IE 514: Optimization Methods for Large-scale Network-based Systems

Credit hours: 4 Instructor: Lavanya Marla

Topical Outline:

- 1. Shortest paths on acyclic networks, labeling algorithms
- 2. Generalized shortest paths and labeling algorithms
- 3. Multi-commodity flows (and differences from the minimum-cost network flow problem)
 - a. Column generation (relation to duality)
 - b. Branch-and-price
 - c. Branch-and-price and cut
 - d. Decomposition techniques (Dantzig-Wolfe decomposition etc.) and related solution methods
- 4. Lagrangean relaxation, formulations and solution techniques
- 5. Airline Schedule Planning models Set-covering and set-partitioning problem formulations
 - a. Case study: Crew Scheduling
 - b. Composite variable modeling
 - c. Solution techniques with adapted column generation
- 6. Airline Schedule Planning models composite variable modeling
 - a. Case study: Airline Fleet Assignment
 - b. Composite Variable modeling with multiple types of composites
 - c. Combining multiple multi-commodity flow formulations
- 7. Data-driven Modeling
 - a. Case study: Ambulance Allocation
 - b. Simulation-optimization framework
 - c. Submodular problem formulations
- 8. Large-Scale neighborhood search
 - a. Case study: Vehicle routing and metaheuristics using large-scale neighborhood search
- 9. Stochastic modeling in large-scale integer programs
 - a. Brief introduction to stochastic programming
 - b. Case study: Stochastic Crew Scheduling
- 10. Robust Optimization for integer programs
 - a. Network flow modeling using worst-case modeling
- 11. Distributionally Robust Optimization
- 12. Operational Learning
 - a. Case study: Big Data Newsvendor problem

The course will present the concepts through real-world case-studies drawn from airline schedule planning, freight and last-mile logistics, emergency systems, vehicle routing and newsvendor problems.

Required Textbooks:

- 1. Network Flows: Theory, Algorithms and Applications, by Ravindra K. Ahuja, Thomas L. Magnanti and James B. Orlin First Edition Partially available online
- 2. Column Generation, by Guy Desaulniers at al (e-book available through UIUC libraries, <u>https://vufind.carli.illinois.edu/all/vf-uiu/Record/13561817</u>)
- Stochastic Optimization Anton J. Kleywegt and Alexander Shapiro a. <u>http://www2.isye.gatech.edu/~anton/stochoptiebook</u>

Learning assessments (tentative):

Homeworks will incorporate smaller versions of real data extracted from consulting case-studies and students will be implementing models in Java/C++ and CPLEX.

Homeworks	25%
Mid-term	15%
Class project	60%