IE 598AC Syllabus Statistical Inference for Stochastic Systems with Long Memory

Instructor: Alexandra Chronopoulou

Office: 216D Transportation Building Email: achronop@illinois.edu Phone: (217) 300-0851 Class Time: T/Th 9:00AM - 10:20AM Office Hours: T/Th 2:00PM - 3:00PM (or by appointment)

Course Objective

The focus of this course is on the probabilistic and statistical properties of stochastic processes that exhibit long memory (or long-range dependence). Specifically, we will study limit theorems for processes with long-memory and consider the problems of parameter estimation and filtering in fully and partially observed stochastic systems with long-memory. Applications of these models will also be discussed, with a particular focus on Mathematical Finance.

By the end of this course, students will be able to:

- identify the presence of long-range dependence in time-series data
- use processes with long-memory as models in different applications.
- estimate parameters in such models.

Prerequisites

Master level course on Stochastic Processes, and ideally on Probability Theory.

References

- 1. Long-Memory Processes: Probabilistic properties and statistical methods (2013), Beran, J., Feng, Y., Ghosh, S., and Kulik, R., Springer.
- 2. Statistics for Long-Memory Processes (1993), Beran, J., Chapman and Hall.

Grading

50% Homework: There will be 2-3 homework assignments throughout the semester. 50% Paper Presentation: The students will be responsible for an in-class presentation of research paper(s) related to the topics discussed in class.

IE 598AC Topics

Main Topics:

- 1. Introduction to Long-Range Dependence (LRD): Origins, definition and applications.
- 2. Limit Theorems for Long-Memory Processes: Limit theorems for sums with finite moments (ARCH(∞), LARCH models); sample covariances; quadratic forms.
- 3. *Parameter Estimation for LRD Processes:* Heuristic estimation of long memory. Exact and approximate maximum likelihood (Whittle) method, Method of moments. Non-parametric methods (variations-based and wavelets).
- 4. Non-linear Models with LRD: Inference for partially observed models, LARCH and $ARCH(\infty)$ processes.
- 5. *Forecasting for Linear Processes:* Forecasting for fractional ARIMA and FEXP processes.
- 6. Simulation Methods for LRD Processes: Exact and approximate techniques for simulation: Wood-Chan algorithm, Wavelet approach, etc.
- 7. Application to Mathematical Finance: Long memory and rough stochastic volatility models.

Additional Topics (depending on students' interest):

- Continuous-time LRD processes: Fractional Brownian motion (definition/ properties), Fractional Ornstein-Uhlenbeck process.
- Drift estimation for linear fractional SDEs.
- Filtering for continuous-time LRD models.
- Applications to queuing theory with heavy-tailed input.