

OUTLINE for AE 514, Boundary Layer Theory, Spring 2013; Jackson

1. Governing Equations
 - (a) Derivation of Reynold's Transport Theorem
 - (b) Derivation of Governing Equations
 - (c) Scalings
 - (d) Role of Reynolds Number in Boundary Layer Theory and the Concept of a Boundary Layer
2. Mathematical Theory of Boundary Layers
 - (a) Theory of Matched Asymptotic Expansions
 - (b) Inner and Outer Solutions, Matching
 - (c) Higher-order Matching
3. Potential Flow Theory - Outer Region
 - (a) Complex Variables
 - (b) Complex Velocity
 - (c) Ideal Fluid Flow - uniform flow, stagnation-point flow; point source; vortex; doublet; flow past a cylinder
4. Incompressible Theory
 - (a) Two-dimensional theory
 - (b) Derivation of the Blasius Boundary Layer
 - (c) Derivation of the Falkner-Skan profile
 - (d) Shear layers and Wakes
 - (e) 2-D Jet
 - (f) Boundary layers with suction/blowing; asymptotic suction profile
 - (g) Numerical methods - shooting methods, finite difference methods
 - (h) Keller Box Method for non-self similar boundary layers
 - (i) Three-dimensional boundary layers
5. Stability Theory
 - (a) Origin of Turbulence
 - (b) Introduction to Stability Theory
 - (c) Derivation of the Orr-Sommerfeld and Rayleigh Equations
 - (d) Absolute/Convective Stability
 - (e) Kelvin-Helmholtz theory
 - (f) Temporal Stability of Continuous Profiles

- i. Rayleigh Inflection Point Theorem
 - ii. Fjortoft's Theorem
 - iii. Plane Poiseuille Flow
 - iv. Plane Couette Flow
 - v. Shear Layers
 - vi. Boundary Layers
 - vii. Discrete and Continuous Spectra
- (g) Spatial Stability of Continuous Profiles
 - i. Shear Layers
 - ii. Boundary Layers
 - iii. Discrete and Continuous Spectra
- 6. Turbulence for Incompressible Flows
 - (a) Fluctuations and Correlations
 - (b) Prandtl Mixing Length Theory
 - (c) Reynolds Shear Stress and Scaling
 - (d) Rough Wall Turbulent Boundary Layers
- 7. Compressible Theory
 - (a) Introduction to Compressible Flows
 - (b) 2-D Boundary Layers
 - (c) Hypersonic Theory
 - (d) Boundary Layer Interactions
 - (e) Mangler Transformation
 - (f) Unsteady Boundary Layer Behind Moving Shock
 - (g) Stability
 - i. Compressible Shear Layer
 - ii. Compressible Boundary Layer