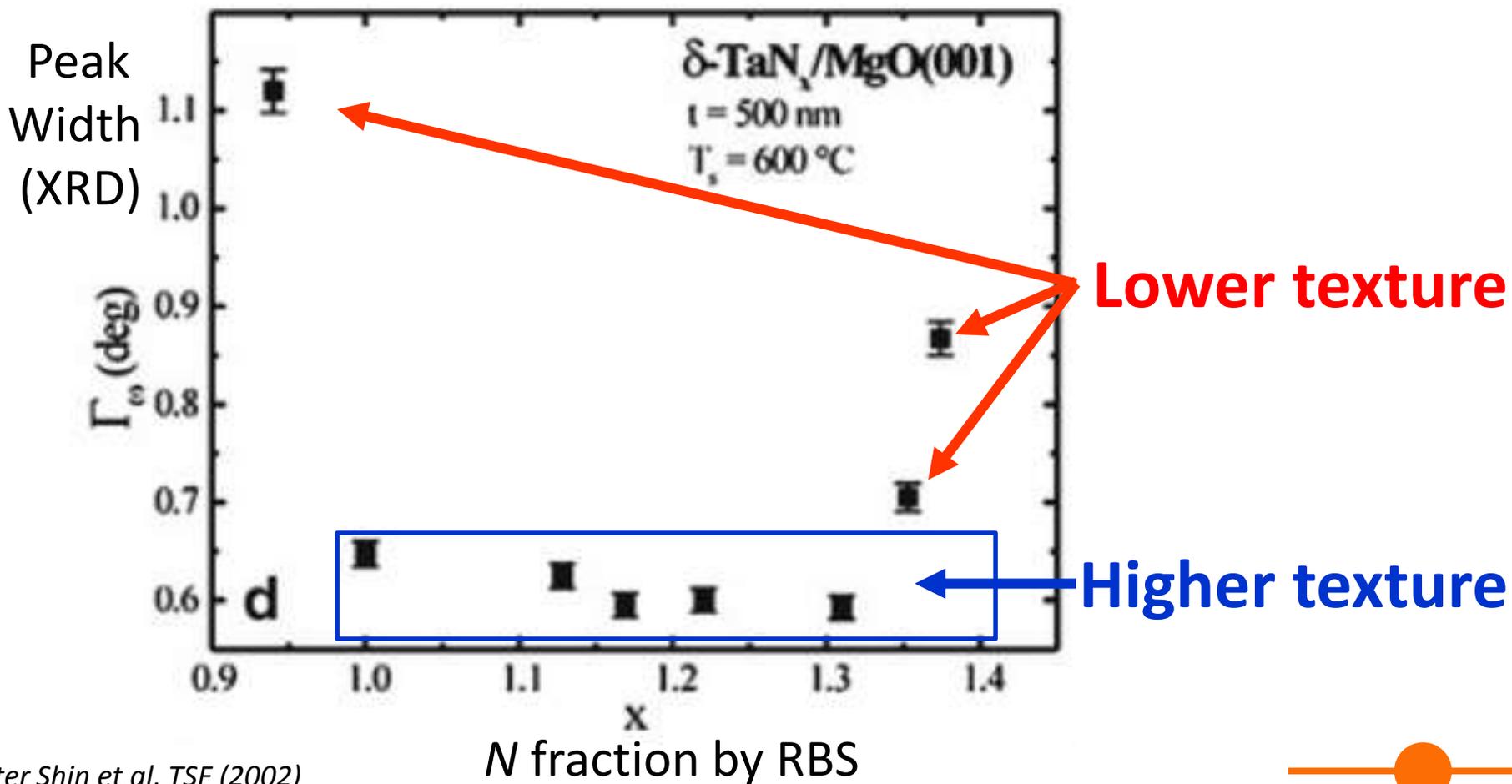


After Shin et al, TSF (2002)

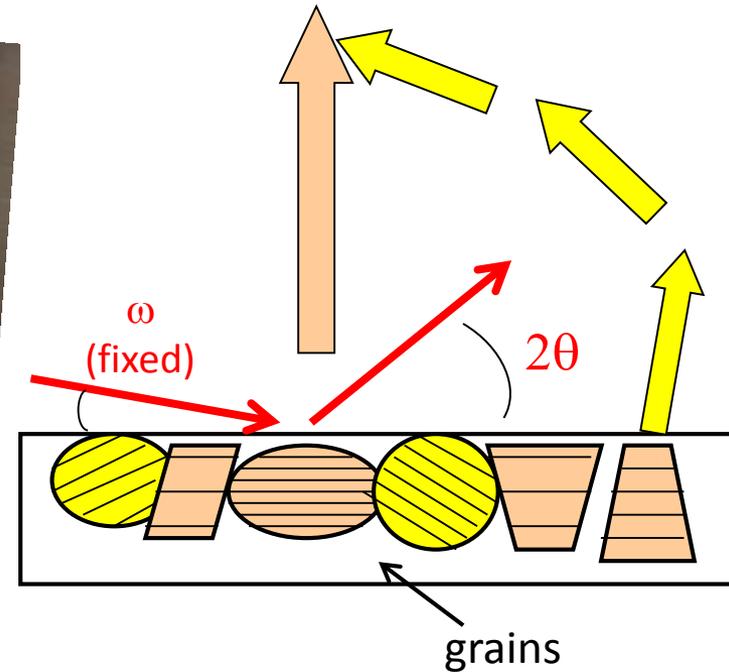
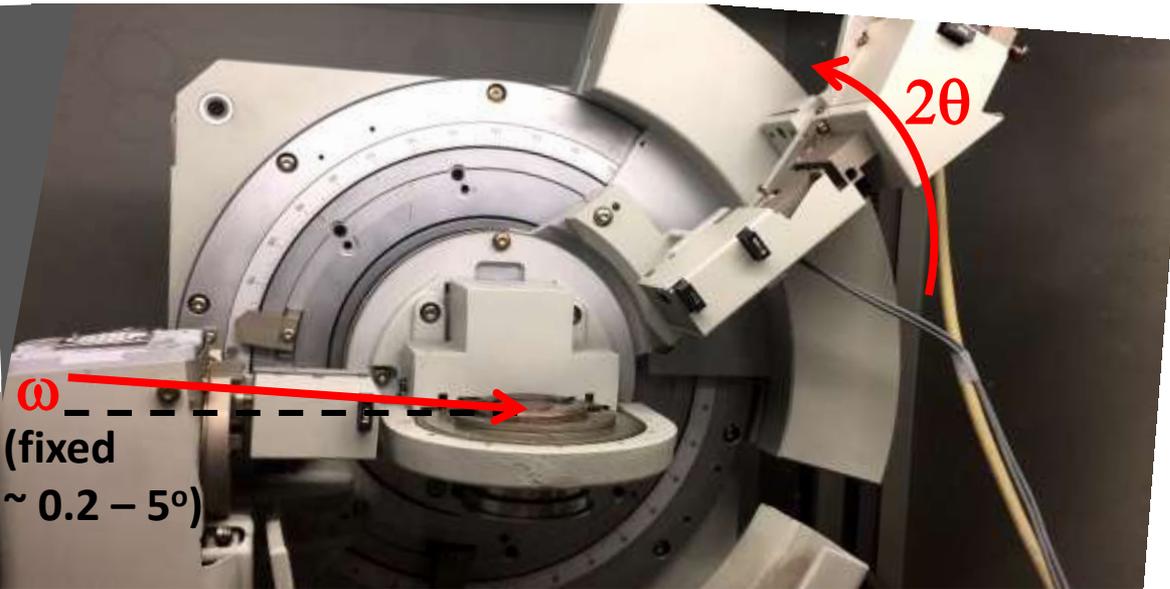
# Thin film analysis walkthrough:

## Peak shape analysis: TaN(002) rocking curve omega scans

**TaN film**  
**MgO (001)**  
substrate



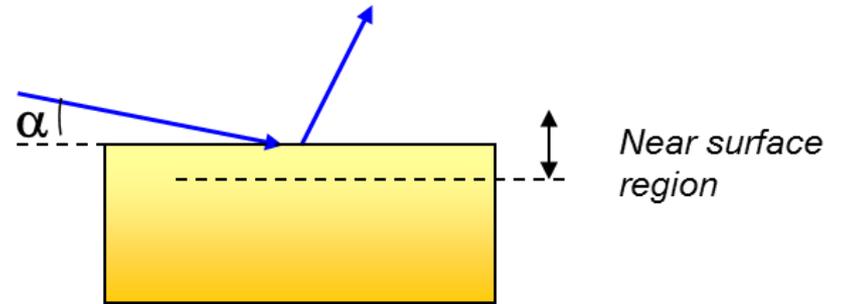
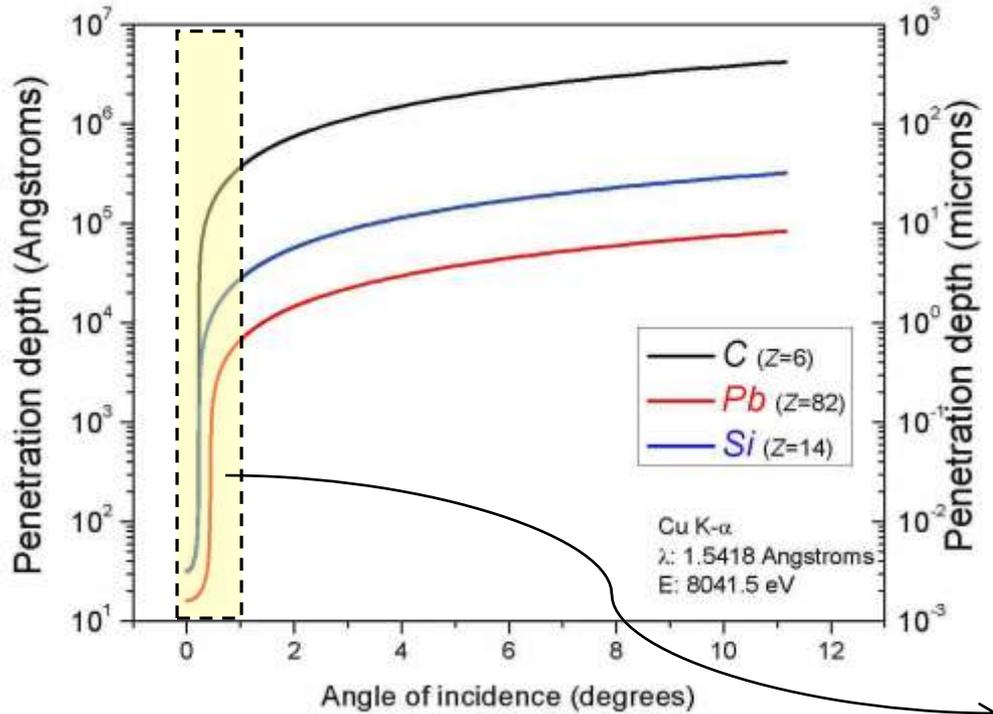
# Glancing incidence x-ray diffraction (GI-XRD)



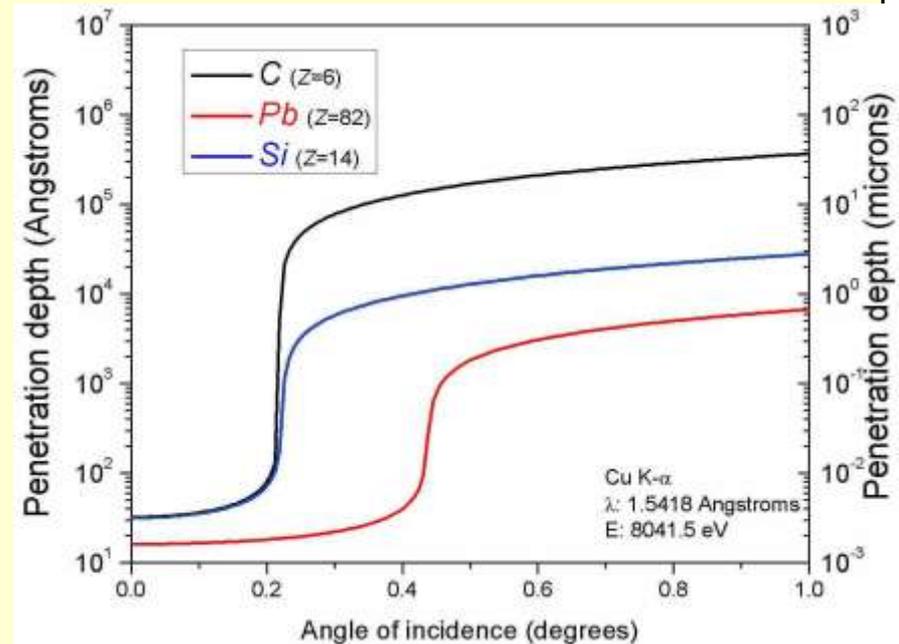
 : **conventional** Bragg-Brentano configuration  
 $2\theta$ - $\omega$  scans probe only grains aligned parallel to the surface

 +  : parallel-beam **glancing incidence** configuration  
 $2\theta$  scans probe grains in all directions

# X-ray penetration depth vs. angle of incidence



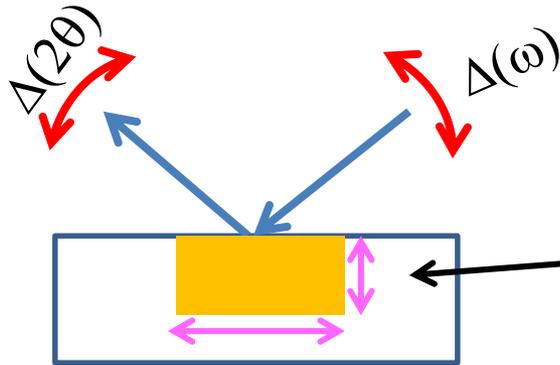
Low angle region



- Type of radiation
- Angle of incidence
- Material (Z, A, r, m)

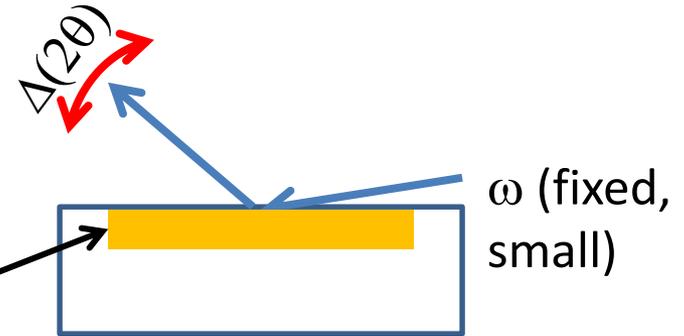
# Regular $2\theta$ - $\omega$ scan vs. glancing incidence $2\theta$ scan

Regular  $2\theta$ - $\omega$  scan



Probe depth:  
Variable (deep)  
Constant (shallow)

Glancing incidence  $2\theta$  scan

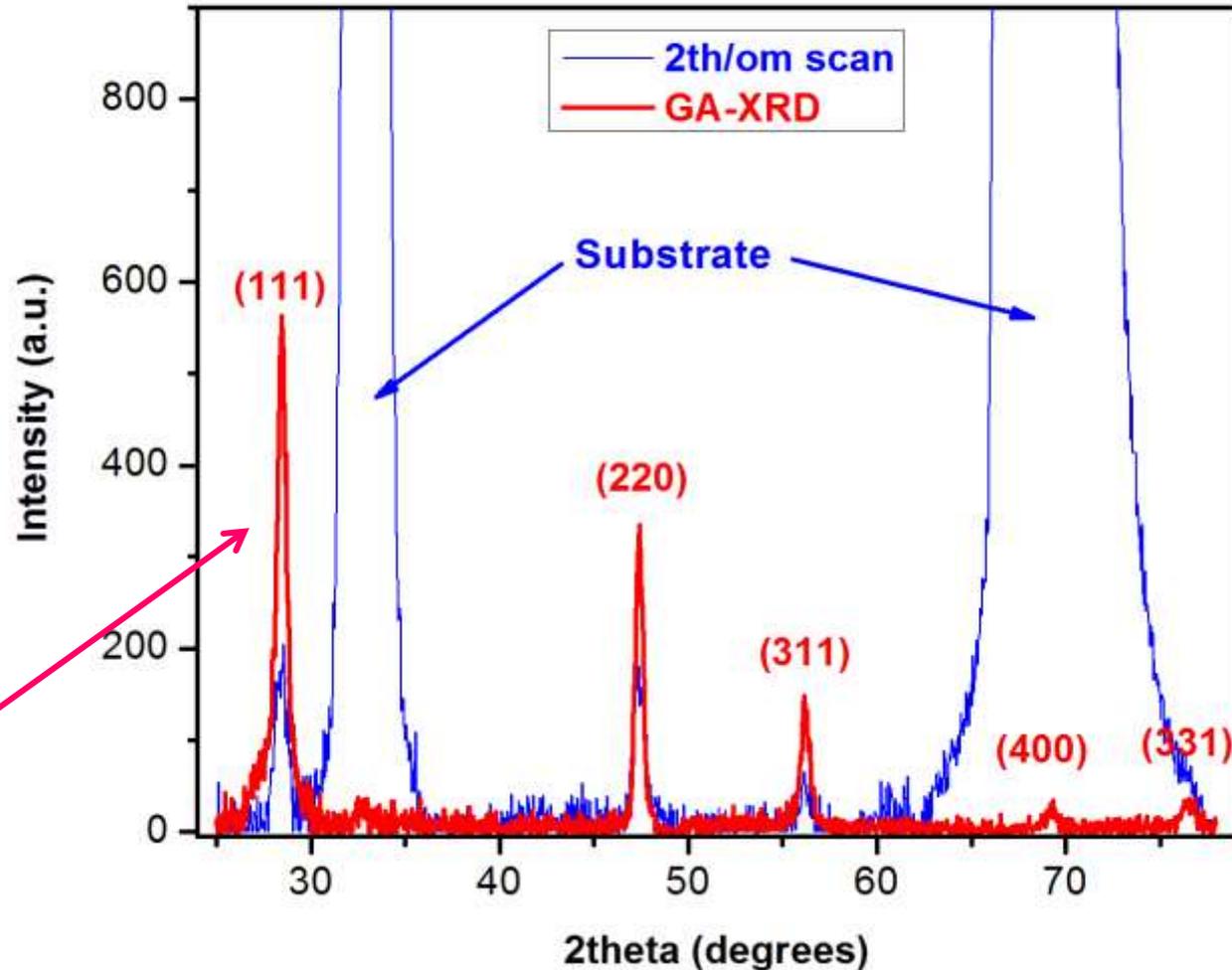


	Regular $2\theta$ - $\omega$ scan	Glancing incidence $2\theta$ scan
<b>Grain orientations</b>	Directions $\perp$ to surface	Various directions
<b>Depth resolution</b>	Constant, many mm	<ul style="list-style-type: none"> <li>From few nm to mm</li> <li><u>Depth profiling</u> possible by varying angle of incidence</li> <li>Sensitive to surface</li> <li>Ideal for ultra-thin layers</li> </ul>
<b>Best configuration</b>	Bragg Brentano Parallel beam	Parallel beam (less sensitive to sample displacement)

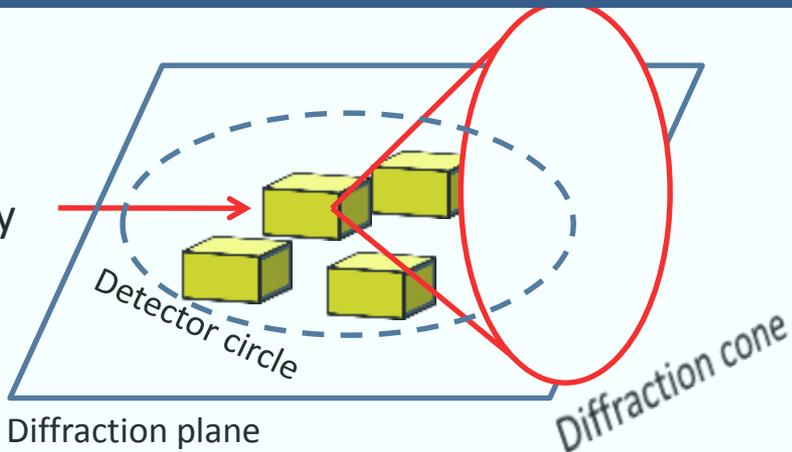
# Glancing incidence x-ray analysis

Example: Poly-Si  $\bar{g}$

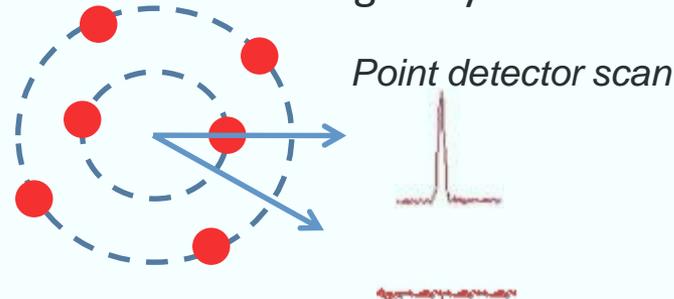
Poly-Si (~ 100 nm)
Si(001) substrate



X-ray

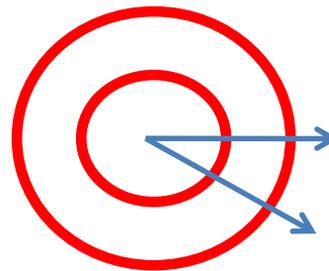
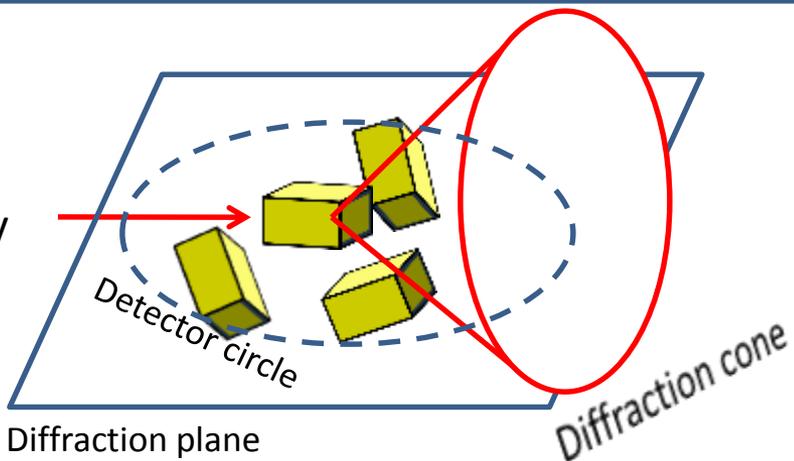


Single crystal



Poly crystal (random)

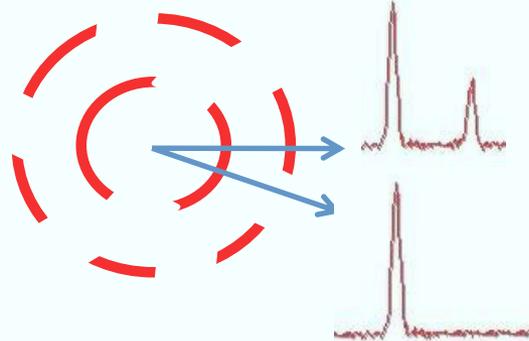
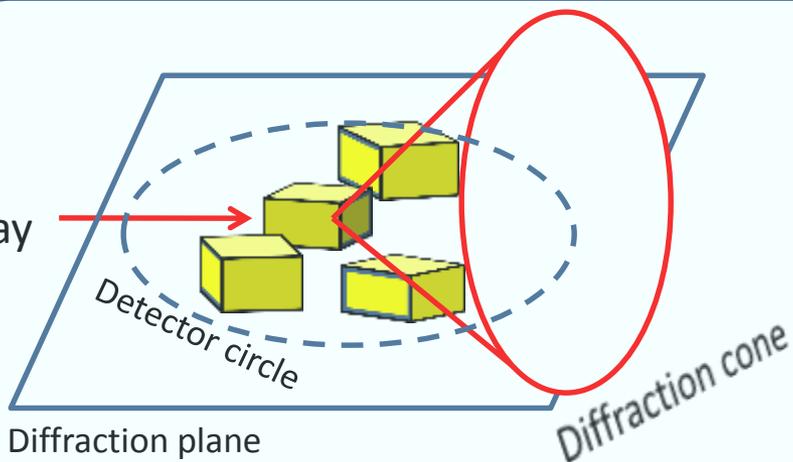
X-ray



Point detector scan

Poly crystal (texture)

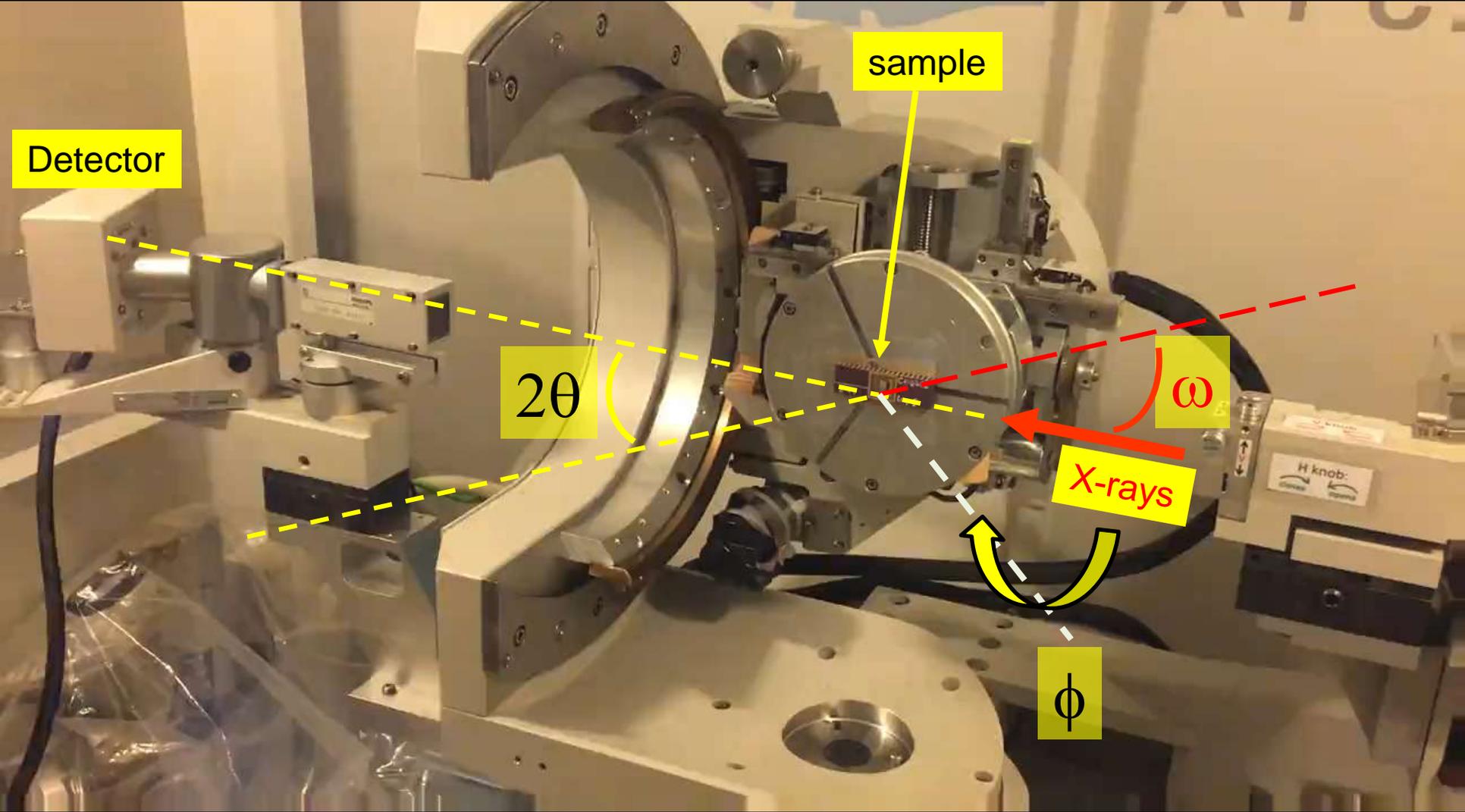
X-ray



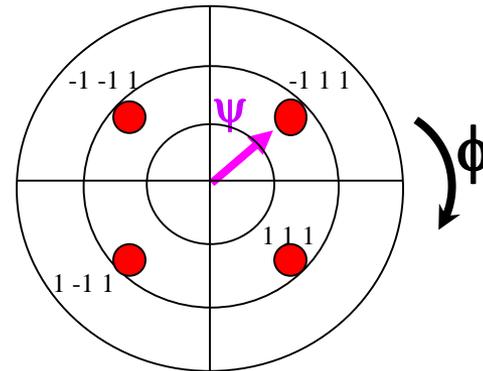
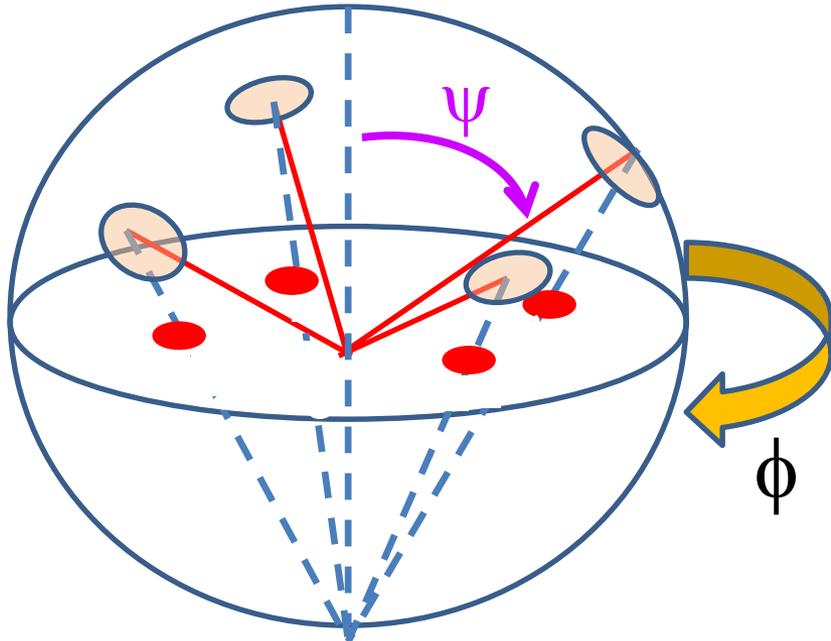
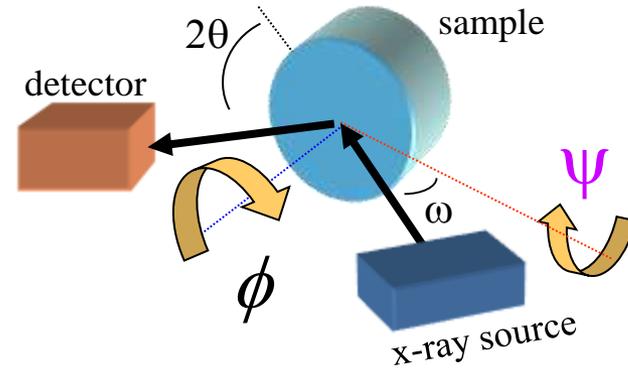
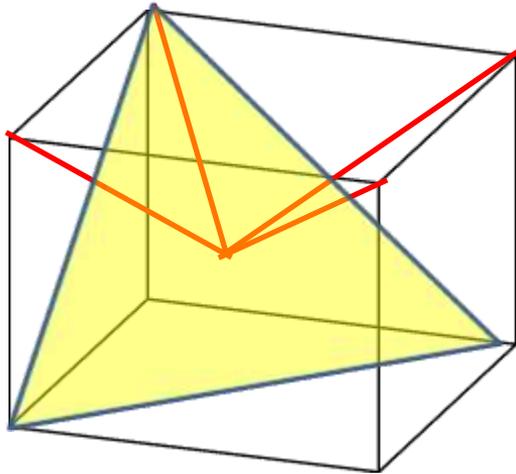
# Determination of preferred orientation

Method	Measurement	Principle	Results
<b>Lotgering factor</b> ( $L_{hkl}$ )	$2\theta$ - $\omega$ scans	Compare $I_{\text{peak}}$ or $A_{\text{peak}}$ with expected values from random samples (PDF)	$L_{hkl}$ as measure of texture strength
<b>March-Dollase</b> (MD)	$2\theta$ - $\omega$ scans	Use $I_{\text{peak}}$ or $A_{\text{peak}}$ with MD formalism	% of grains that are more oriented along a specific direction
<b>Rocking curve</b>	$\omega$ scans	Measure FWHM from $\omega$ scan for a particular ( $hkl$ )	FWHM decreases with stronger texture
<b>Pole figure</b>	$\phi$ scans at various tilts $\psi$	Pole plots of intensities from a particular ( $hkl$ )	Texture distribution for a single ( $hkl$ )
<b>Orientation Distribution Function</b> (ODF)	Pole figures from various ( $hkl$ )'s	Calculate ODF from various pole figures with background and defocussing correction	% of grain orientation distribution in all directions (Euler angles).

# Pole figure measurement



# Pole figures

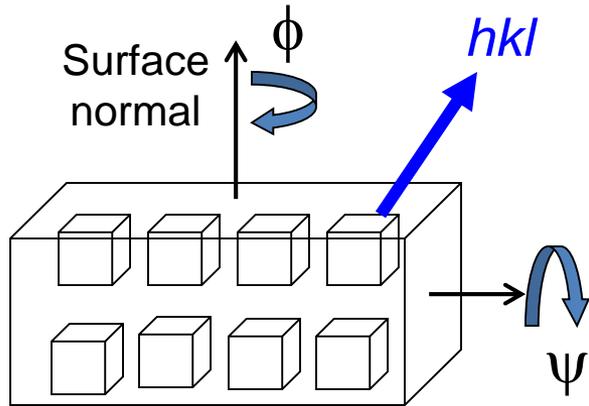


Azimuth  
 $\phi = 45^\circ, 135^\circ,$   
 $225^\circ, 315^\circ$

Tilt  $\psi = 54.7^\circ$

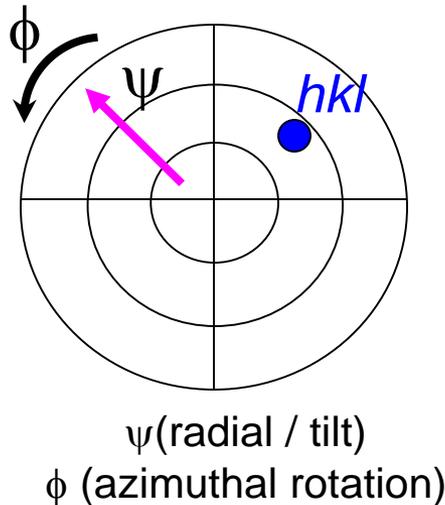
$\psi$ : [100],[111]

# Basics of pole figure analysis

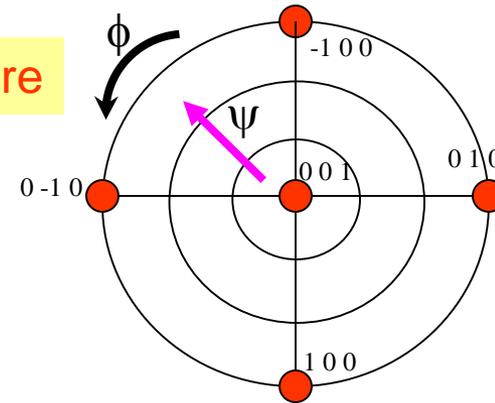
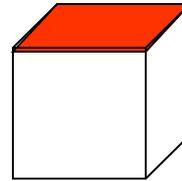


Example: (100) cubic crystal

Pole figure plot



(100) Pole figure

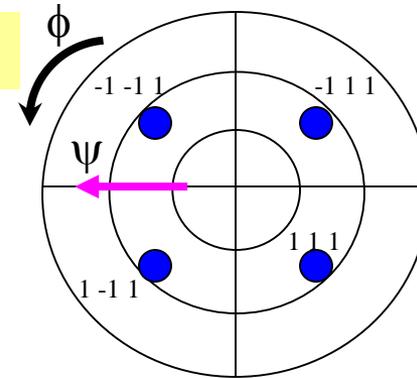
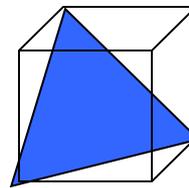


Azimuth  
 $\phi = 0, 90^\circ, 180^\circ, 270^\circ$

Tilt  
 $\psi = 0, 90^\circ$

$\psi: [100], [100]$

(111) Pole figure

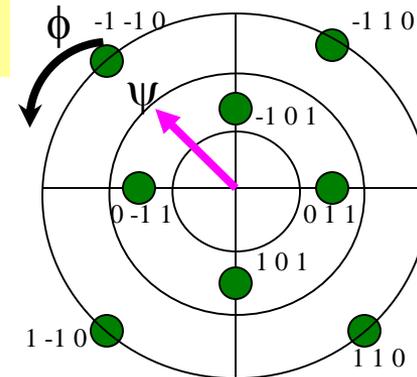
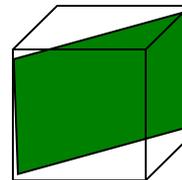


Azimuth  
 $\phi = 45^\circ, 135^\circ, 225^\circ, 315^\circ$

Tilt  $\psi = 54.7^\circ$

$\psi: [100], [111]$

(110) Pole figure



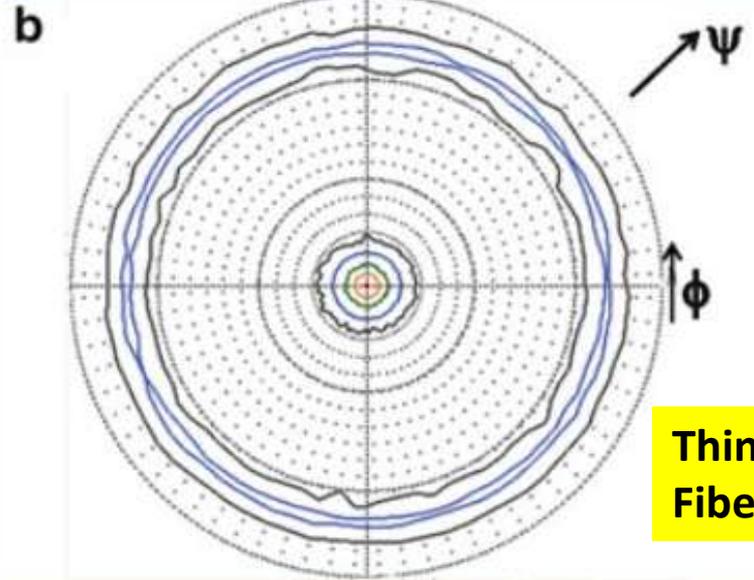
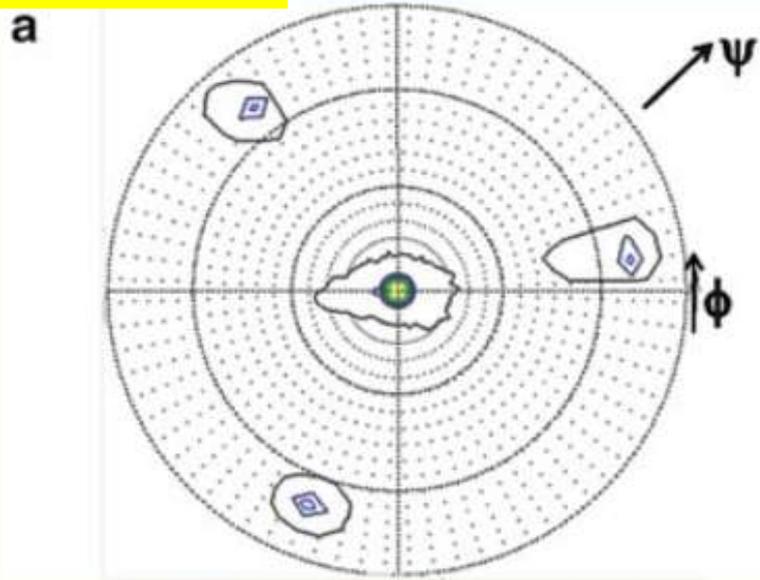
Azimuth  
 $\phi = 0, 90^\circ, 180^\circ, 270^\circ, 45^\circ, 135^\circ, 225^\circ, 315^\circ$

Tilt  $\psi = 45^\circ, 90^\circ$

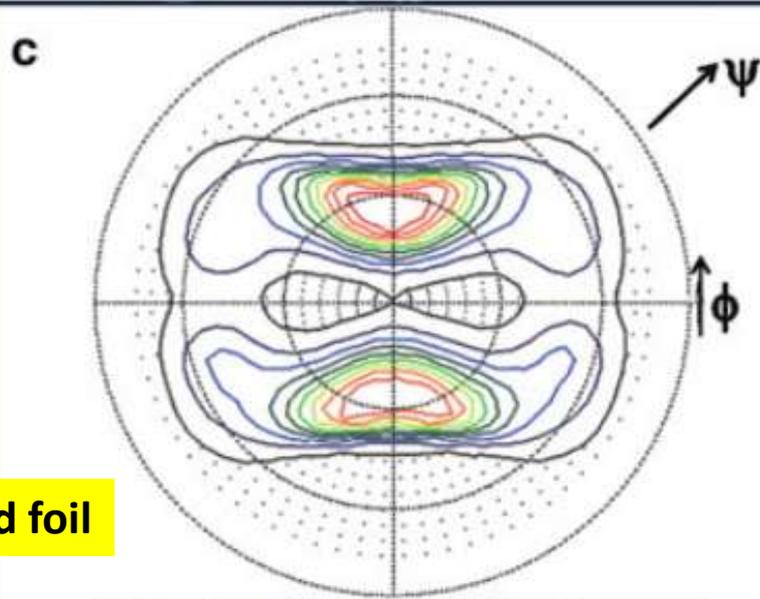
$\psi: [100], [110]$

# Cu (111) pole figure

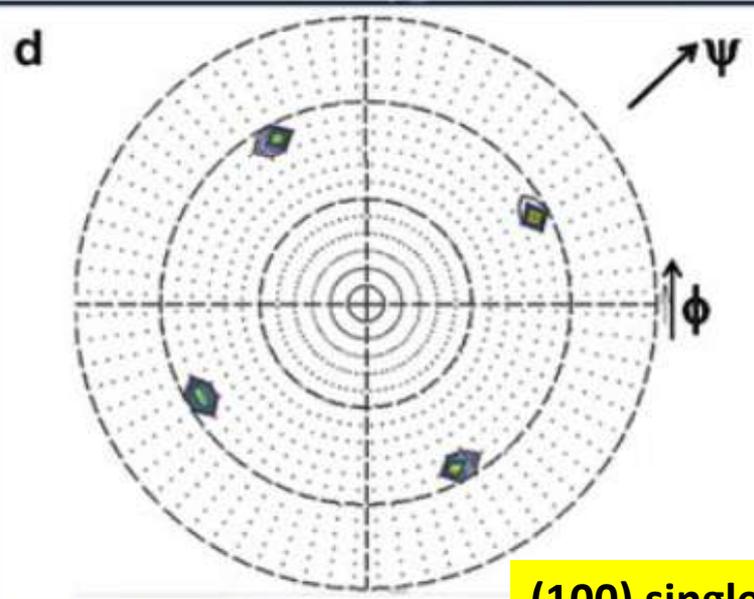
(111) single crystal



Thin film  
Fiber texture



Rolled foil

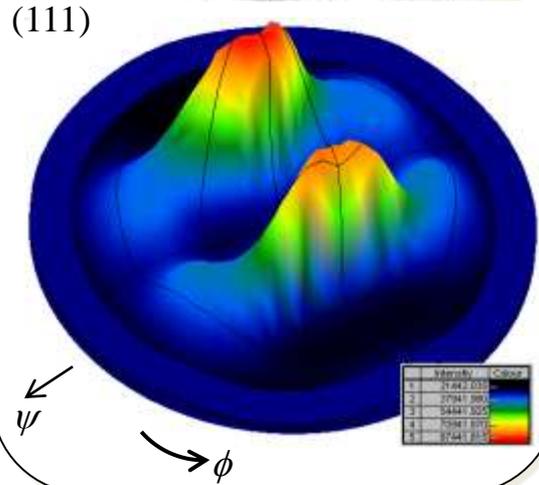
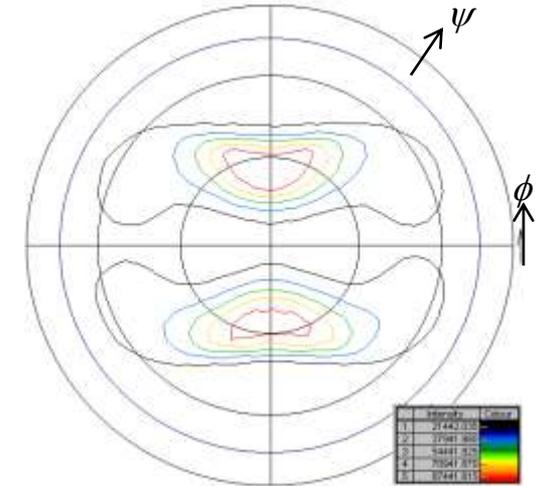


(100) single crystal

# X-ray pole figure analysis of textured materials

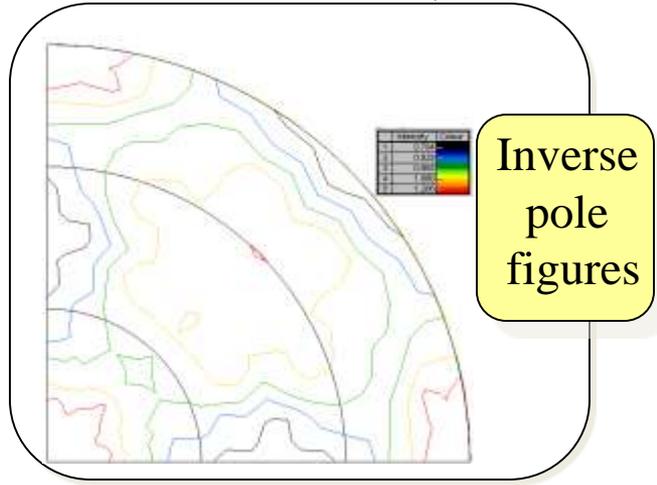
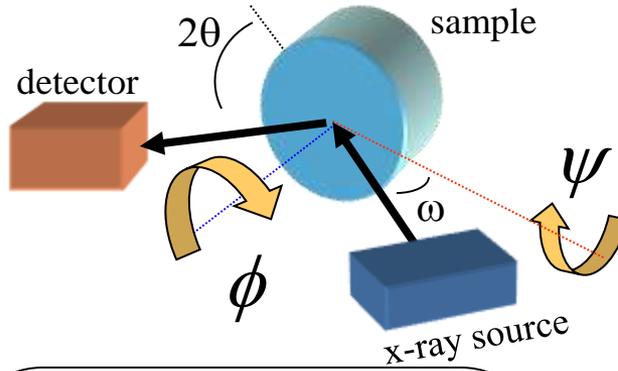
Texture results from a rolled Cu foil

Pole figures

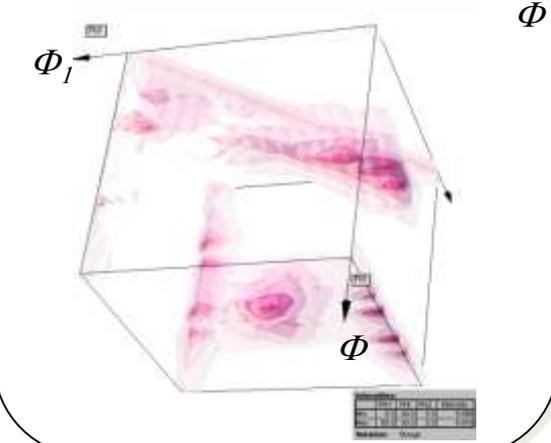
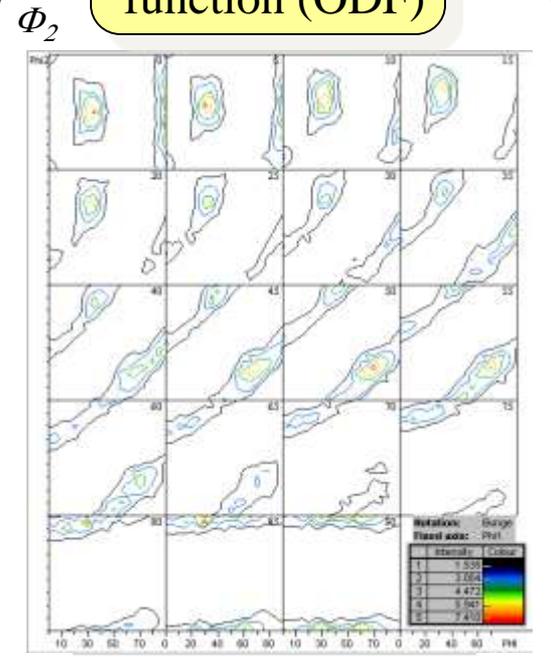


Data: Sardela, UIUC

- Texture orientation and quantification.
- Volume fraction of textured grains, twinning and random distributions.
- Texture strength and sharpness.
- Crystallographic orientation.
- Crystallographic relationship between layers and substrate.



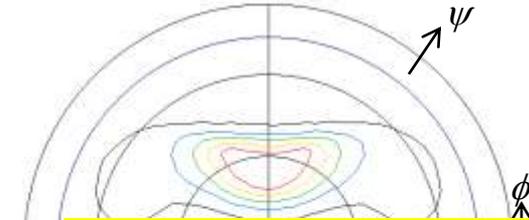
Orientation distribution function (ODF)



# X-ray pole figure analysis of textured materials

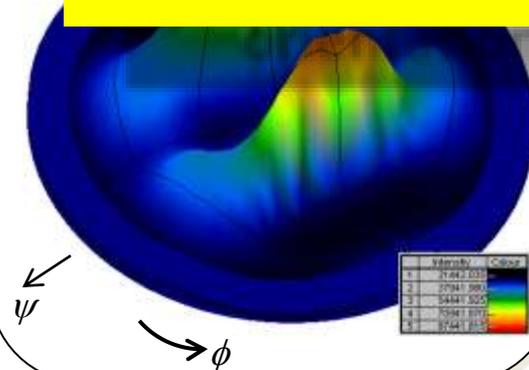
Texture results from a rolled Cu foil

Pole figures



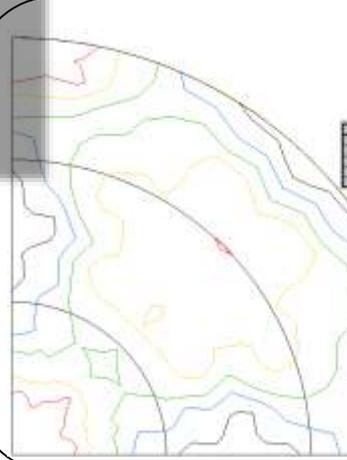
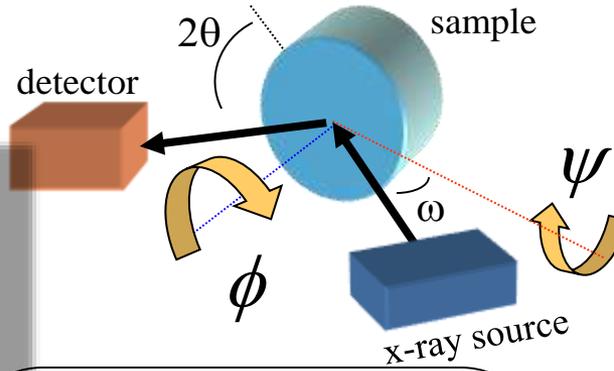
**Pole figure:**  
Distribution of grains with a particular (hkl) orientation

(11)



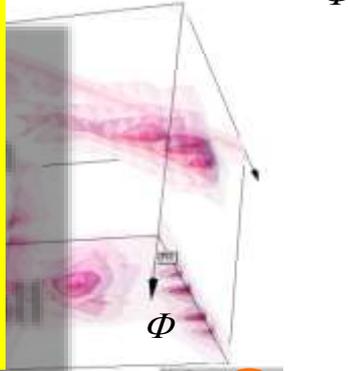
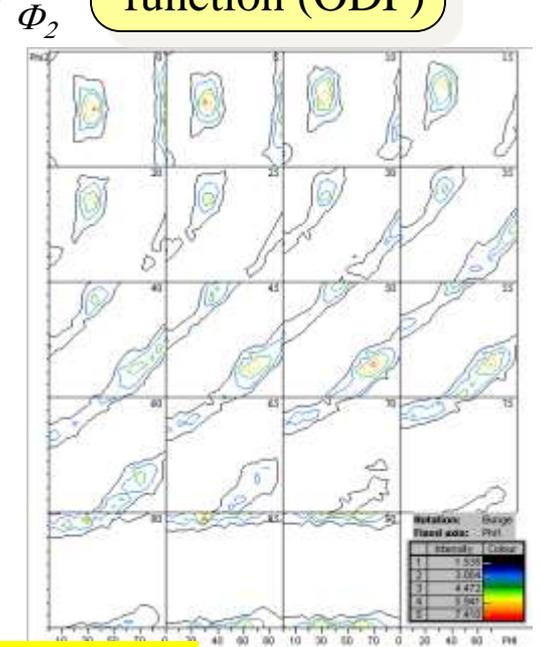
Data: Sardela, UIUC

- Texture orientation and quantification.
- Volume fraction of textured grains, twinning and random distributions.
- Texture strength and sharpness.
- Crystallographic orientation.
- Crystallographic relationship between layers and substrate.



**ODF:**  
fraction of grain orientation distribution for all directions

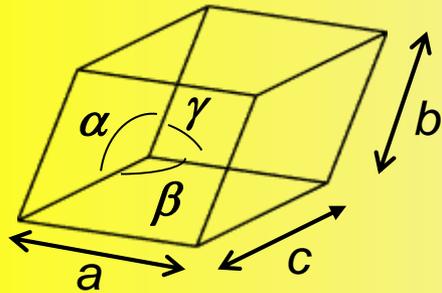
Orientation distribution function (ODF)



directions



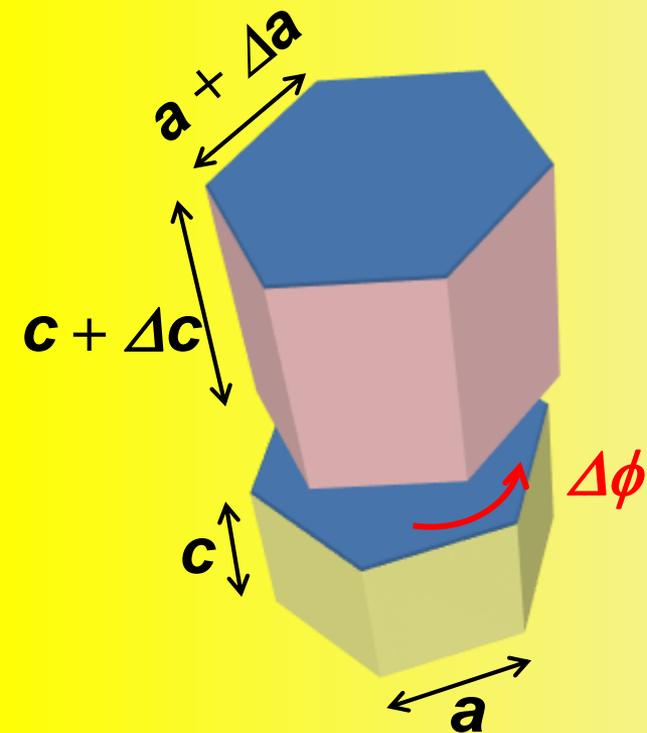
# High resolution XRD methods



## Single crystals:

Accurate measurements of  $a$ ,  $b$ ,  $c$ ,  $\alpha$ ,  $\beta$ ,  $\gamma$

Detailed peak shapes: defects, mosaicity.

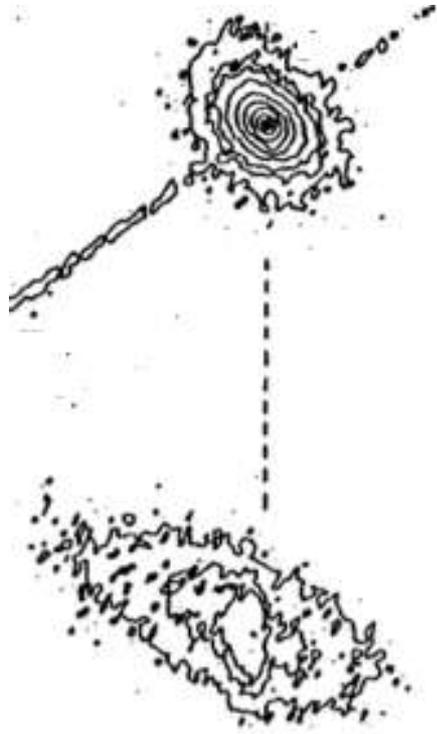
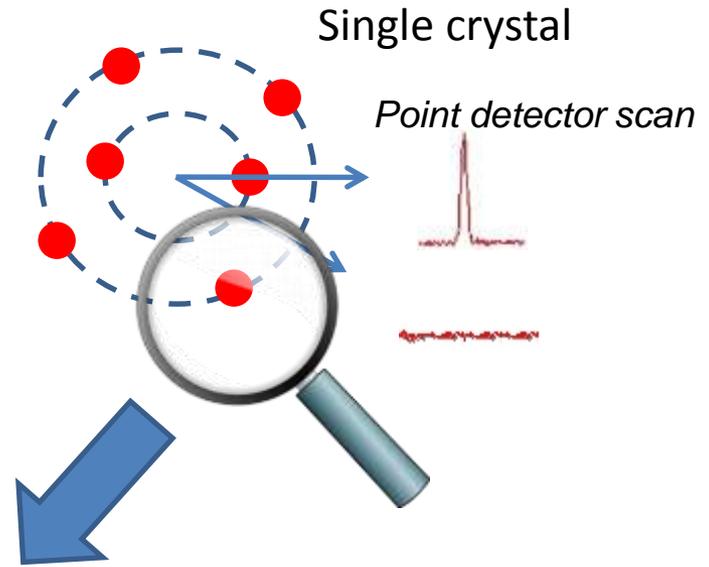
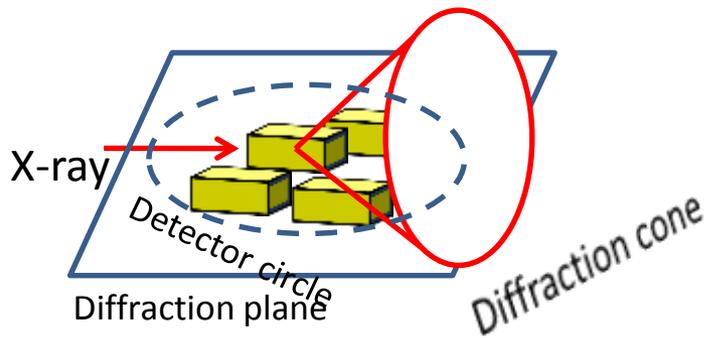


## Film / substrate epitaxial systems:

Measure small variations  $\Delta a$ ,  $\Delta c$ , ... ( $\sim 10^{-5}$ ).

Measure layer tilts  $\Delta\phi$ , ...

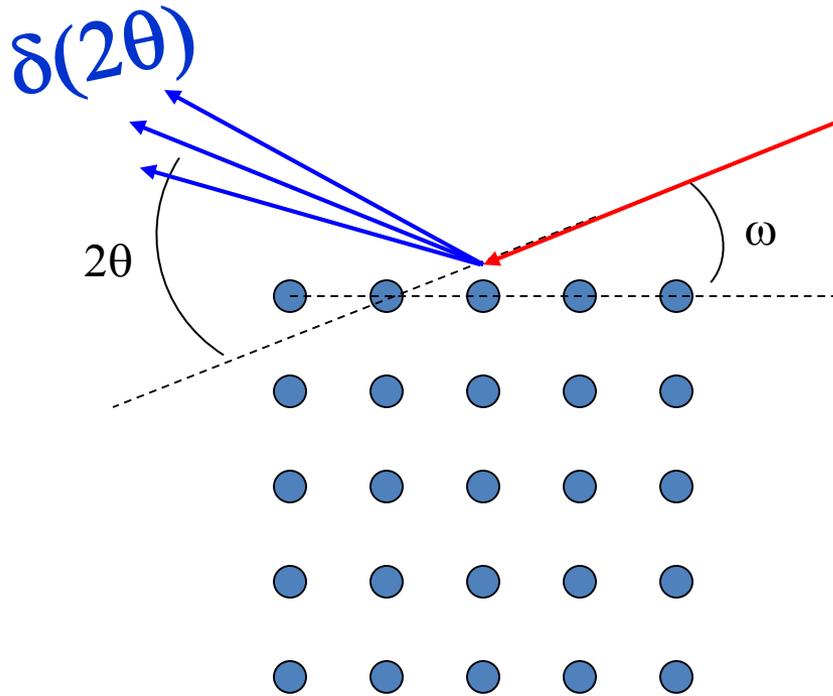
Detailed peak shapes: defects, strain, mosaicity.



Multiple rlp's  
Relative position  
Orientation  
Shape

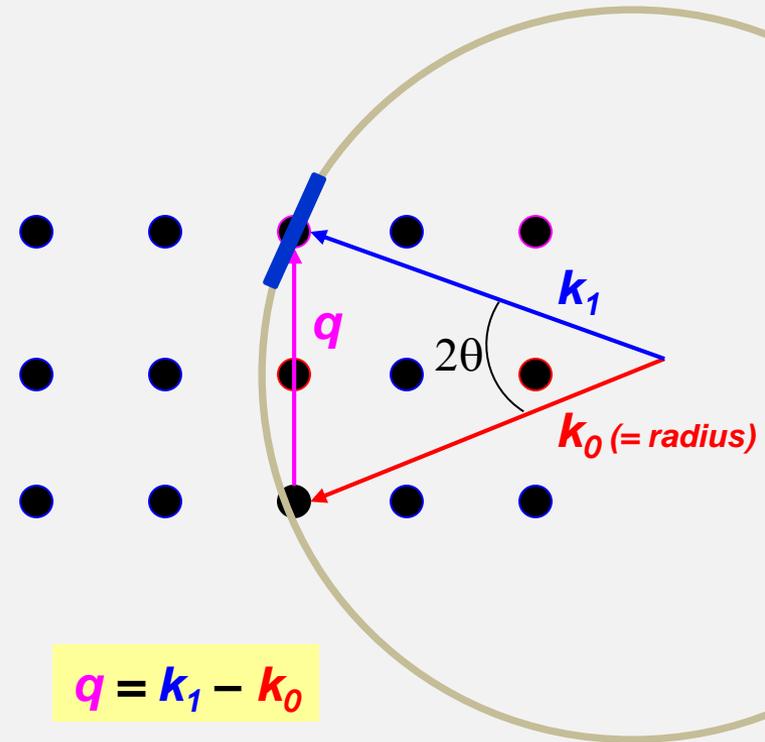
# Instrument resolution in reciprocal space

“Real” space



Reciprocal space

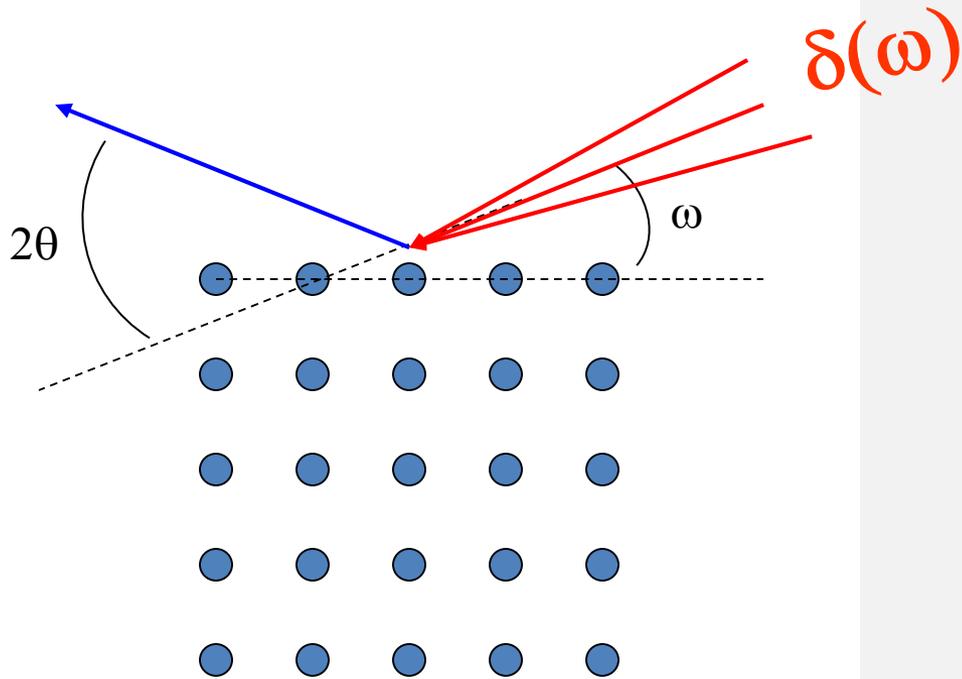
Ewald's sphere



$$q = k_1 - k_0$$

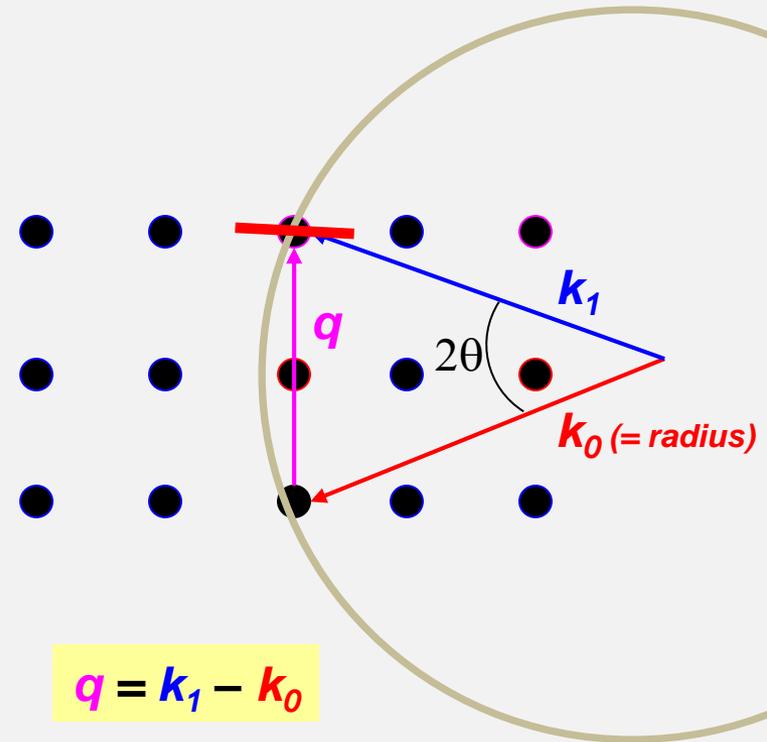
# Instrument resolution in reciprocal space

“Real” space



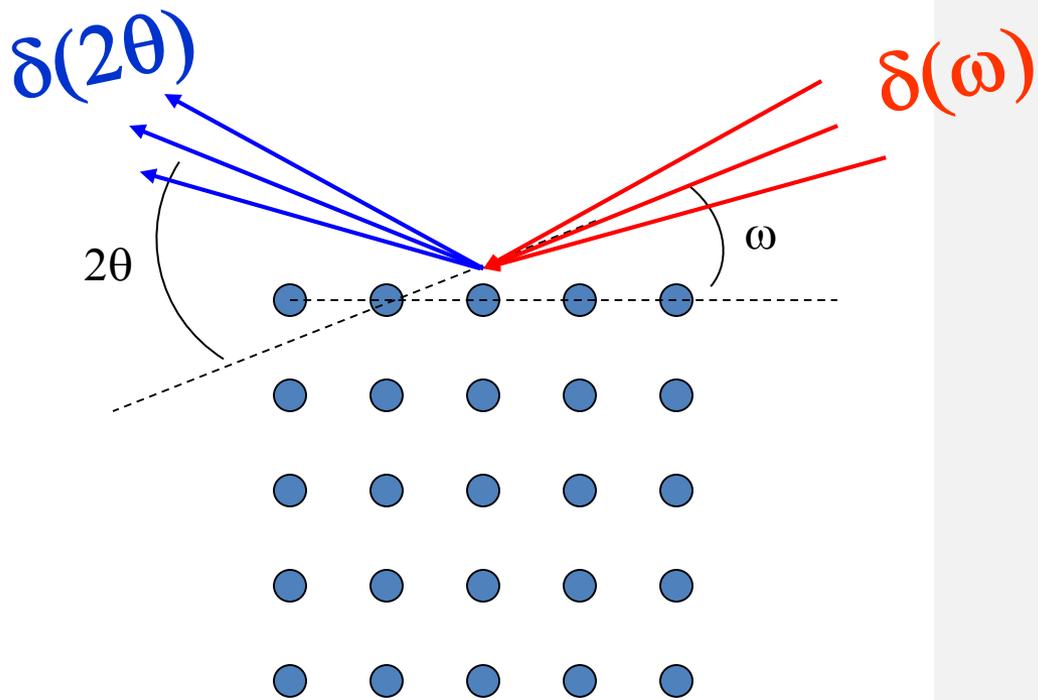
Reciprocal space

Ewald's sphere



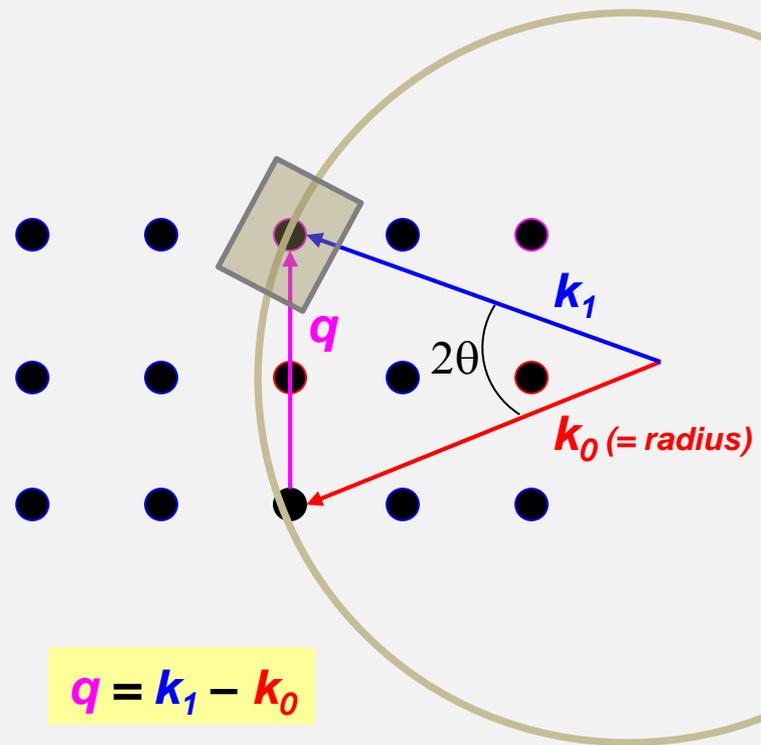
# Instrument resolution in reciprocal space

"Real" space

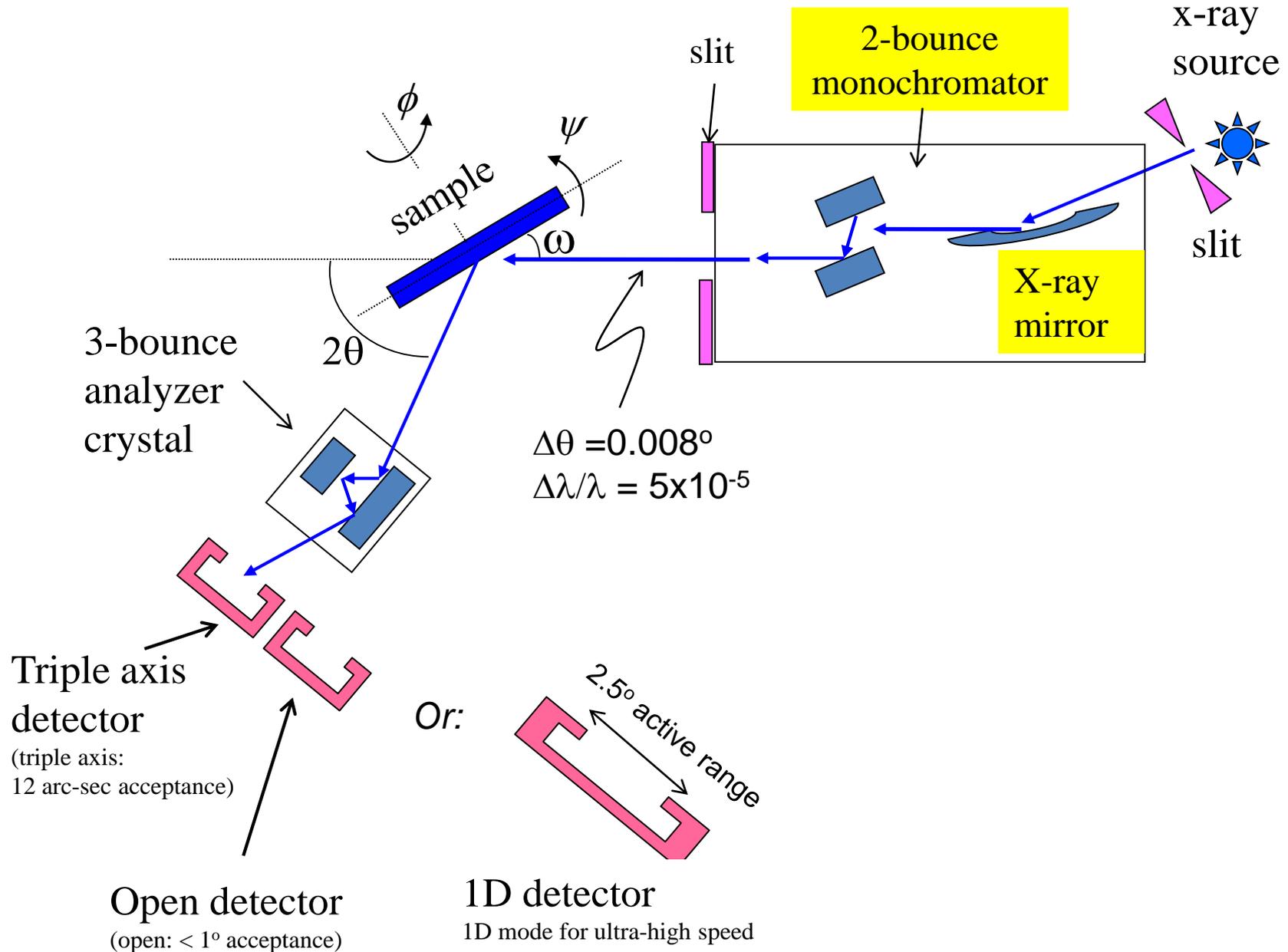


Reciprocal space

Ewald's sphere



# Instrumentation: high resolution configuration

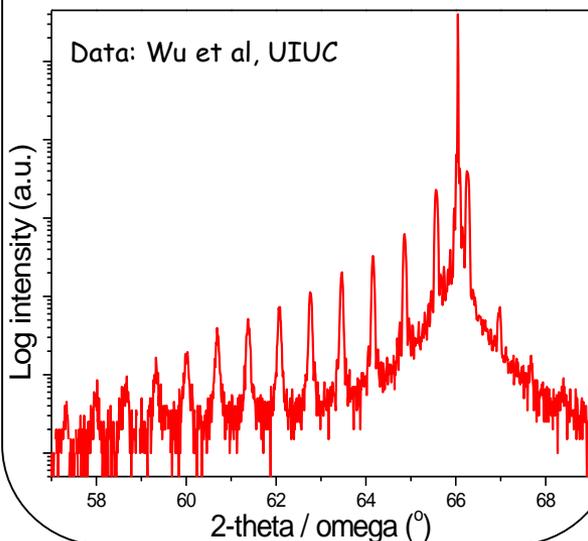


# High resolution x-ray analysis

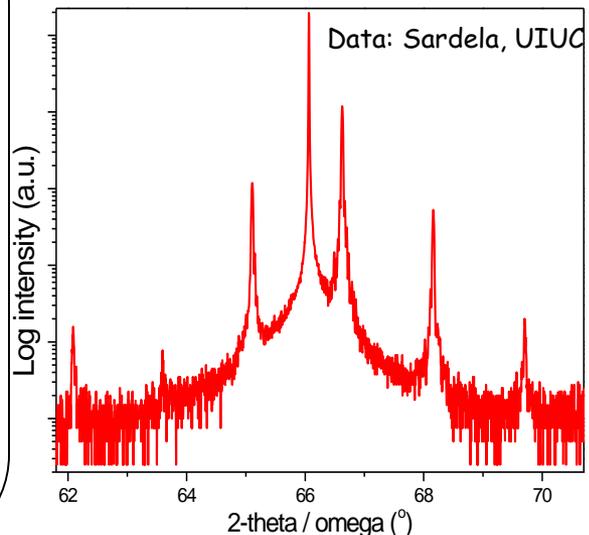
- Lattice distortions within  $10^{-5}$ .
- Rocking curve analysis.
- Film thickness.
- Strain relaxation and lattice parameter measurements.
- Alloy composition and superlattice periods.
- Interface smearing in heterostructures (dynamical simulation).

Single crystals  
Epitaxial films  
Heterostructures  
Superlattices  
Quantum dots

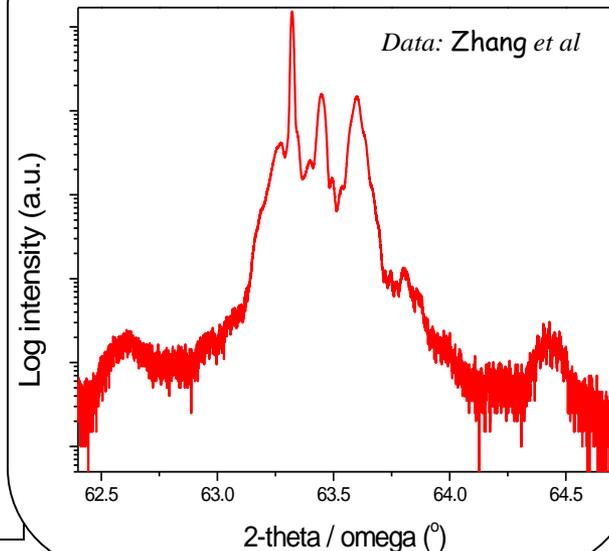
InAs / GaAs multilayer



SiGe / Ge superlattice



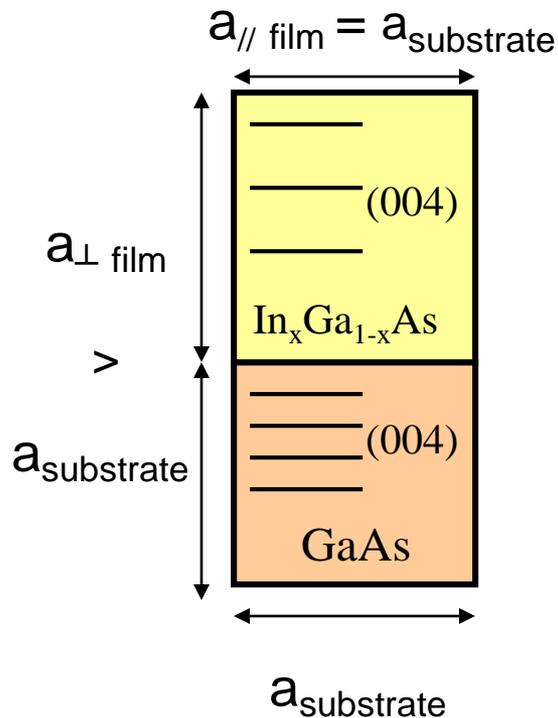
InAs quantum dots on GaAs



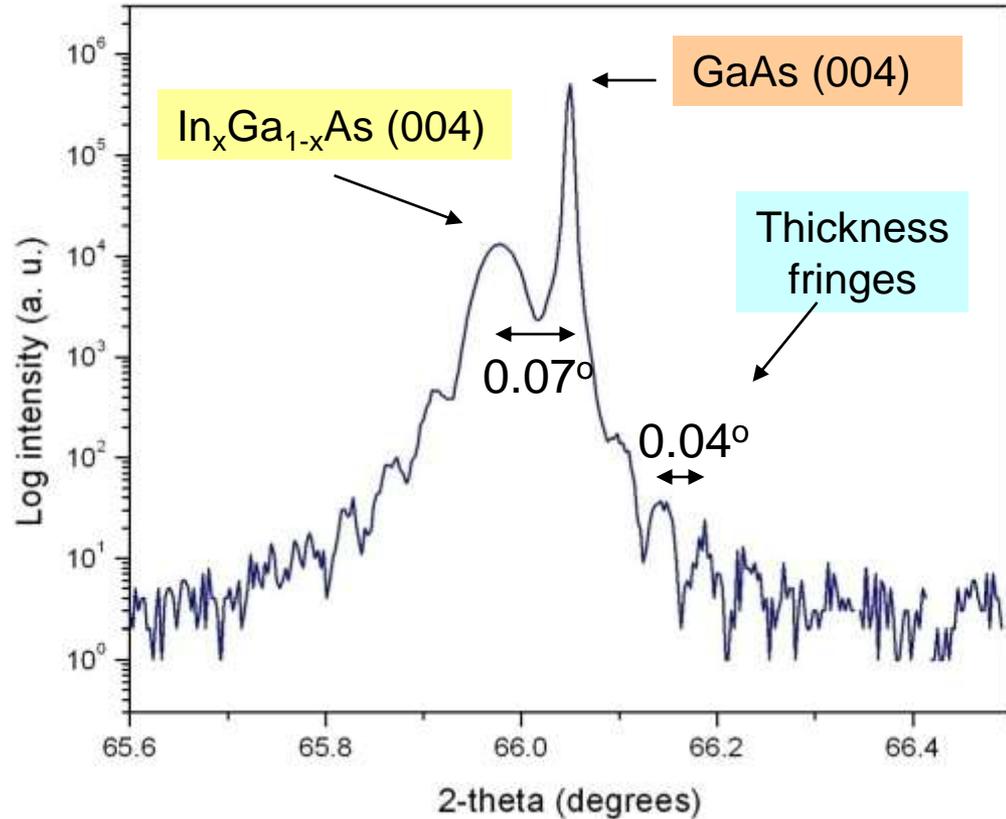
# High resolution x-ray analysis

Example: strained  $\text{In}_x\text{Ga}_{1-x}\text{As}$  on GaAs (001) substrate

## Lattice structure



## High resolution $2\theta/\theta$ scan near GaAs(004)



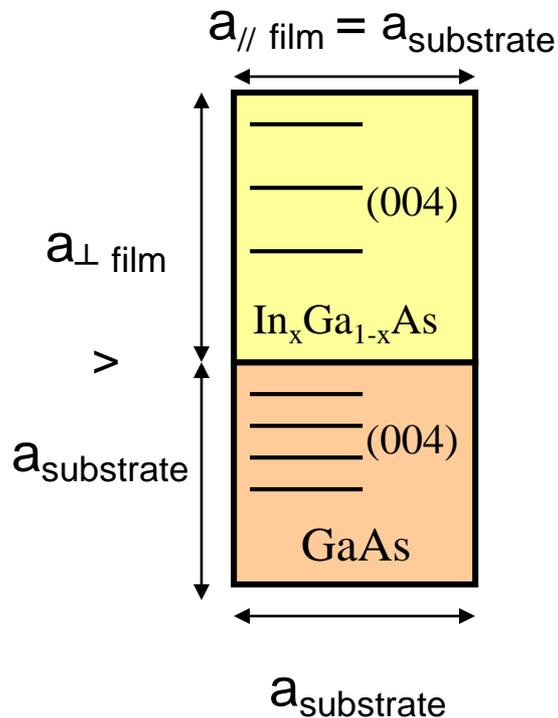
$$\frac{\Delta a}{a} = \frac{\sin \theta(\text{substrate})}{\sin \theta(\text{film})} - 1$$

$$\text{Thickness} = \frac{\lambda}{2 \Delta \theta \cos \theta}$$

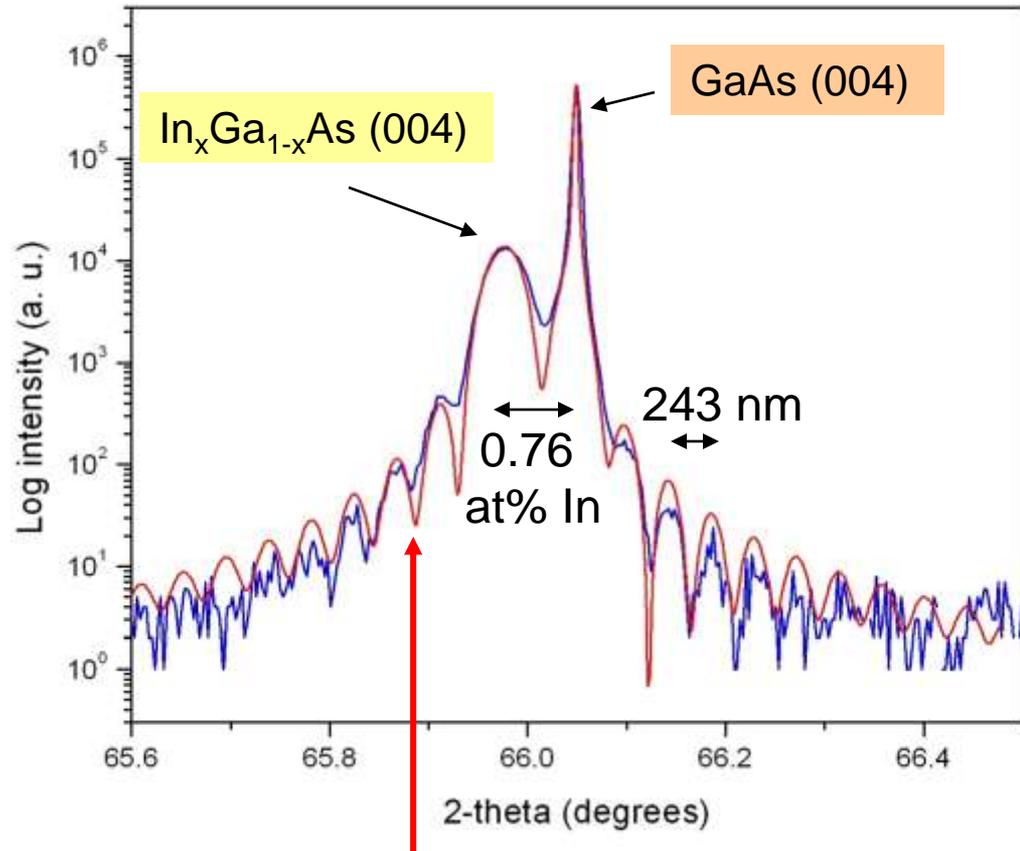
# High resolution x-ray analysis

Example: strained  $\text{In}_x\text{Ga}_{1-x}\text{As}$  on GaAs (001) substrate

## Lattice structure



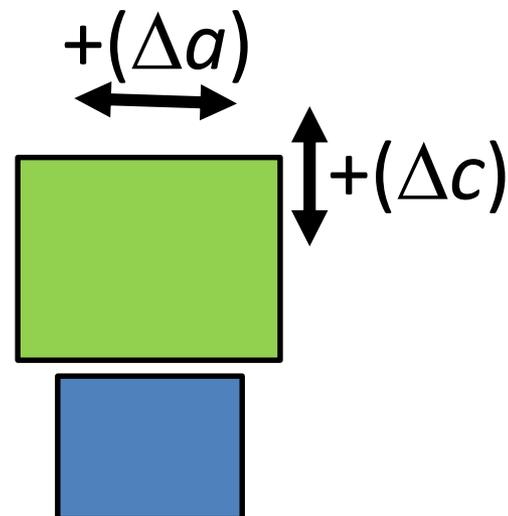
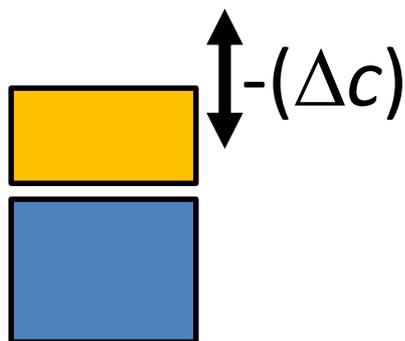
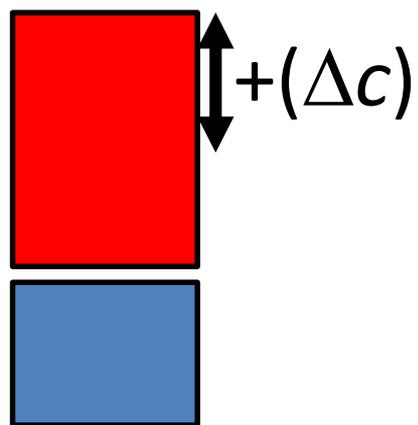
## High resolution $2\theta/\theta$ scan near GaAs(004) and dynamical scattering simulation



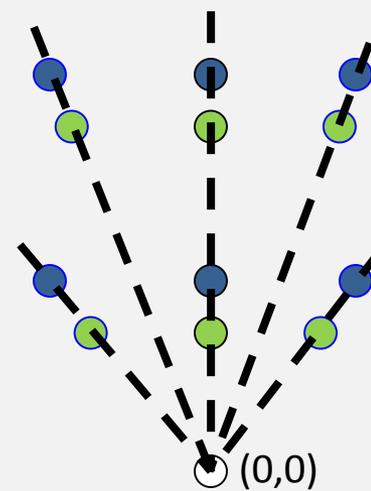
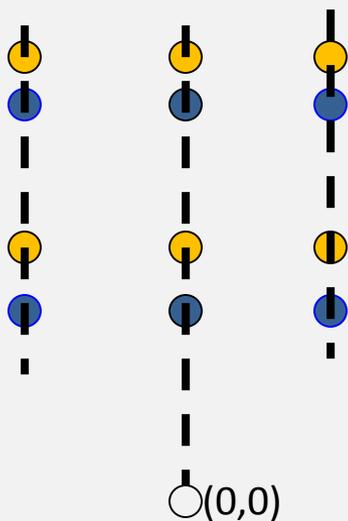
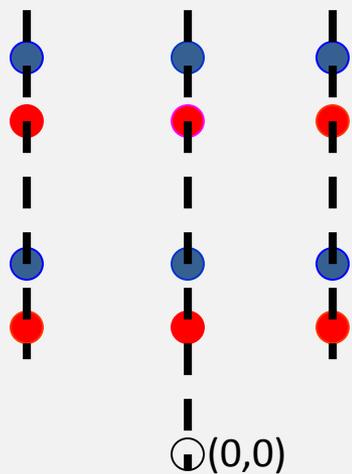
Takagi-Taupin dynamical scattering simulation

# Reciprocal space mapping

*Direct space:*

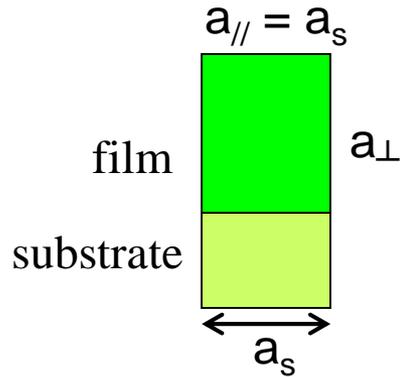


*Reciprocal space:*

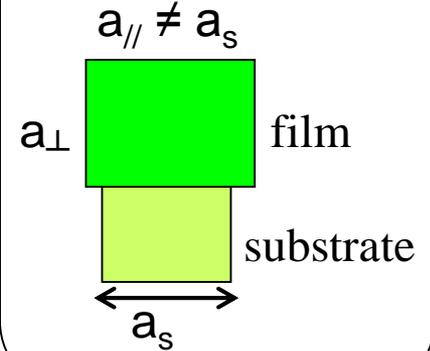


# Reciprocal space mapping

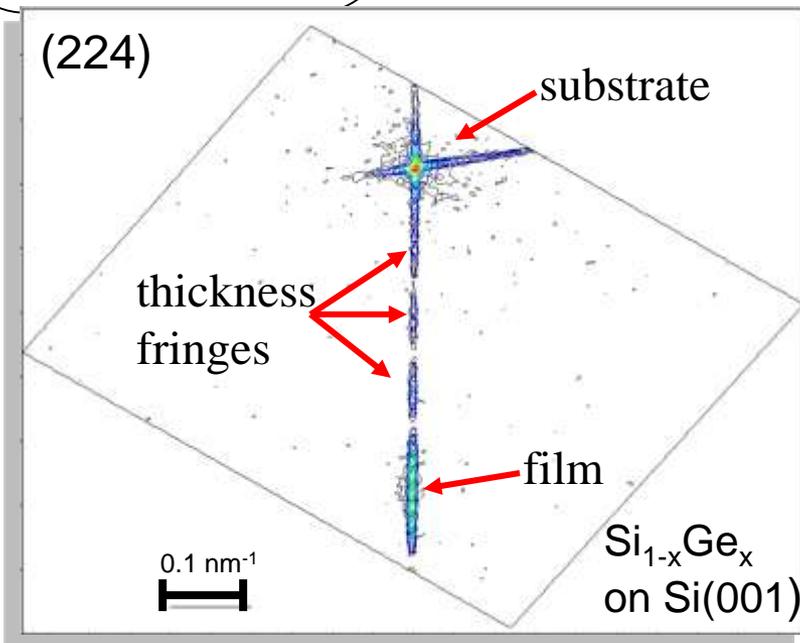
No strain relaxation:



Strain relaxation:

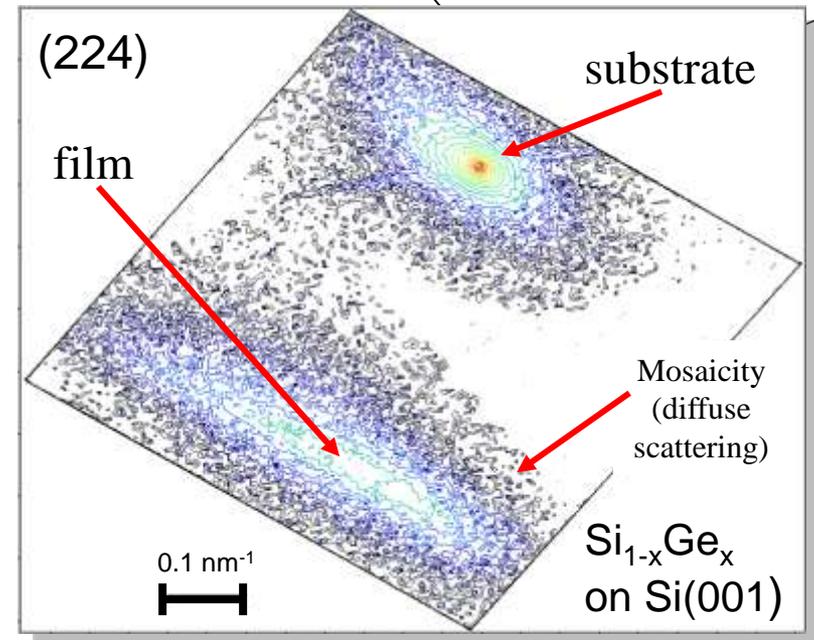


- Separation of strain and mosaicity
- Lattice distortions within  $10^{-5}$ .
- Accurate lattice parameters in and out of plane
- Strain and composition gradients
- Strain relaxation
- Mosaic size and rotation
- Misfit dislocation density
- Nanostructure dimensions,
- Lattice disorder and diffuse scattering.



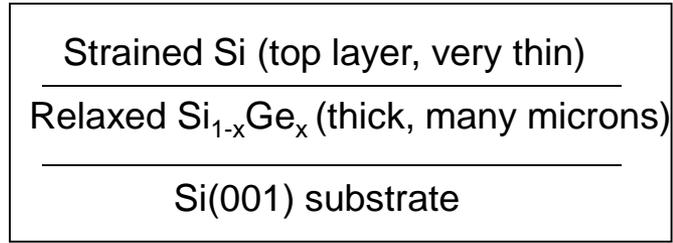
$\Delta q_{001}$

$\Delta q_{110}$

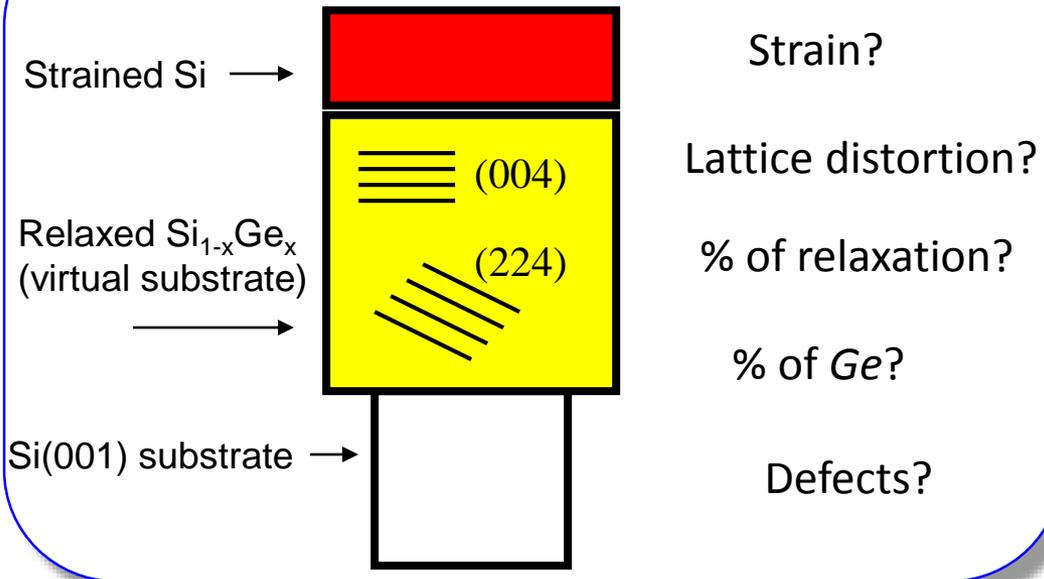


# High resolution reciprocal space mapping

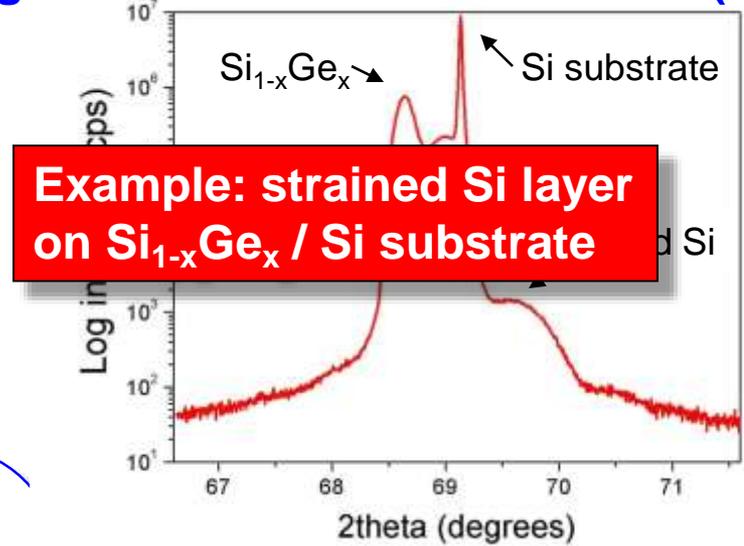
## Layer structure



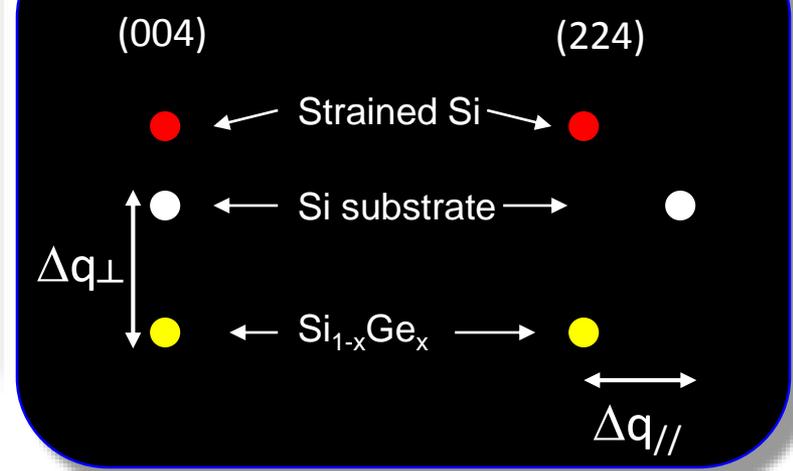
## Lattice structure



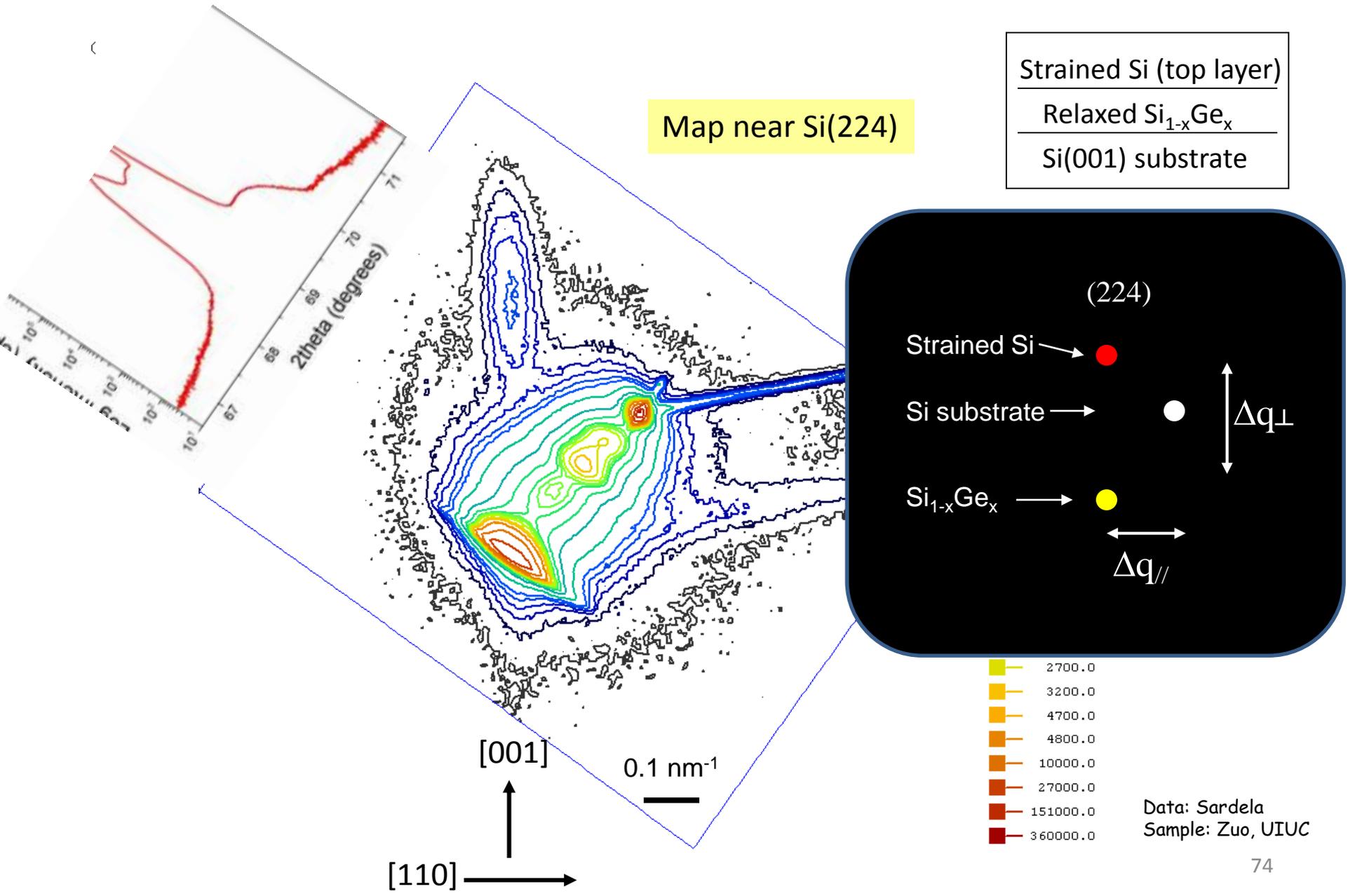
## High resolution $2\theta/\omega$ scan near Si(004)



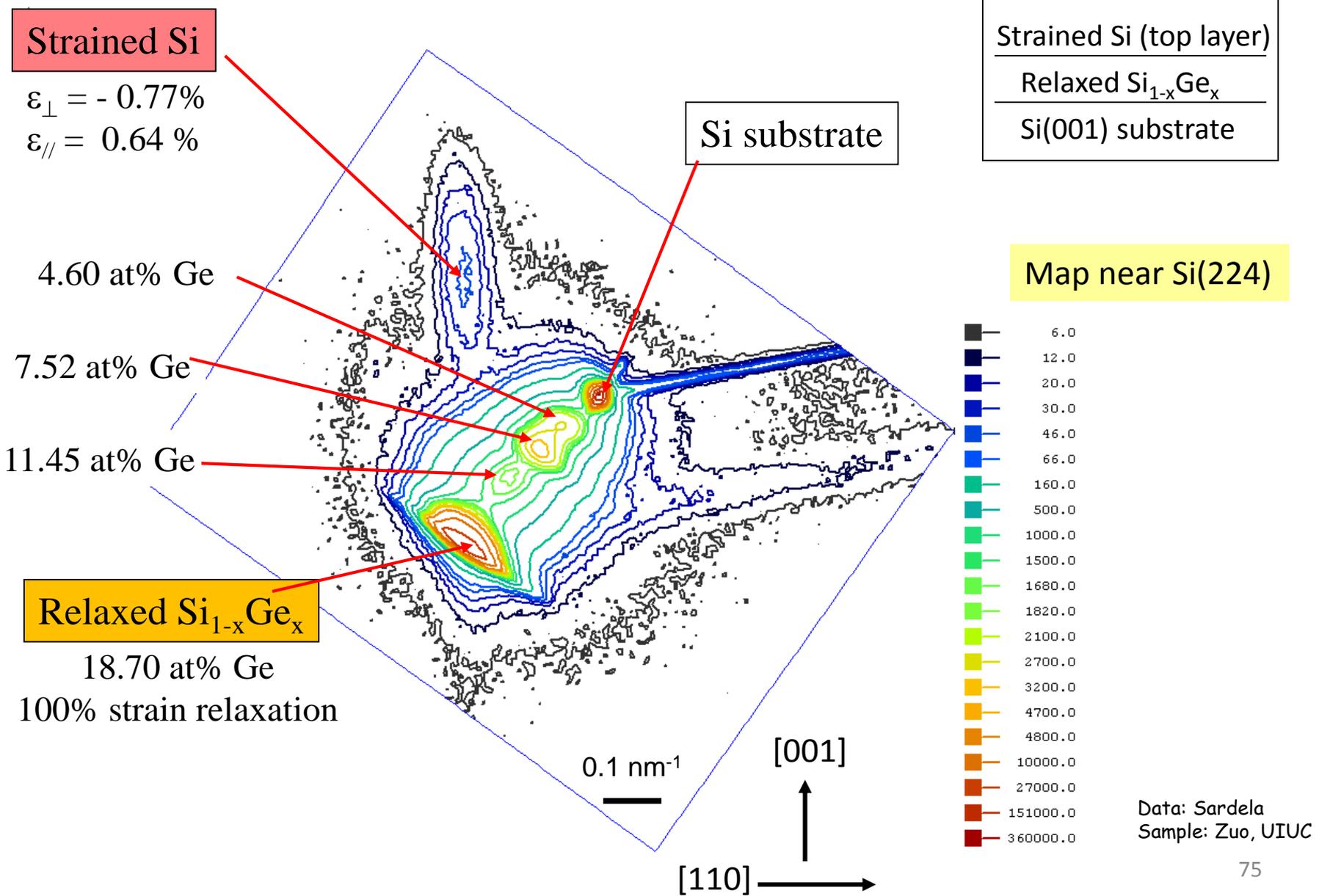
## Reciprocal lattice



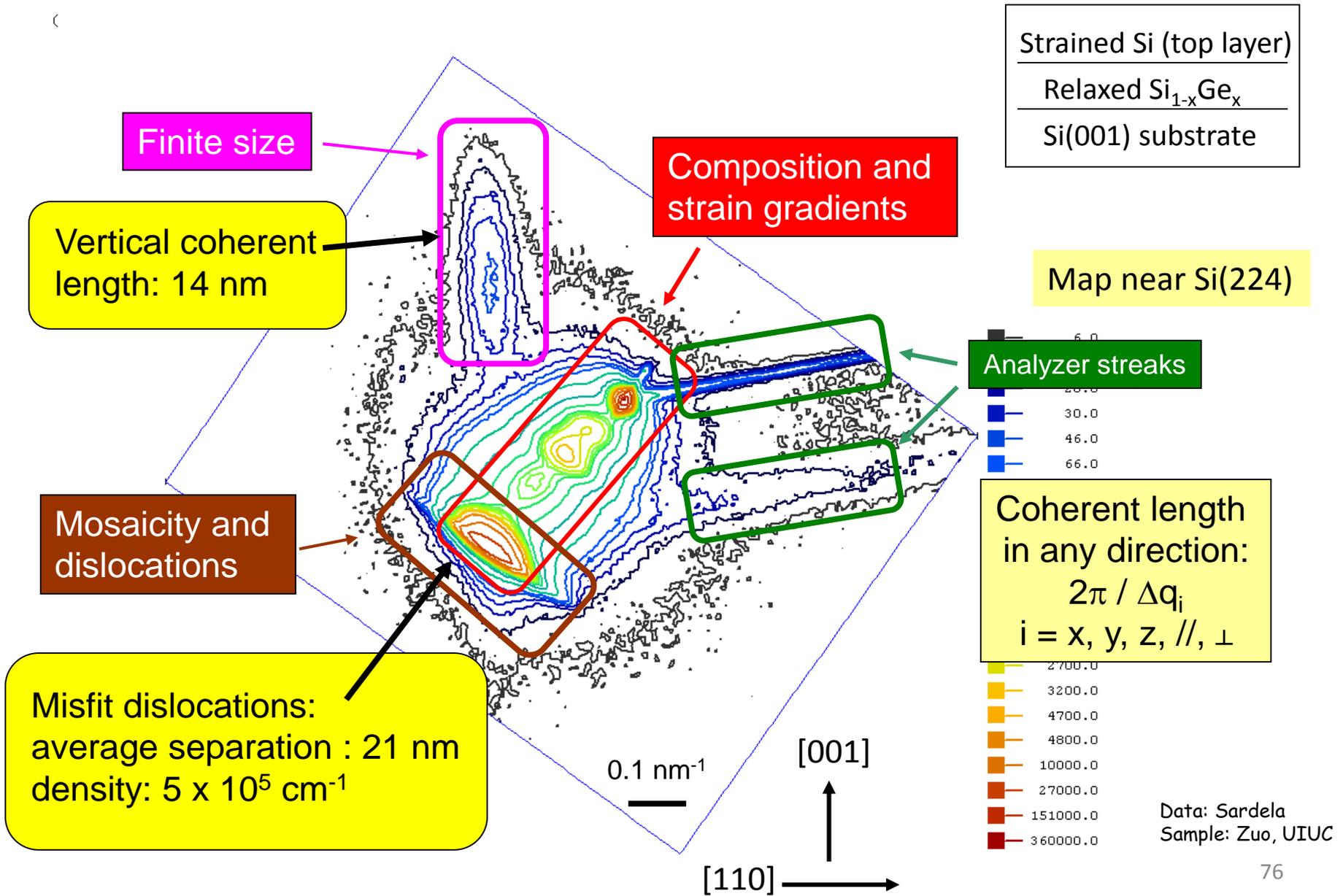
# High resolution reciprocal space mapping



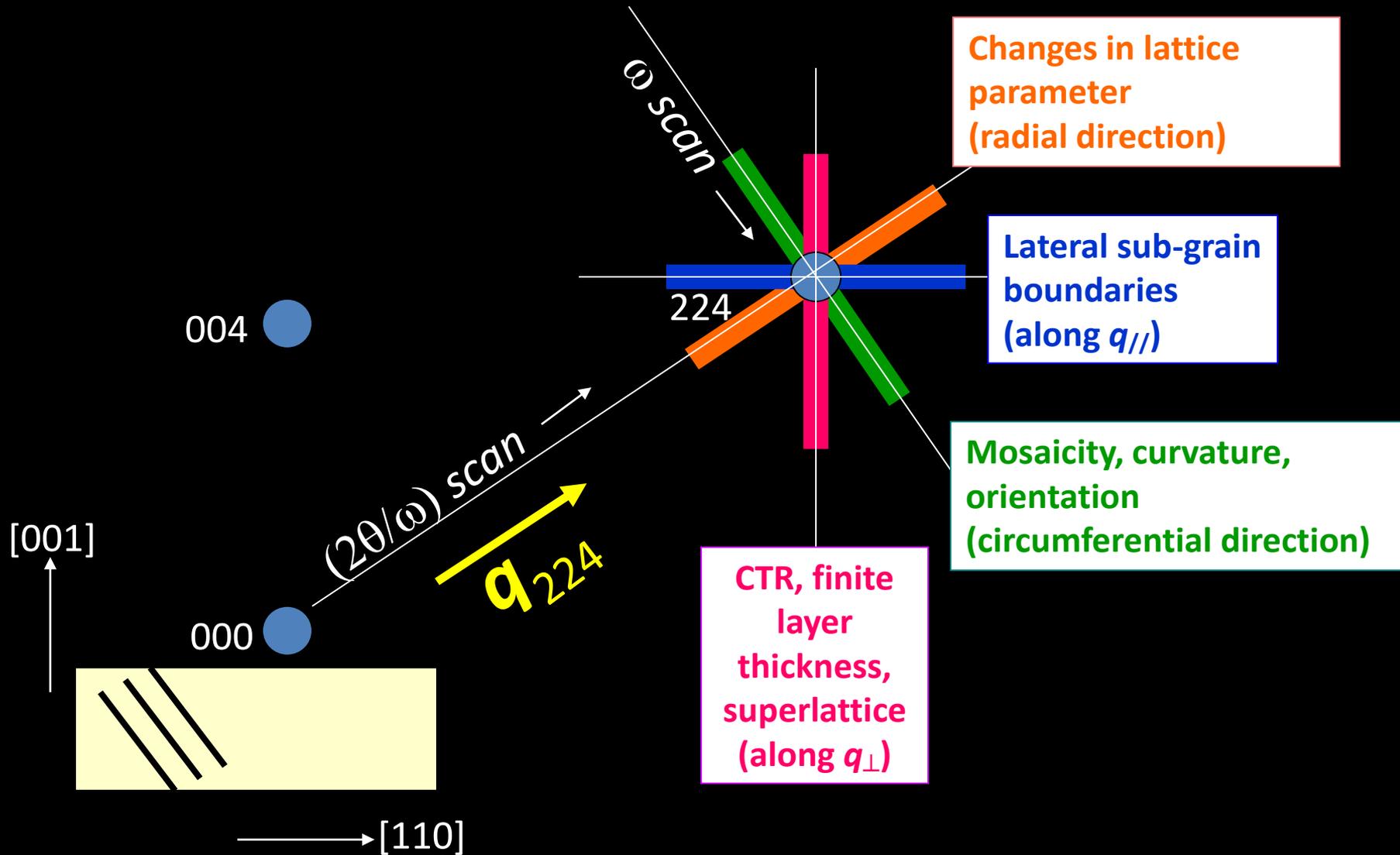
# High resolution reciprocal space mapping



# High resolution reciprocal space mapping

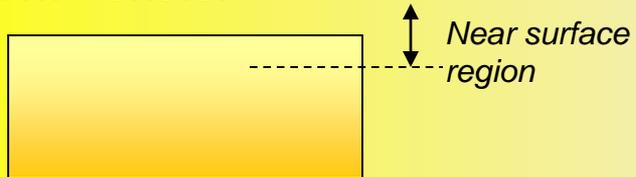


# The "shape" of the reciprocal lattice point



# X-ray reflectivity

*Bulk materials:*



*Liquids:*



**Near surface and interface information on:**

**Density**

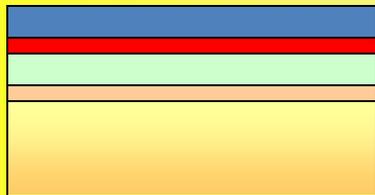
**Porosity**

**Roughness**

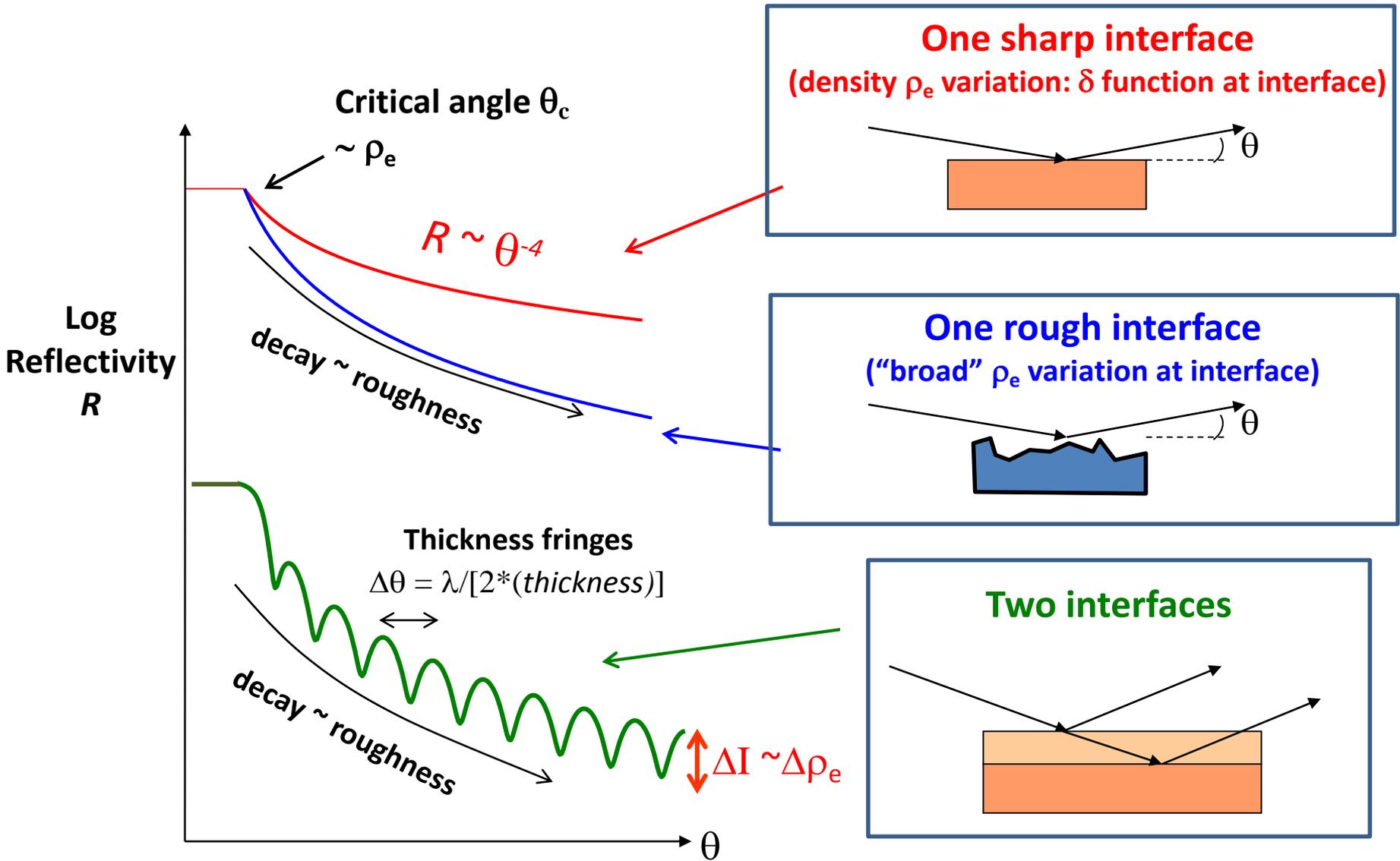
**Thickness in films (ultra thin to thick)**

**Amorphous or crystalline materials**

*Multilayered systems:*

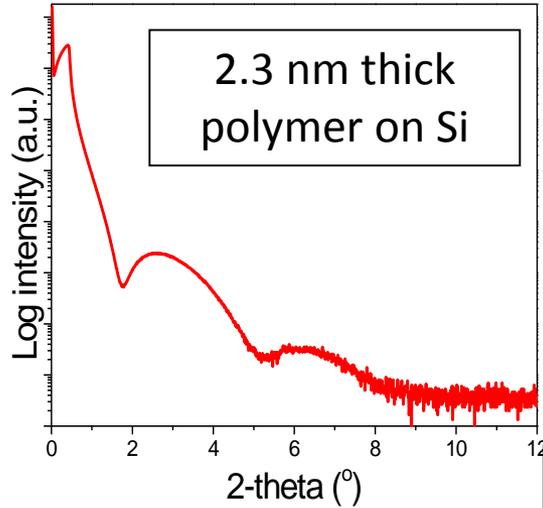


# X-ray reflectivity



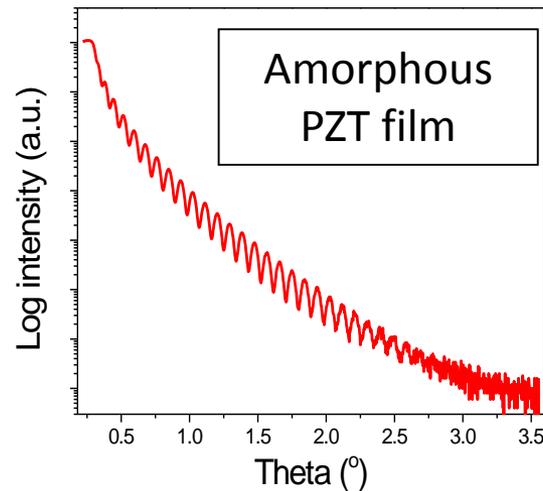
# X-ray reflectivity analysis of thin films

## Ultra-thin film



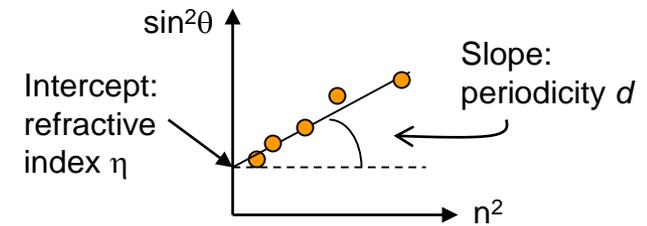
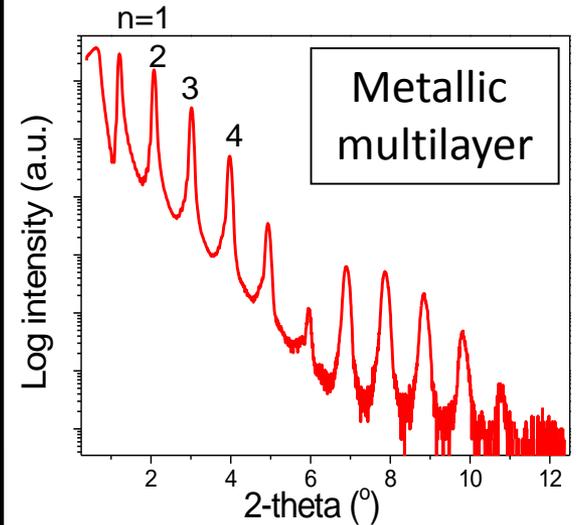
Data: Heitzman et al, UIUC

## Non crystalline



Data: Mikalsen et al, UIUC

## Multilayers

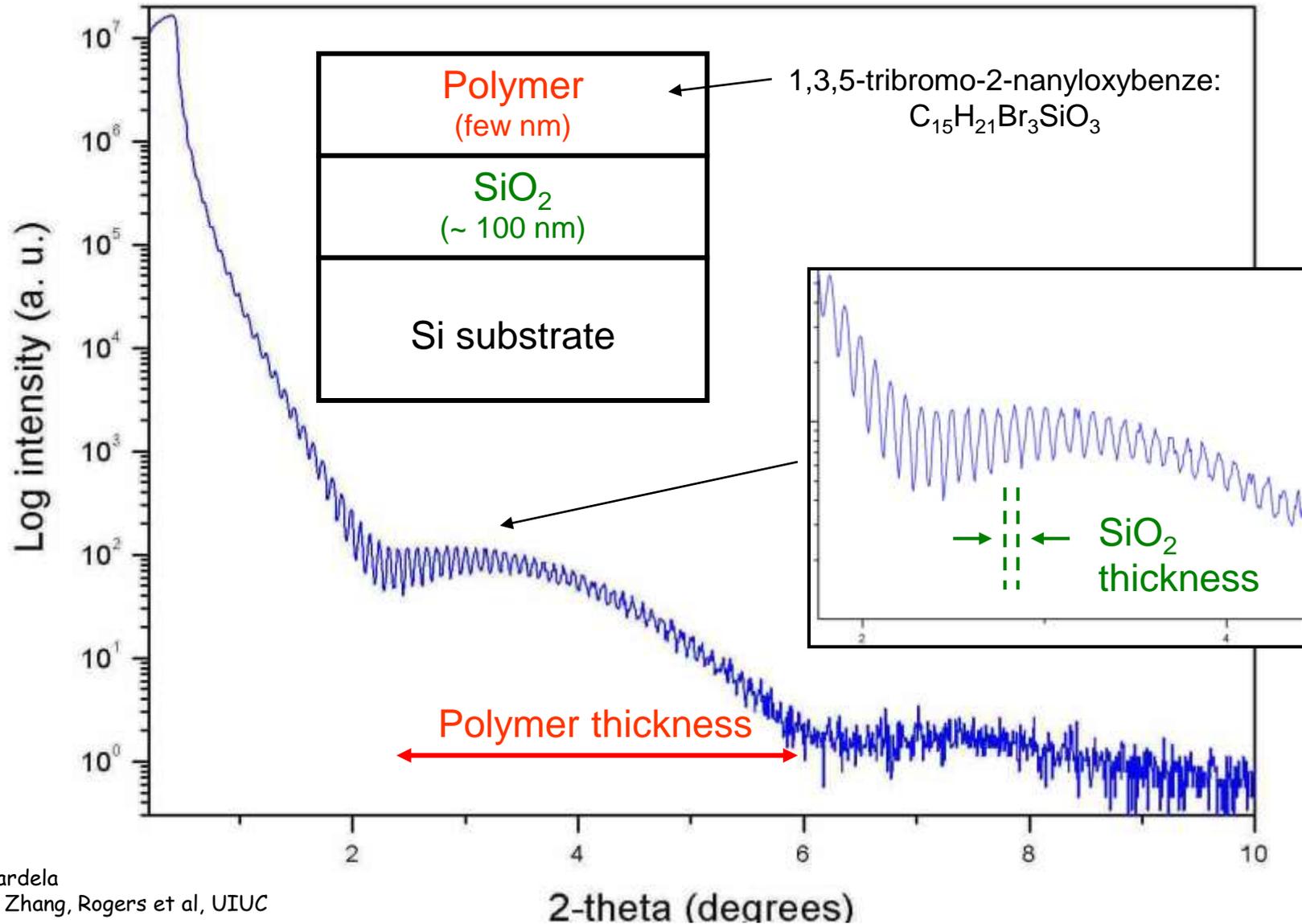


$$\sin^2\theta = (\lambda^2/2d)^2 n^2 - (\eta^2 - 1)$$

(modified Bragg's law to include refractive index)

Data: Sardela, UIUC  
Sample: Auoadi et al, SIU

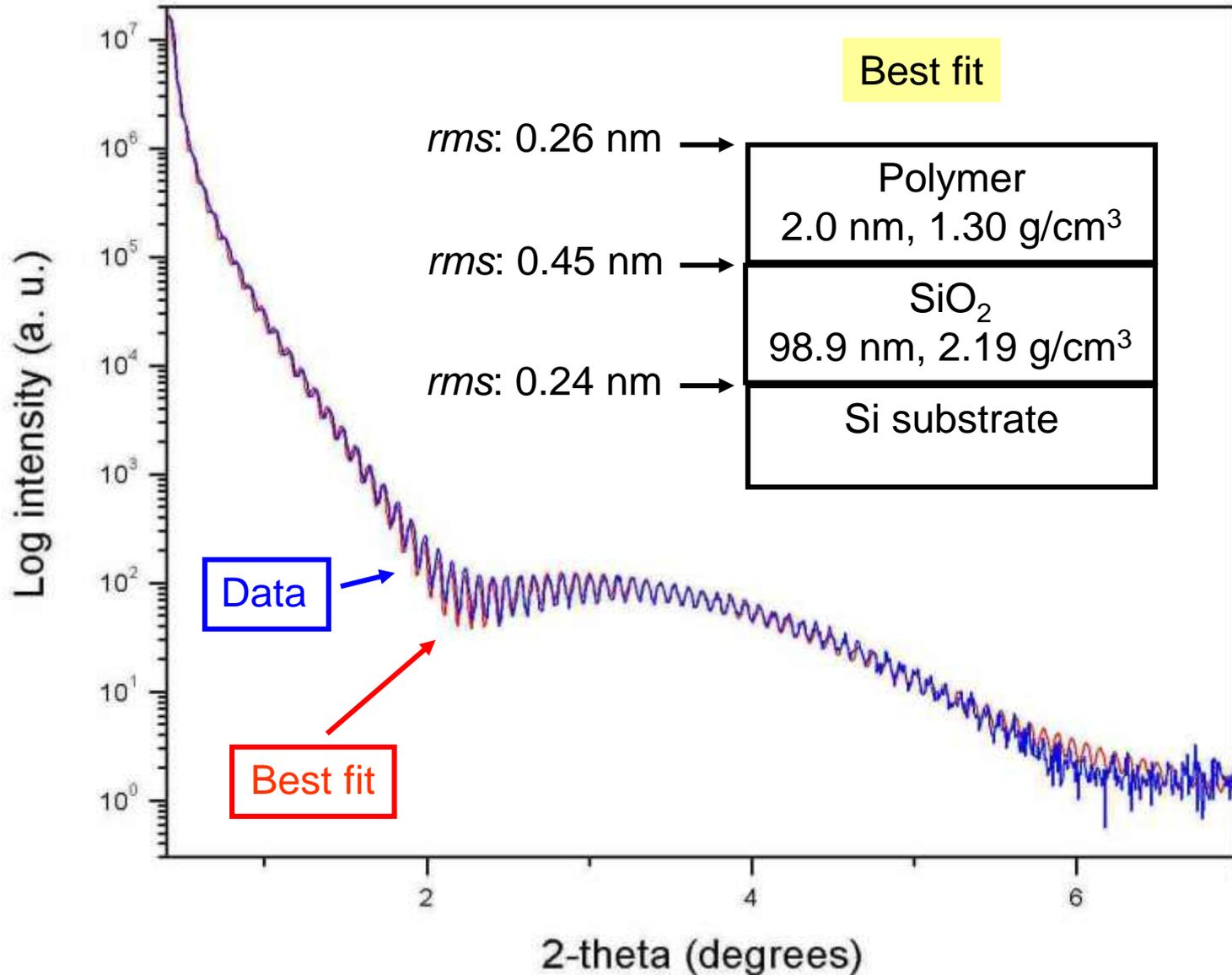
# X-ray reflectivity data fitting in ultra-thin films



Data: Sardela  
Sample: Zhang, Rogers et al, UIUC

# X-ray reflectivity data fitting

Simulation using Parrat's formalism and generic algorithm fitting



# X-ray reflectivity: summary

- \* Non destructive method
- \* Applicable to whole wafers (wafer mapping option)
- \* Fast method (in most cases)
- \* Do not depend on crystalline quality of the films (can also be used in amorphous layers).

## Quantification of:

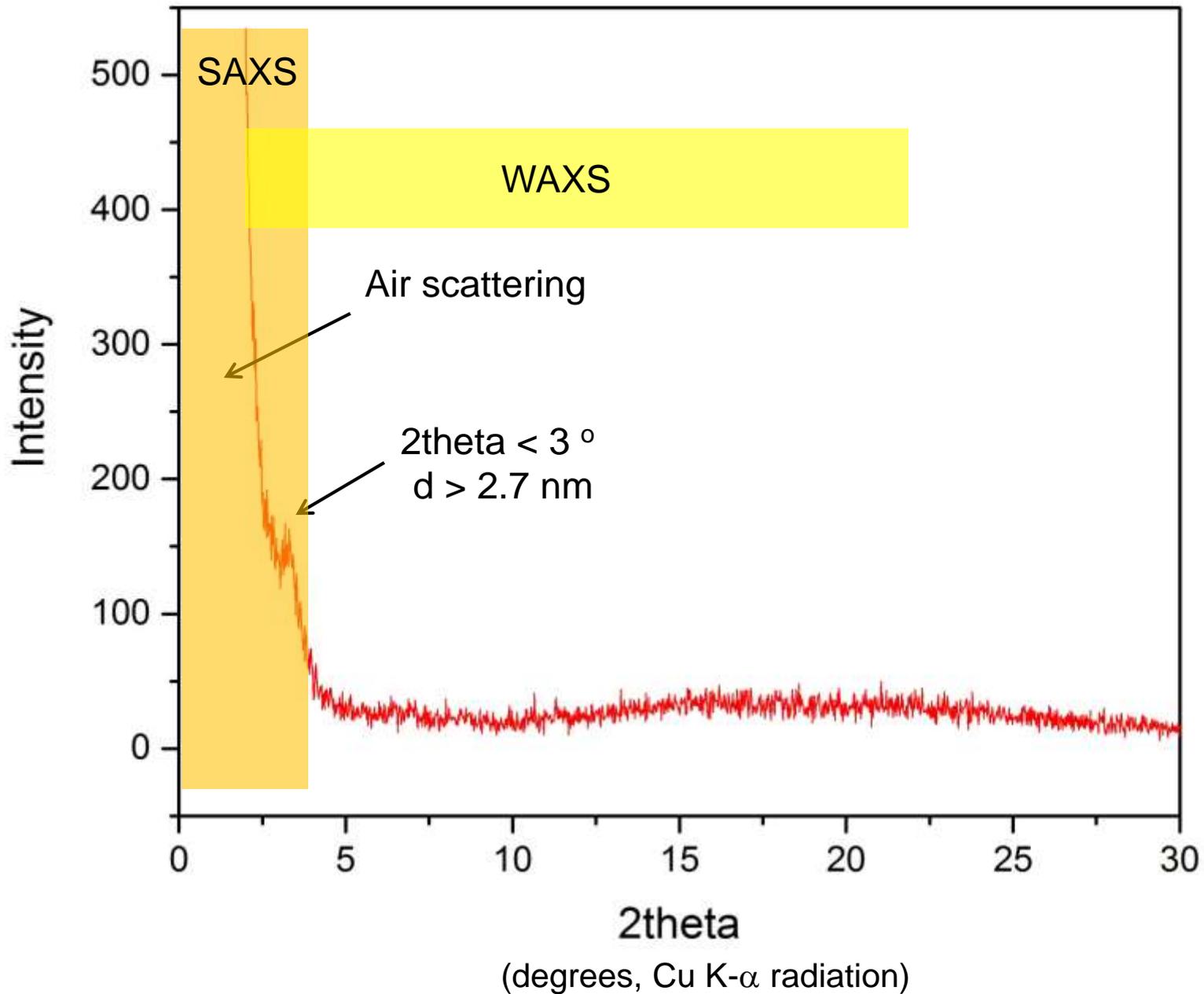
- \* Layer **thickness** in thin films and superlattices: 1 nm ~ 1  $\mu\text{m}$  ( $\pm$  0.5-1%).
- \* Layer **density** and **porosity** ( $\pm$  1-2%).
- \* Interface **roughness**: 0.1 – 10 nm (model dependent; reproducibility ~ 3%).
- \* Layer density **gradients** (variations > 2%).
- \* Interface roughness **correlation** in superlattices and multilayers.

## Alternative techniques:

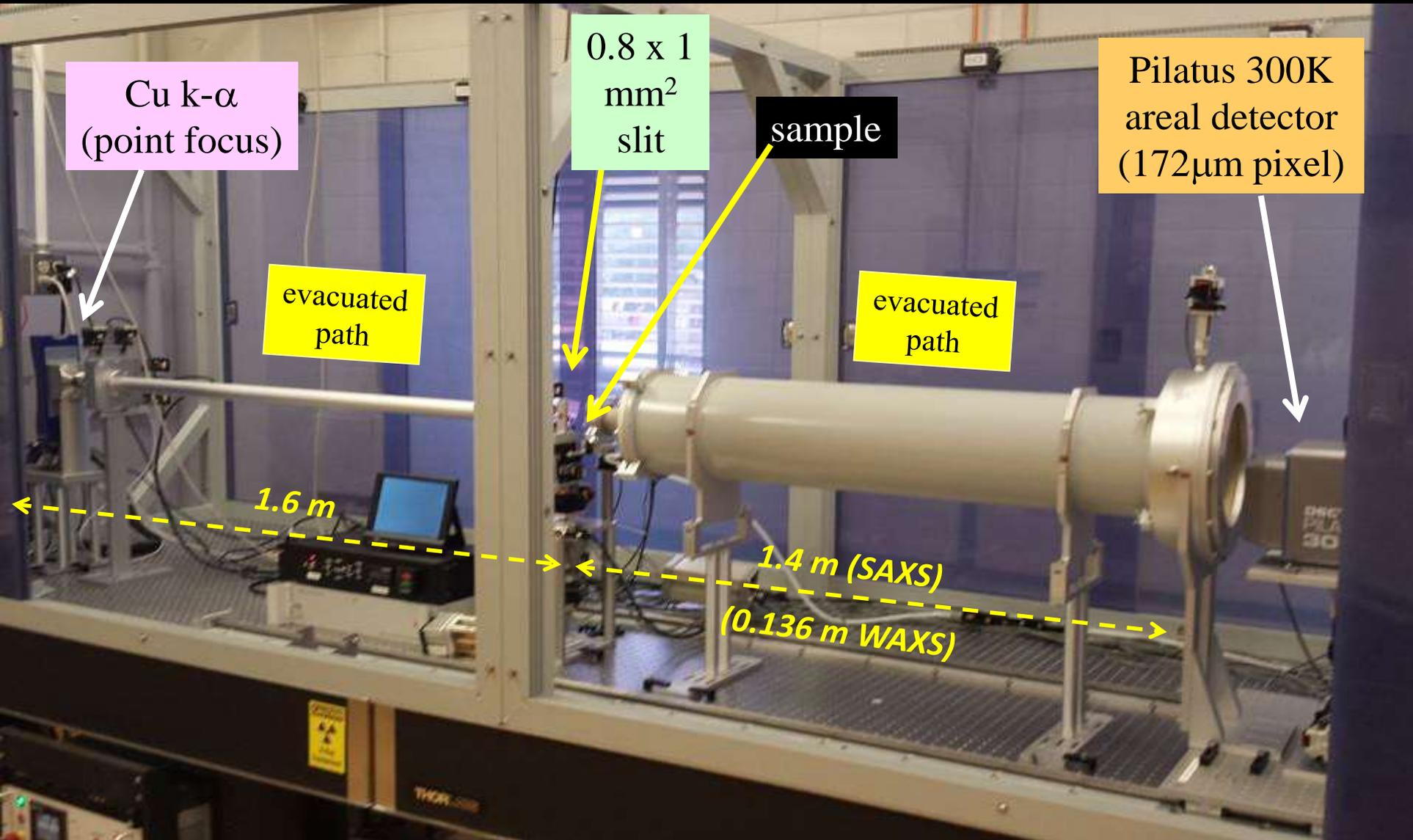
- \* Thickness: optical methods (TEM, SEM) poor contrast issues.
- \* Density: RBS (issues for ultra thin layers).
- \* Interface roughness: AFM (surface only – not buried interfaces).



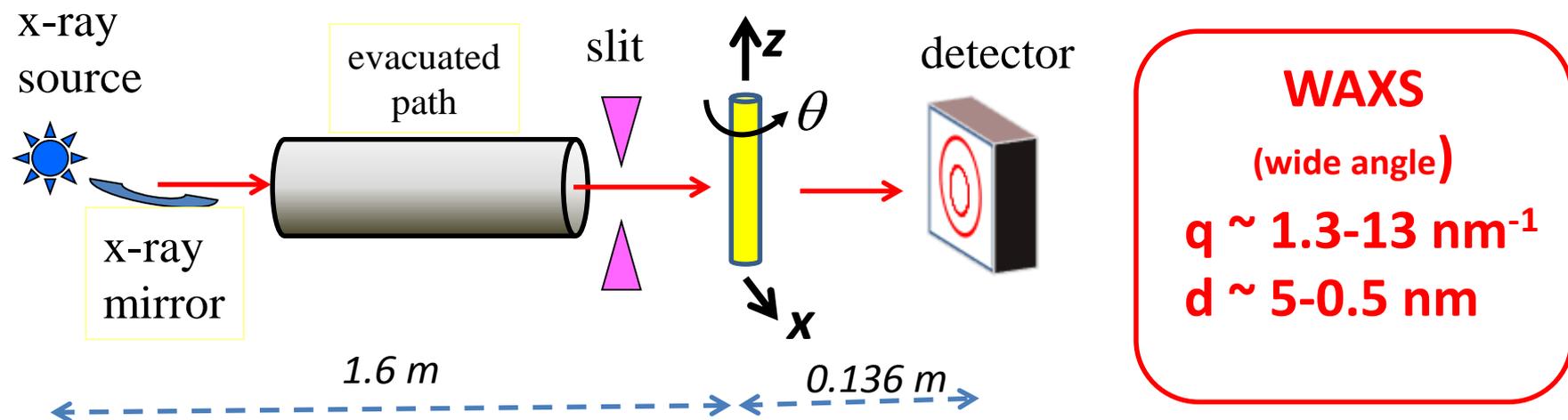
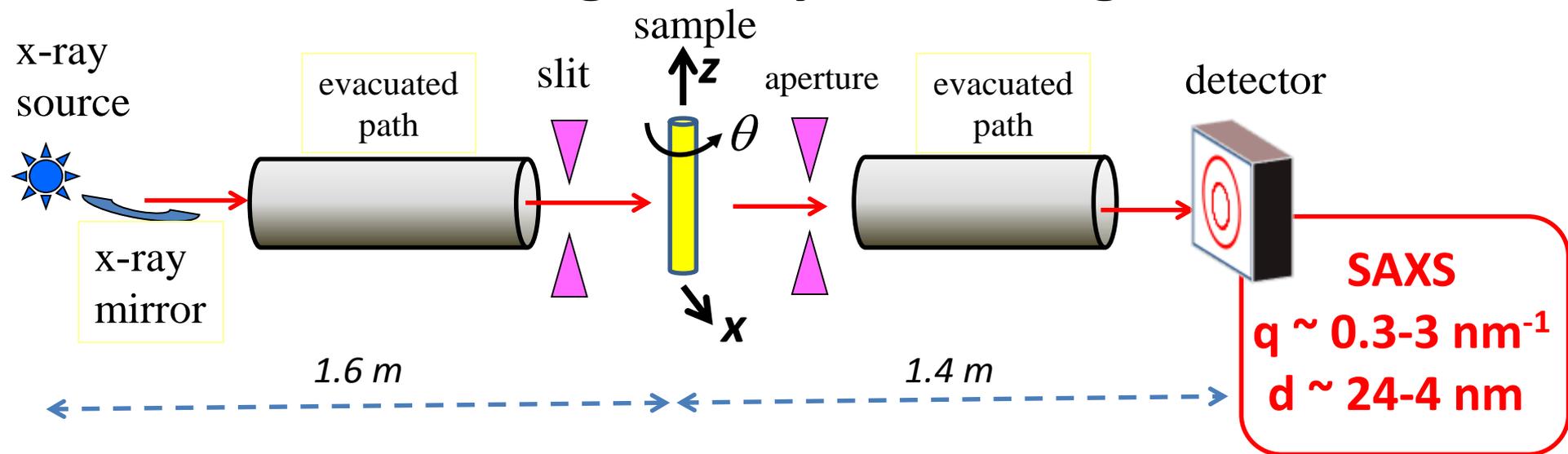
Small angles... large things...



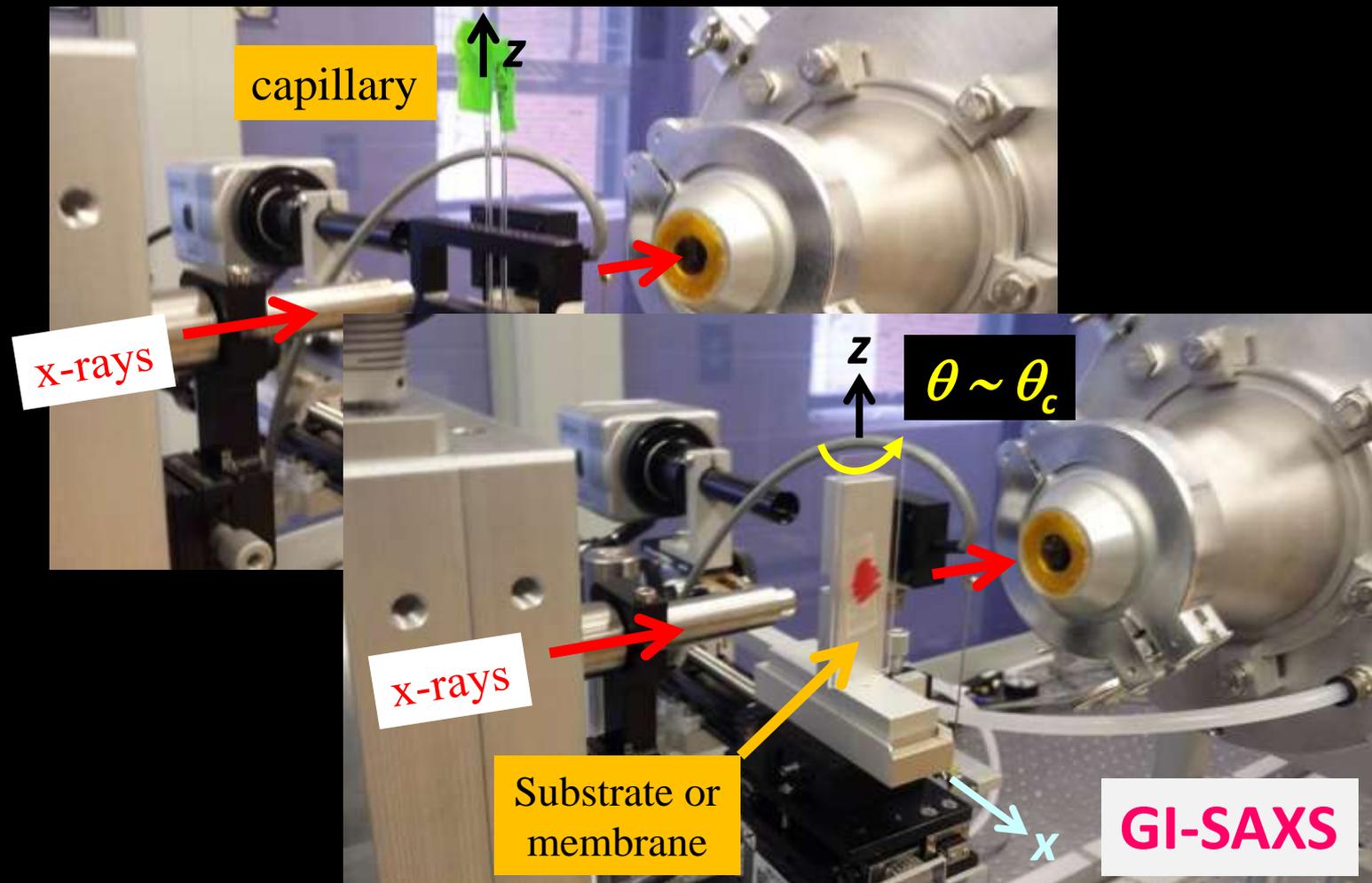
# SAXS instrument



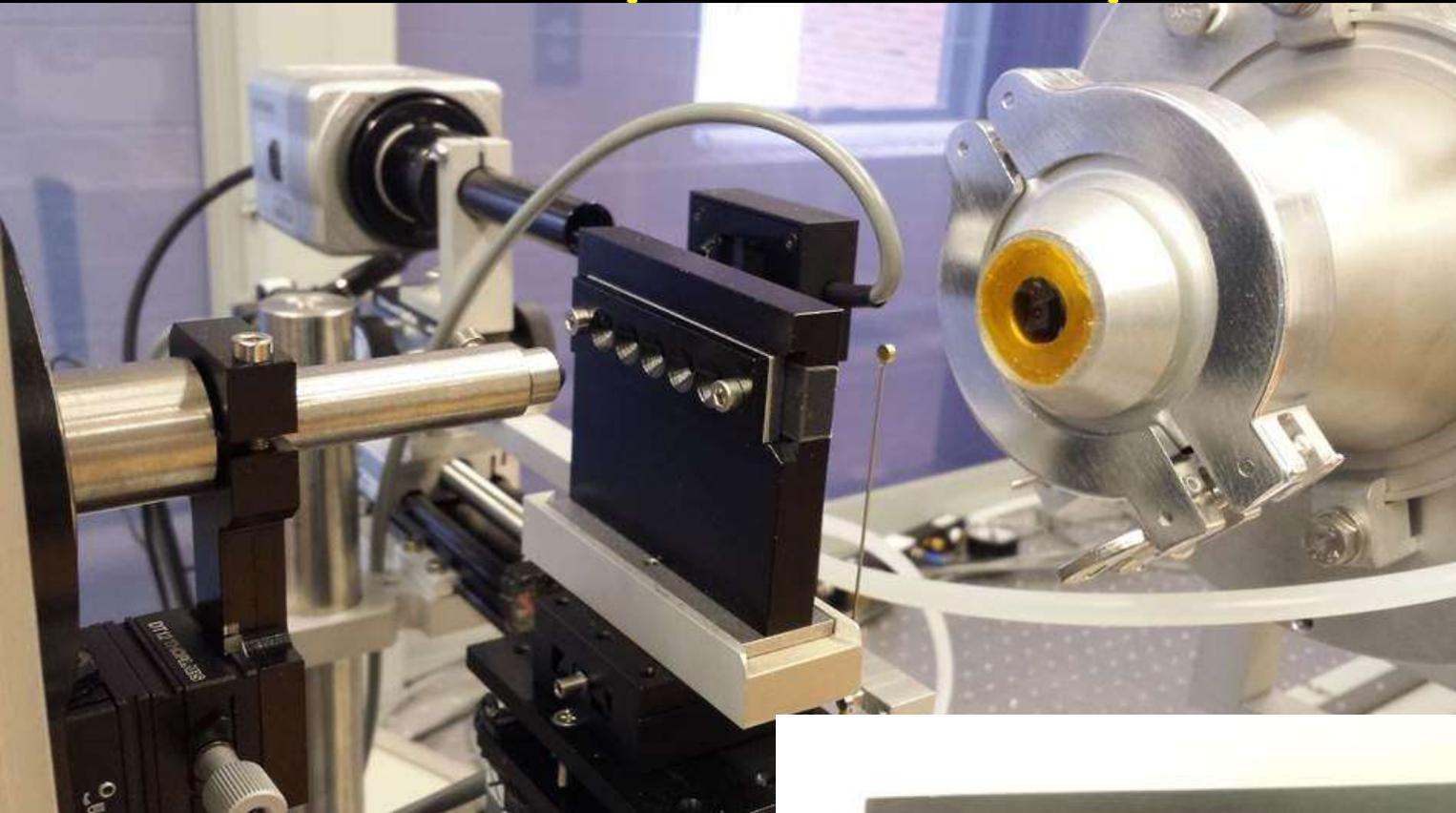
# Small angle x-ray scattering



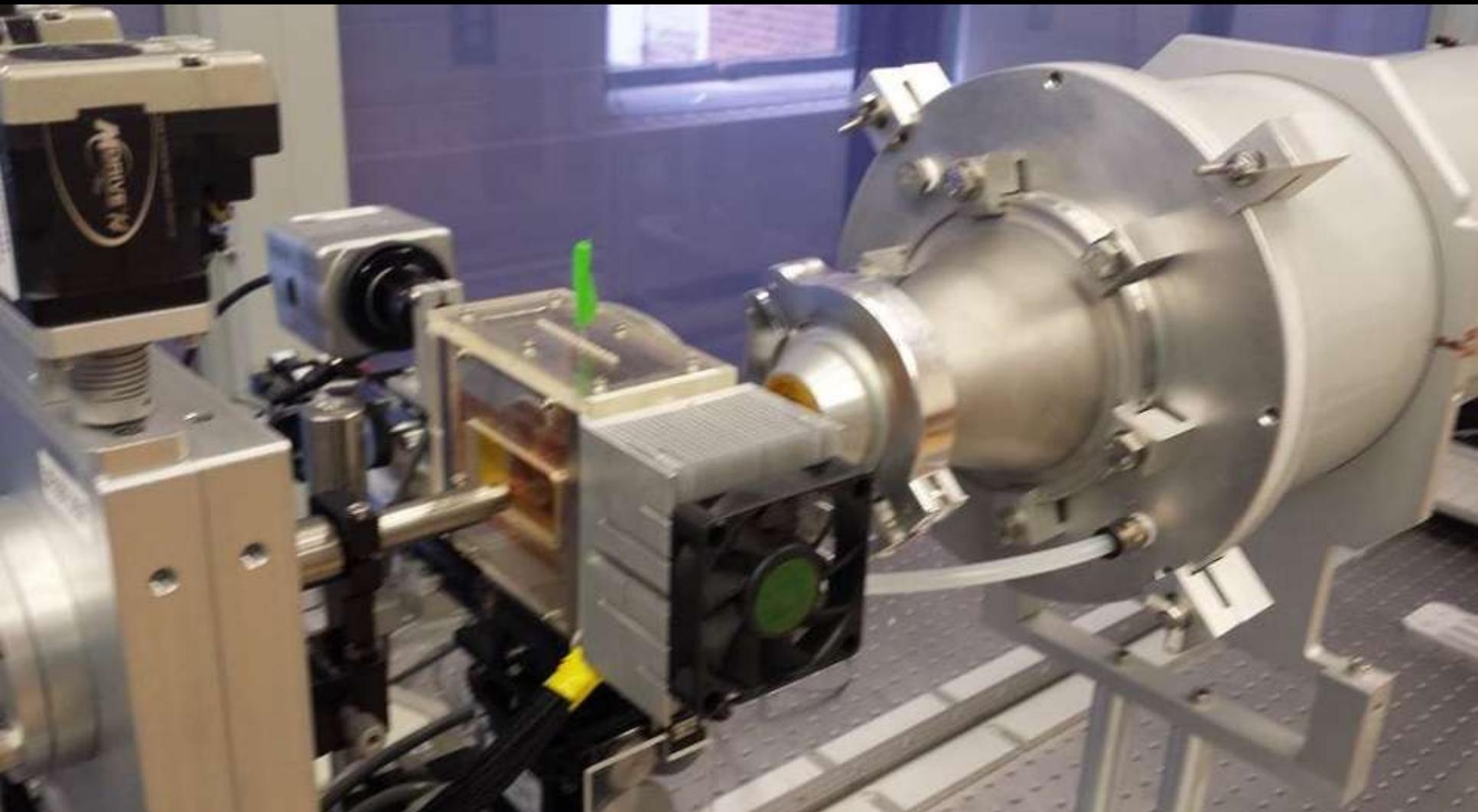
# SAXS and GI-SAXS



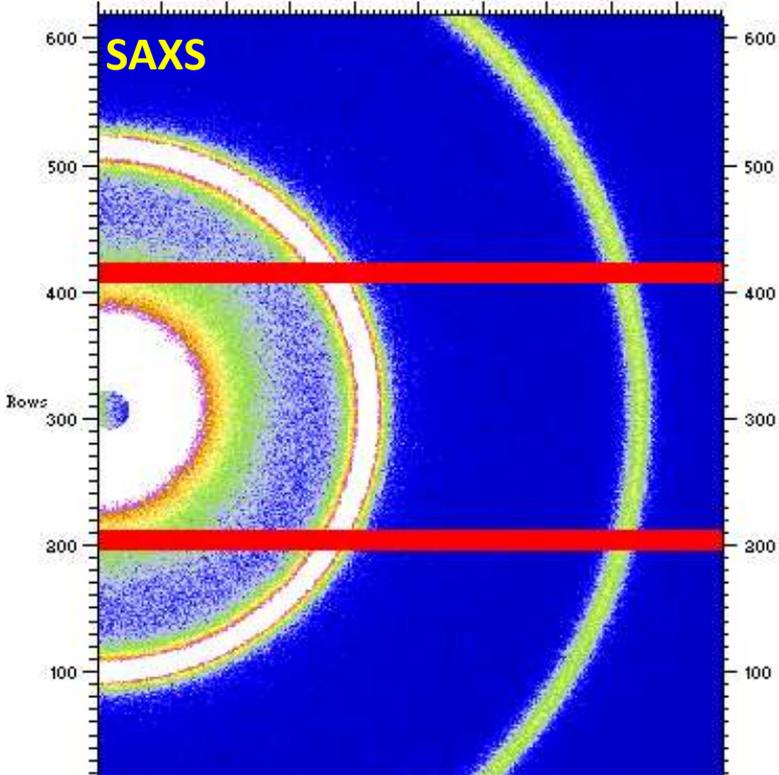
# Sample holder for powders



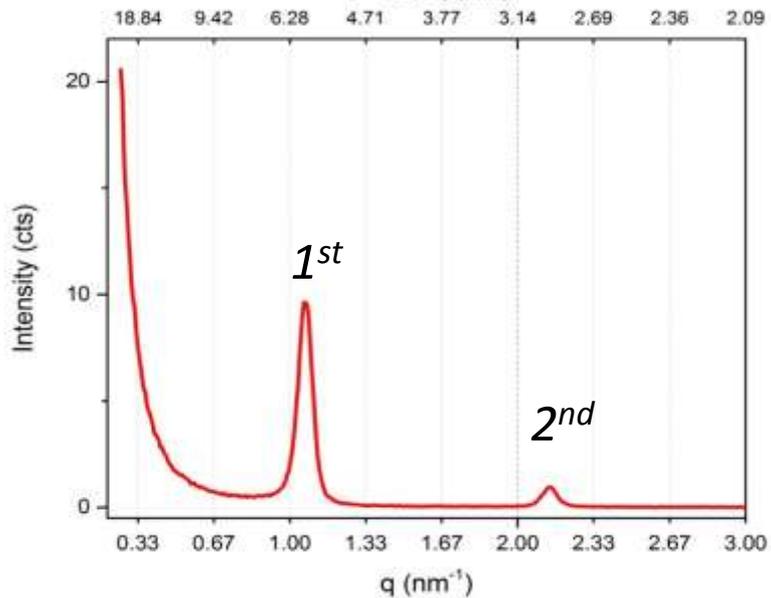
# Temperature control stage for capillaries



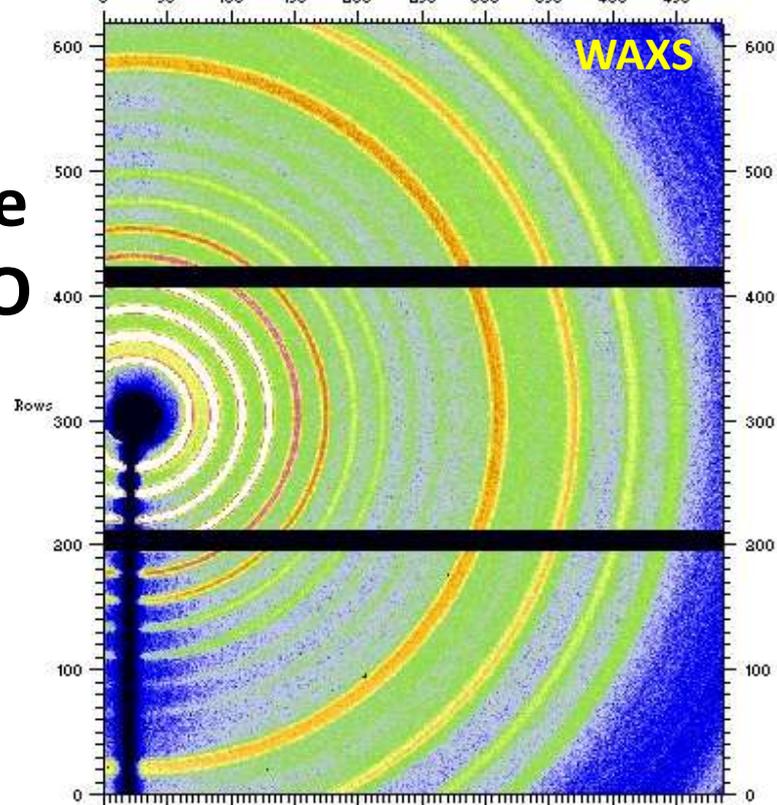
-20°C up to 120°C



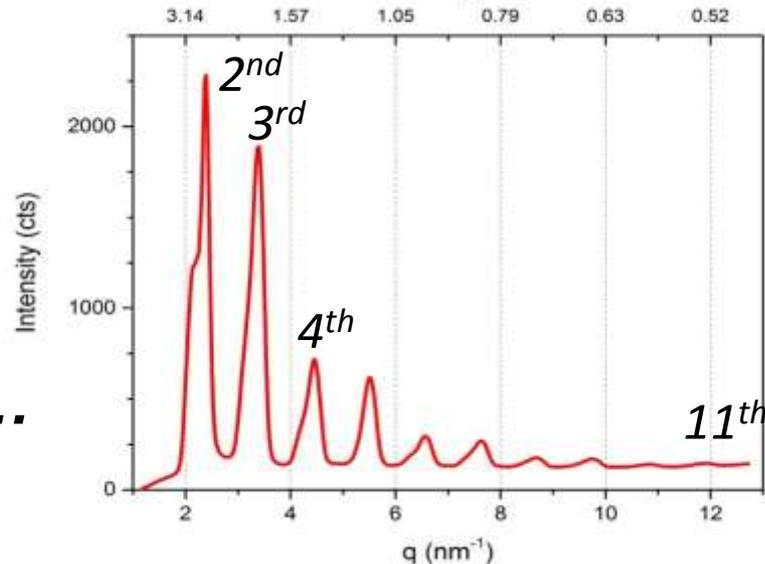
$d = 2\pi / q$  (nm)



**Silver behenate**  
**AgC<sub>22</sub>H<sub>43</sub>O**



$d = 2\pi / q$  (nm)



$$\frac{q_n}{q_1} = 1, 2, 3, 4 \dots$$

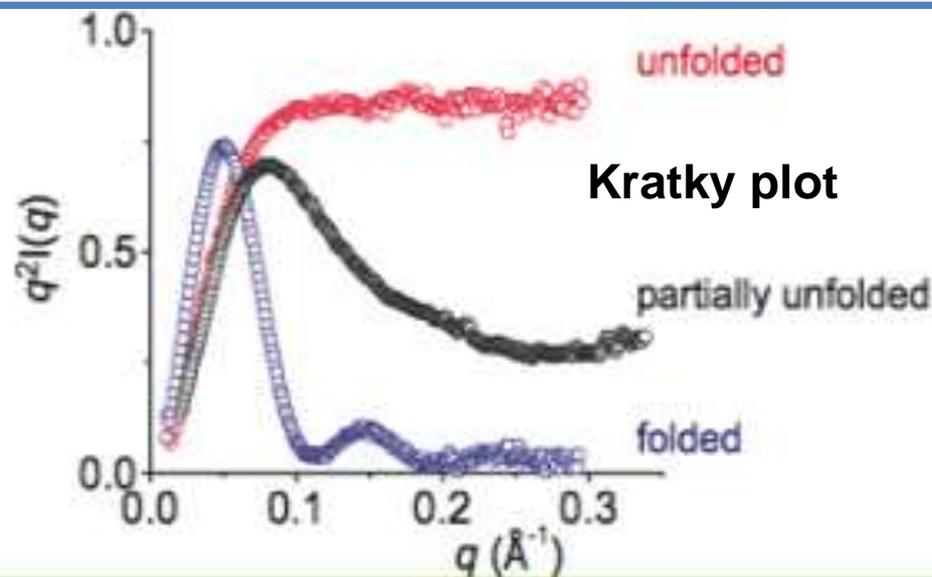
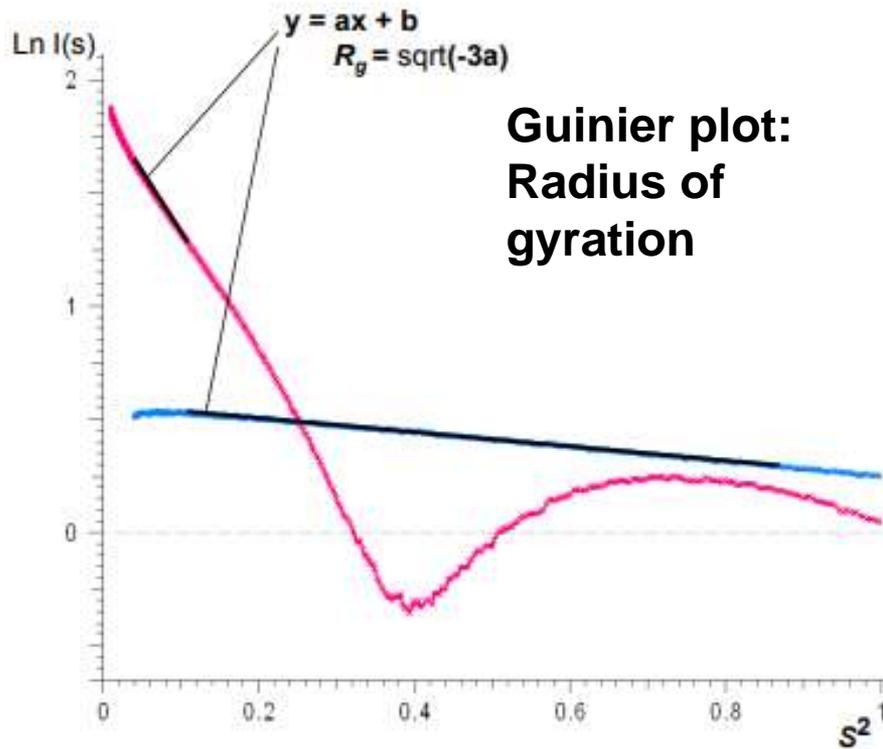
**lamellar**

# SAXS applications:

## Analysis:

- Crystalline structure
  - Degree of crystallinity and orientation
  - Particle shape, size, distribution
  - Radius of gyration
- Guinier plot  $\ln I(q)$  vs.  $q^2$
- Folded, partially or unfolded proteins
- Kratky plot  $I(q)*q^2$  vs.  $q$
- Distance distribution function  $p(r)$

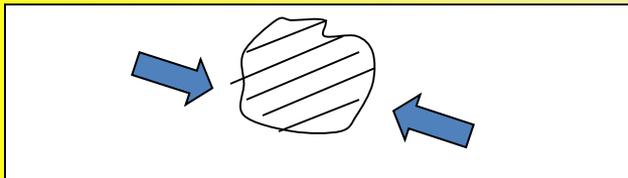
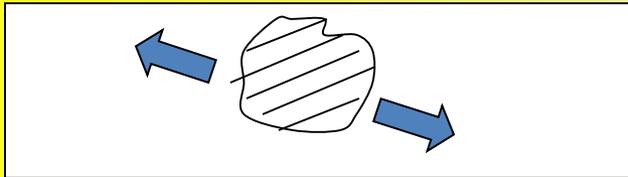
## Guinier plot: Radius of gyration



## Materials:

- Nanoparticles
- Membranes
- Lipids
- Polymers
- Proteins
- Solutions
- Nanocomposites
- Polymers
- Thin films ...

# Residual stress analysis methods



Residual stress?

How much? (MPa – GPa)

Type?

Direction (s)?

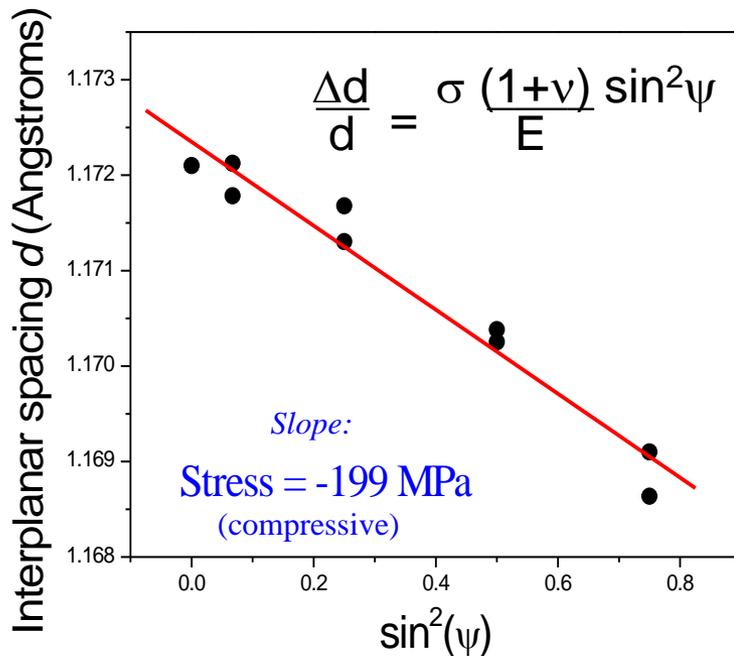
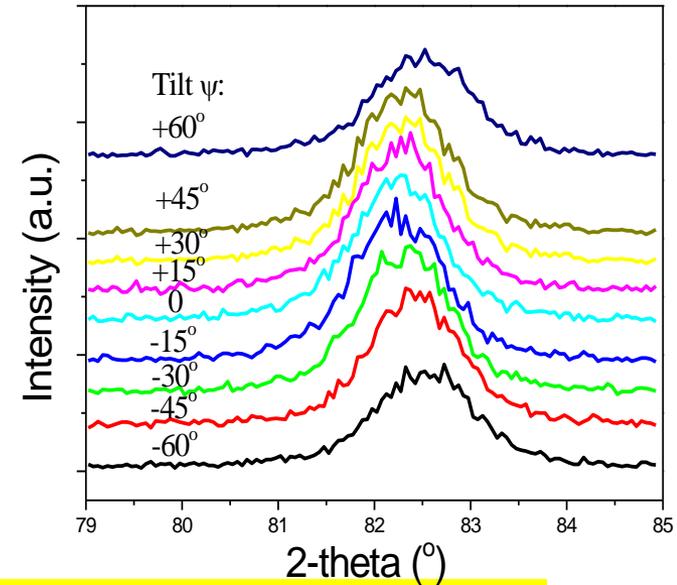
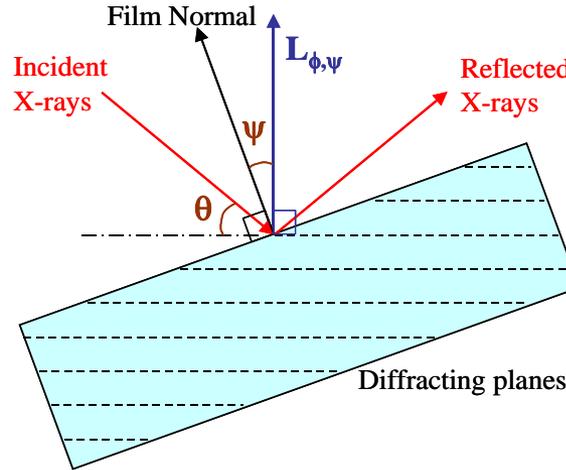
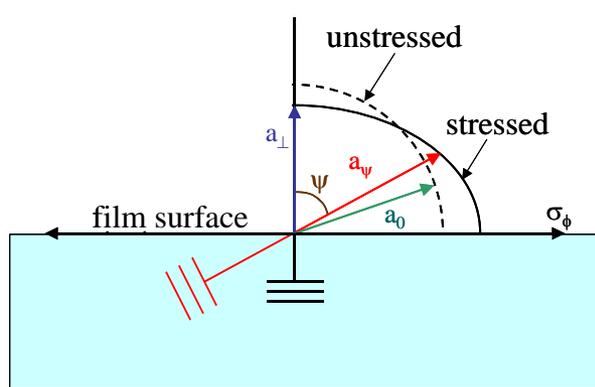
Stress gradients?

XRD measures strain ( $\Delta d$ )

*Hooke's law*  
→  
*Elastic properties ( $E, \nu$ )*

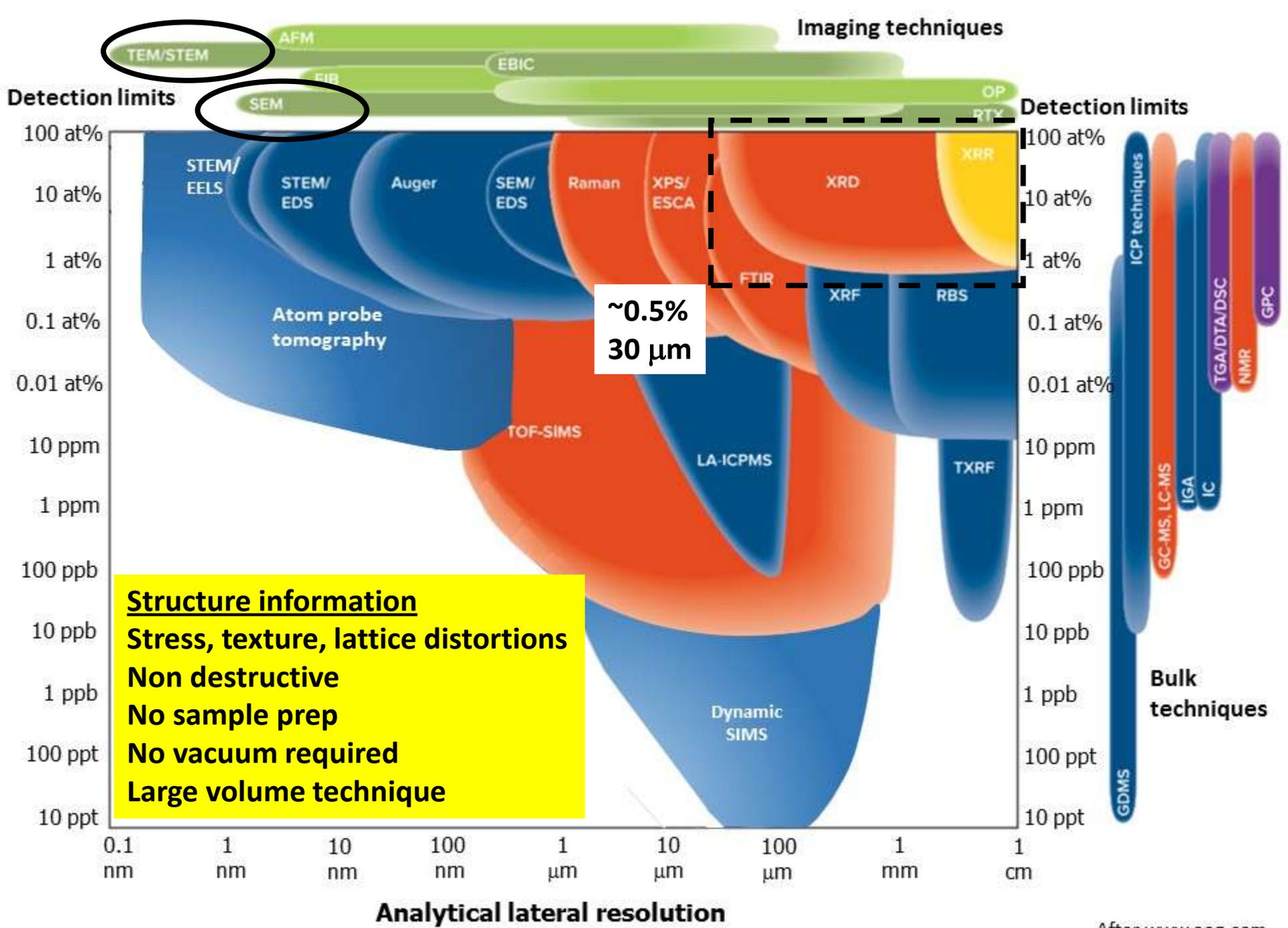
Stress tensor

# X-ray analysis of residual stress



Stress results from a steel sample  
Data: Sangid et al, UIUC

- Quantification of residual stress.
- Compressive (-) and tensile (+) stress.
- Crystallographic orientation of stress.
- **Sin<sup>2</sup>ψ** method. Linear for rotationally symmetric biaxial stress where the only non-zero components are  $\sigma_{11} = \sigma_{22} = \sigma_{//}$
- **ψ** and **ω** scan methods.
- **Glancing angle method (texture)**.
- Determination of stress tensor.
- Requires crystallinity (no amorphous).



TEM/STEM

SEM

AFM

FIB

EBIC

OP

RTY

100 at%  
10 at%  
1 at%  
0.1 at%  
0.01 at%  
10 ppm  
1 ppm  
100 ppb  
10 ppb  
1 ppb  
100 ppt  
10 ppt

100 at%  
10 at%  
1 at%  
0.1 at%  
0.01 at%  
10 ppm  
1 ppm  
100 ppb  
10 ppb  
1 ppb  
100 ppt  
10 ppt

0.1 nm 1 nm 10 nm 100 nm 1 μm 10 μm 100 μm 1 mm 1 cm

STEM/  
EELS

STEM/  
EDS

Auger

SEM/  
EDS

Raman

XPS/  
ESCA

XRD

XRR

Atom probe  
tomography

TOF-SIMS

LA-ICPMS

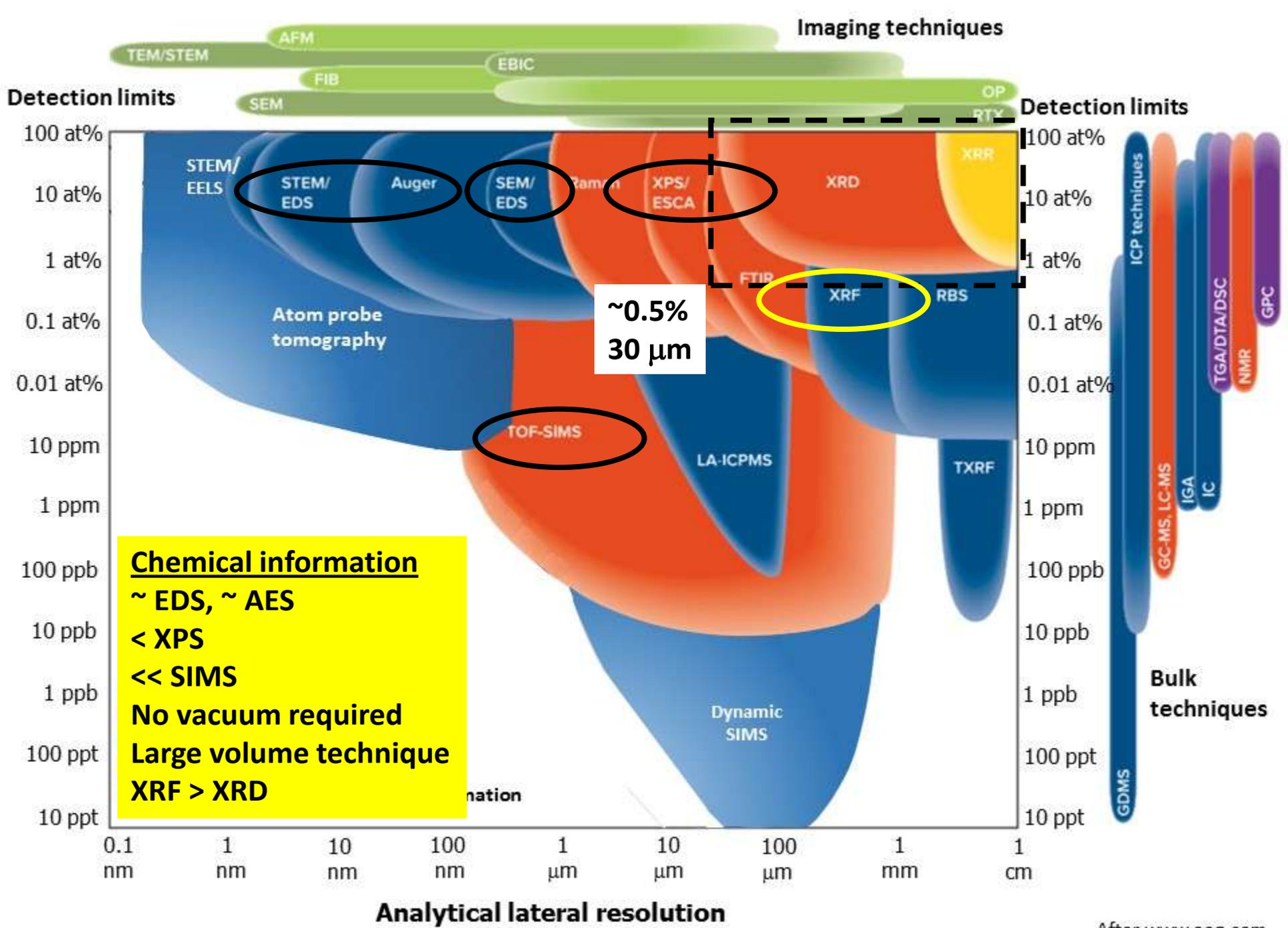
FTIR

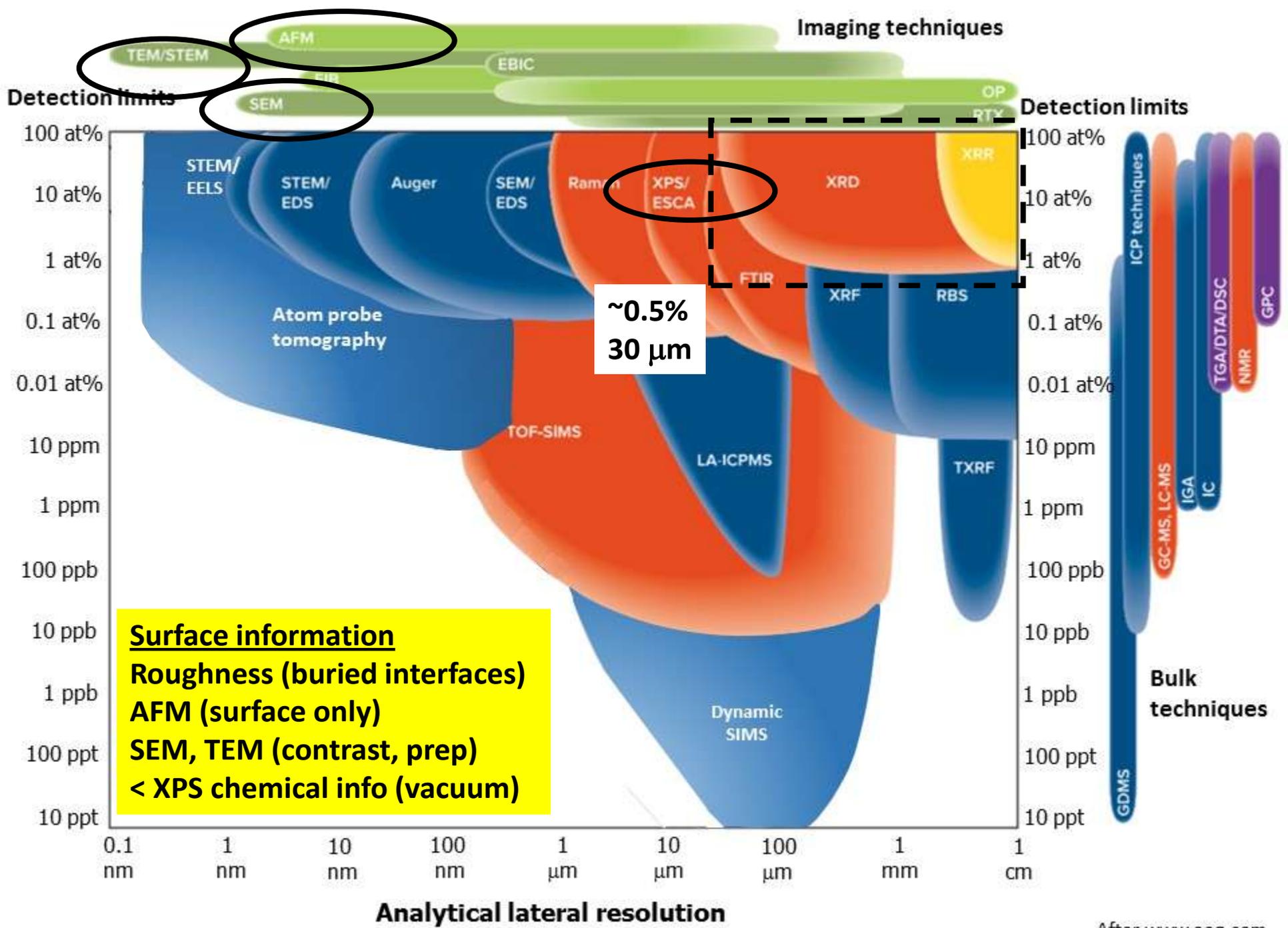
XRF

RBS

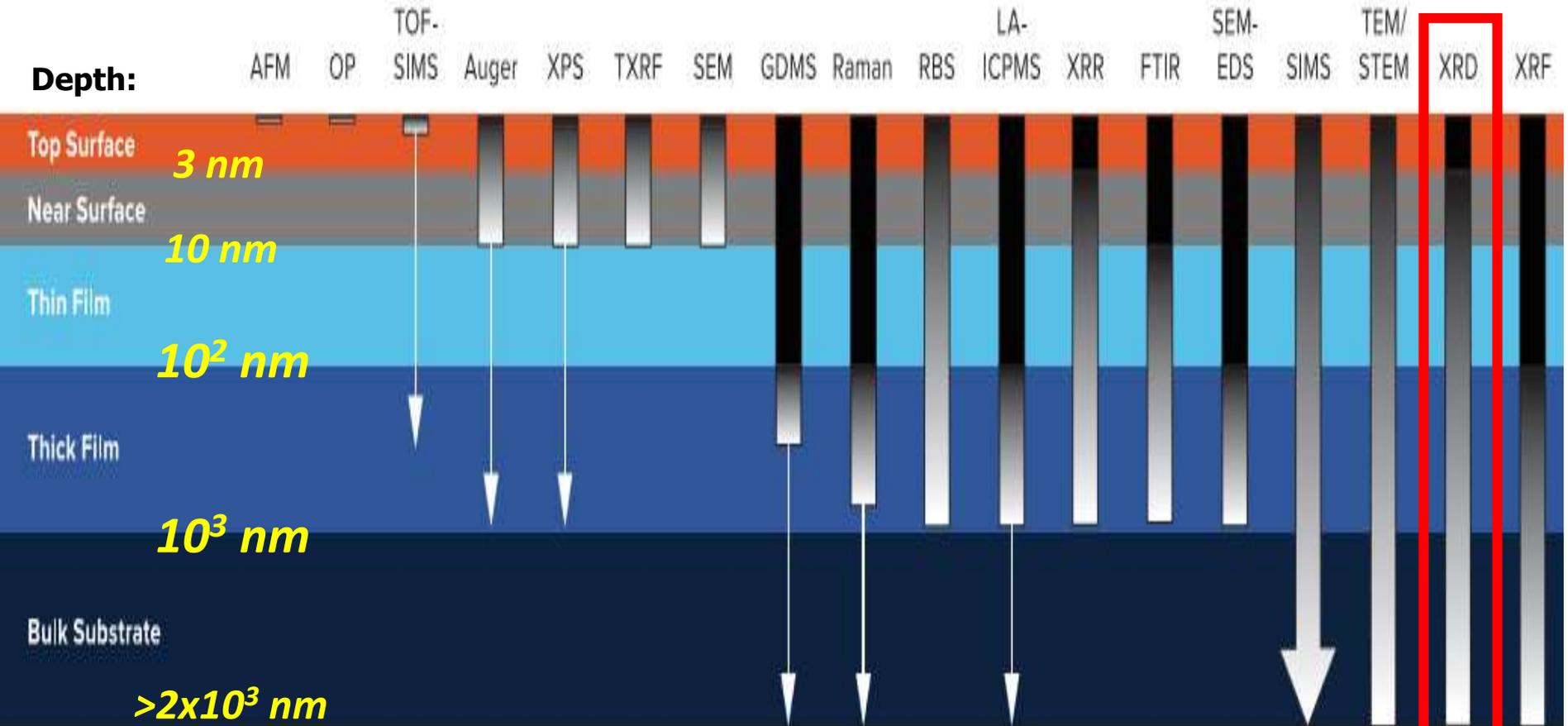
TXRF

ICP techniques  
GC-MS, LC-MS  
IGA  
IC  
TGA/DTA/DSC  
NMR  
GPC  
GDMS

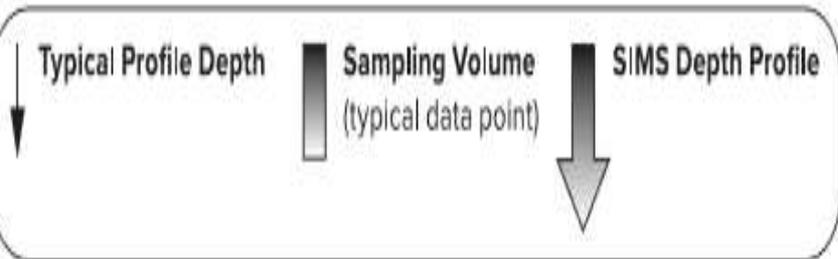




# Typical analysis depth for common analytical techniques



**GI-XRD can reduce depth**



# X-ray analysis summary

(+)

Non destructive

Quantitative

Finger printing (chemical info)

Very accurate crystalline structure info

Averages over large volume ( $\sim 30 \mu\text{m} \times 0.5\text{-}2 \text{ cm's}$ )

Levels of complexity: simple to complex

Microdiffraction, pair distribution function, fast areal detectors

(-)

Localized info (below  $100 \mu\text{m}$ )

Defects identification and quantification

Direct imaging

